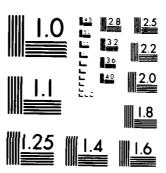
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UNSTEADY TRANSONIC PRESSURE MEASUREMENTS ON A SEMI-SPAN WIND TUNNEL MODEL OF A TRANSPORT-TYPE SUPERCRITICAL WING (LANN MODEL)

PART II: PRESSURE DISTRIBUTIONS (PLOTTED) AND PLOTS OF THE VIBRATION MODES



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March 1983 Final Report for Period April 1980 - April 1982

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This technical report has been reviewed and is approved for publication.

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to 0.2 at M = 0.95 (related to half mean aerodynamics)	mic chord).

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Part I of the report presents the general description, the aerodynamic coefficients (printed and plotted vs. incidence, reduced frequency and Mach number and the vibration modes.

Part II presents the plotted pressure distributions and vibration modes.

#### **FOREWORD**

AFOSR Grant 80-0136, "Transonic Wind Tunnel Measurements on a Supercritical Wing" was initiated by the Structures and Dynamics Division (FIB) of the Air Force Wright Aeronautical Laboratories (AFWAL). The objective of this effort was to obtain experimental data on a supercritical wing to guide improvements in transonic unsteady aerodynamics.

This effort was a part of a cooperative program involving <u>L</u>ockheed-Georgia, <u>Air Force</u>, <u>N</u>ASA, and <u>N</u>LR. This cooperative effort has become known as the LANN program.

The principal investigators at NLR were J. J. Horsten, R. G. den Boer, and R. J. Zwaan. The AFWAL project engineer was L. J. Huttsell and the work unit was 24010236.

Part I of this report presents the general description, the aerodynamic coefficients (printed and plotted vs incidence, reduced frequency, and Mach number) and the vibration modes. Part II presents the plotted pressure distributions and vibration modes. The pressure distributions in tabulated form can be obtained from AFWAL/FIBRC upon request.

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#### LIST OF SYMBOLS

Note: Coefficients derived from the zeroth harmonic component of unsteady pressure signals, are indicated simply as "steady" coefficients instead of "mean" coefficients. For a pure sinusoidal signal, there is principally no difference between steady and mean coefficients.

a.	modulus of pressure tube transfer function, $a = mod(p_u/p_i)$ (see section 3.1 and figure 6 in part I)
AR	aspect ratio, AR = 7.92
AC	aerodynamic center
c	local chord, m
c <sub>AC</sub>	mean aerodynamic chord, $c_{AC} = 0.268 \text{ m}$
c <sub>r</sub>	root chord, m
$c_{\mathbf{t}}$	tip chord, m
Cm	steady sectional pitching moment coefficient (see App. A)
Cmi	unsteady sectional pitching moment coefficient, $Cmi = Cm' + i Cm''$ (see App. A)
Cmq	quasi-steady sectional pitching moment coefficient (see App. A)
$^{\rm C}{}_{ m M}$	steady wing pitching moment coefficient (see App. A)
$^{\mathrm{C}}_{\mathtt{Mi}}$	unsteady wing pitching moment coefficient (see App. A)
$^{\mathrm{C}}$ Mq	quasi-steady wing pitching moment coefficient (see App. A)
Cpi	unsteady pressure coefficient, $Cpi = Cp' + i Cp''$ (see App. A)
$\mathtt{Cpi}_{\mathrm{T}}$	value of Cpi measured with in situ transducer, $\operatorname{Cpi}_T = \operatorname{p_i}_T / \operatorname{q_{\infty}\alpha_i} = \operatorname{Cp_T} + \operatorname{i} \operatorname{Cp_T}$
Cpm	steady pressure coefficient (see App. A)
Cpq	quasi-steady pressure coefficient (see App. A)
Cz	steady sectional normal force coefficient (see App. A)
Czi	unsteady sectional normal force coefficient, Czi = Cz + i Cz (see App. A)
Czq	<pre>quasi-steady sectional normal force coefficient (see App. A)</pre>
$c_{Z}$	steady wing normal force coefficient (see App. A)
$^{\mathrm{c}}_{\mathtt{Zi}}$	unsteady wing normal force coefficient, $C_{Zi} = C_Z^{\dagger} + iC_Z^{\prime\prime}$ (see App. A)
$c_{Zq}$	quasi-steady wing normal force coefficient (see App. A)

```
DZ
                   ratio of acceleration pick-up signal and LVDT
                   displacement signal, DZ = DZ' + i DZ"
DZ<sub>1</sub>
                   amplitude of LVDT displacement, mm
f, FREQ
                   frequency, Hz
harm, HARM
                   harmonic component (harm = 0: mean, harm = 1:
                   1st harmonic, harm = 2: 2nd harmonic)
                   \sqrt{-1}
i
                   reduced frequency, k = \pi f c_{\Lambda C}/V
k, REDFR.
M, Mach, MACH
                   free stream Mach number
                   steady sectional pitching moment about quarter-chord,
                   Nm/m (see App. A)
Mi
                   unsteady sectional pitching moment about quarter-chord,
                   Nm/m/rad (see App. A)
Miwing
                   unsteady wing pitching moment about aerodynamic center,
                   Nm/rad (see App. A)
M-LOC
                   local Mach number
M_{\perp 1}
                   quasi-steady sectional pitching moment about quarter-
                   chord, Nm/m/rad (see App. A)
^{\rm Mq}wing
                   quasi-steady wing pitching moment about aerodynamic
                   center, Nm/rad (see App. A)
\mathbf{M}_{\mathrm{wing}}
                   steady wing pitching moment about aerodynamic center,
                   Nm. (see App. A)
                   number of acceleration pick-ups, N_m = 12
N_{\rm m}
                   number of pressure tubes at each section, N_{\rm p} = 40
                   number of sections, N_s = 6
Ns
                   number of transducers, N_{\rm TP} = 1a
N
                   pressure at model surface, p = p_m + p_i, Pa
p
p, P-SETTL.
                   stagnation pressure, Pa
                   nth harmonic component of unsteady pressure at model
P_i
                   surface, p_i = [p_i] \exp[i(\omega t)], Pa (see Fig. 6 in part I)
\mathbf{p_{i}}_{\mathbf{T}}
                   value of p; measured with in-situ transducer
                   mean pressure, Pa
P_{m}
\mathbf{p}_{\mathbf{q}}
                   amplitude of quasi-steady pressure oscillation,
                   p_{\alpha} = [p_{m}(\alpha_{m} + \Delta \alpha) - p_{m}(\alpha_{m} - \Delta \alpha)]/2, Pa
                   nth harmonic component of unsteady pressure at the end
{\tt P}_{u}
                   of a pressure tube, p_{ij} = [p_{ij}] \exp[i(\omega t + \phi)], Pa (see Fig. o
                   in part I)
                   free-stream dynamic pressure, Pa
q_, Q
```

```
Reynolds number, Re = Vc_{AC}/v
Re, RE
                   semi-span, s = 1.000 m
s
S
                   wing surface, S = 0.2526 \text{ m}^2
                   airfoil thickness, m
                   time, s
                   model temperature, deg cent.
T-SETTL.
                   stagnation temperature, deg cent.
                   free-stream velocity, m/s
WRP
                   Wing Reference Plane (see Fig. 1) (X-y plane)
                  x = X-X_{leading}
\mathbf{x}_{\mathrm{tr}}
                   x-coordinate of boundary layer transition strip
χ
                   coordinate in free-stream direction, m (see Fig. 1)
                   X-coordinate of rotation axis, m (see Fig. 1)
Xr
                   spanwise coordinate, m (see Fig. 1)
У
                   coordinate normal to the X-y plane, m
                   steady sectional normal force, N/m (see App. A)
7.i
                   unsteady sectional normal force, N/m/rad (see App. A)
^{\mathrm{Zi}}wing
                   unsteady wing normal force, N/rad (see App. A)
Zq
                   quasi-steady sectional normal force, N/m/rad (see App. A)
^{\mathrm{Zq}}wing
                   quasi-steady wing normal force, N/rad (see App. A)
z_{\rm wing}
                   steady wing normal force, N (see App. A)
\alpha, alpha, ALFA wing incidence at LVDT position, \alpha = \alpha_m + \alpha_i, acg
                   unsteady wing incidence at LVDT position,
αi
                   \alpha_i = |\alpha_i| \exp(i\omega t) = \Delta \alpha \exp(i\omega t), deg
                   steady wing incidence at LVDT position, deg
Au, Dalpha, DALFA amplitude of unsteady wing incidence at LVDT position
                   \Delta \alpha = \{\alpha_i\}, \deg
                   phase of tube transfer function, \varphi = \arg (p_n/p_i)
φ
                   relative spanwise coordinate, \eta = y/s
η
10.25
                   sweep angle of quarter chord line, deg
                  kinematic viscosity (m<sup>2</sup>/s)
                   angular velocity, \omega = 2\pi f, rad/s
θ
                   local wing incidence, deg (see Fig. 1)
                   wing twist, 0 = \theta_t - \theta_r, deg (see Fig. 1)
0
```

- + upper z < 0 (see Fig. 1)</pre>
- lower z > 0 (see Fig. 1)
- ∞ free-stream

TABLE 1
Steady test program for LANN model (run numbers)

M a	0.62	0.72	0.77	0.82	0.87	0.95
-0.4	16	27	46	67	88	97
0.35	17			68		
0.60*)	15/19	28	47	69	89	98
0.85	18			70		
1.60	20	29	48	71	90	99
2.00	183			218		
2.35	235	238	240	132		155
2.50				219		
2.60*)	234	109	121	222/133		154
2.75				220	242	245
2.85	236	237	241	134		156
2.90				231		230
3.00*)	184			221	168	246
3.25			Í	223	244	247
3.50				224		
3.60	104/232	110	122	135		157
4.00				225	169	248
4.50				226		
4.75			201	205		
5.00*)	185	193	202	206		228
5.25			203	207		
5.50				227		ļ
6.00	186	194	204	208		229

<sup>\*)</sup> Steady incidences for which unsteady measurements were performed as well

TABLE 2
Unsteady test program for LANN model (run numbers)

	f	12	24	30	48	60	72
Δ	α	1.0	0.25	0.25	0.25	0.25	.025
α	М						
0.6	0.62	36	129/22	23	24	25	26
	0.72		30		31	32	33
	0.77	117	118	119	120	65	66
	0.82	83	73	77	85	86	87
	0.87	91	92	93	94	95	96
	0.95		100		101	102	103
2.6	0.62		105		106	107	108
	C.72	111	112	113	114	115	116
	0.77	123	124	125	12°C		128
	0.82	139	143	150	15.1	152	153
		) 					
3.0	0.72		165				
	0.77		166				
	0.82		167				
	0.07		170		171	172	173
	0.95	250	175	179	180	181	182
5.0	0.62	187	188	189	190	191	192
	0.72	195	196	197	198	199	200
	0.82	211	212	214	215	21€	217

TABLE 3

Test program for amplitude variation and higher harmonics

for LANN model (run numbers)

М	Q.	f	Δα harm	0.125	0.25	0.5	1.0
0.62	0.6	12	1	34	21	35	36
		24	1	37	22/39/129	42	
İ		24	2		40/130	43	
		24	3		41/131	44	
		36	1	45	23		
0.82	0.6	12	1		72	82	83
		24	1	78	73	79	
		24	2		74	80	
		24	3		75	81	
		36	1	76	77		
0.82	2.6	12	1	136	137	138	139
		24	1	140	143	146	
		24	2	141	144	147	
		24	3	142	145	148	
		36	1	149	150		
0.95	2.6	12	1		161	162	163
0.95	3.0	24	1		175	178	
		24	2		176		
		24	3		177		
0.82	5.0	12	1		209	210	211
		24	1		212	213	

TABLE 4
Miscellaneous runs for LANN-model

run number	Œ	М	f	Δα	harm
38	0.6	0.62	24.0	0.50	1
84	0.6	0.82	18.0	0.50	1
127	2.6	0.77	50.0	0.25	1
164	3.0	0.95	12.0	0.50	1
174	3.0	0.95	12.0	0.50	1
		}		 	
158	0.6	0.95	30.1	0.05	1
159	0.6	0.95	30.1	0.05	ڌ
160	0.6	0.95	30.1	0.05	3
253	4.0	0.00	12.0	0.25	1
254	4.0	0.00	24.0	0.25	1
255	4.0	0.00	36.0	0.25	1
256	4.0	0.00	48.0	0.25	1
257	4.0	0.00	60.0	0.25	1
258	4.0	0.00	72.0	0.2%	1

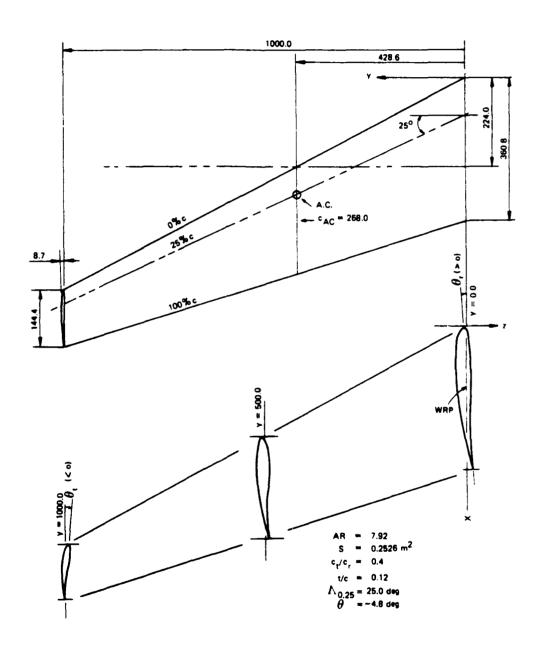
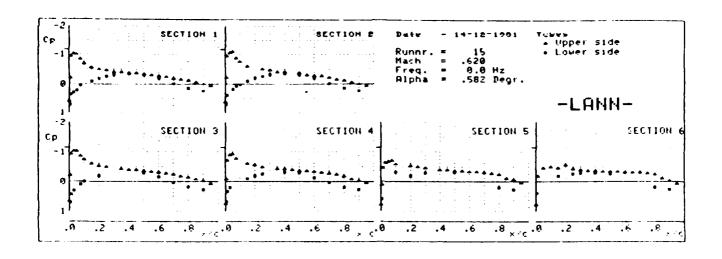
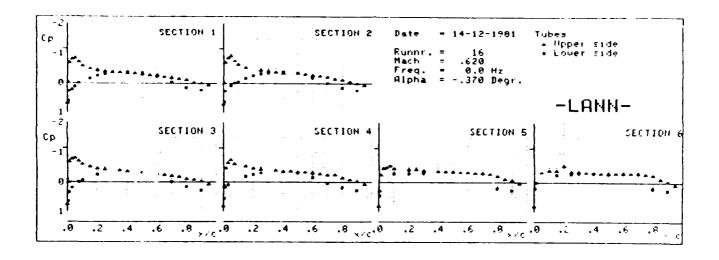
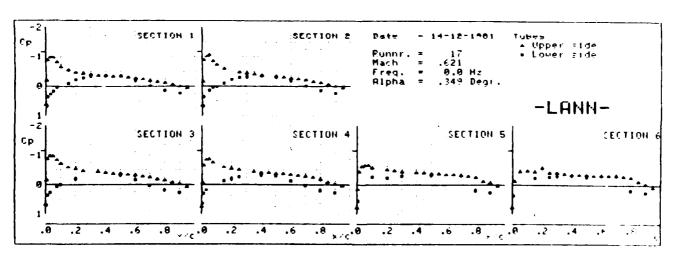
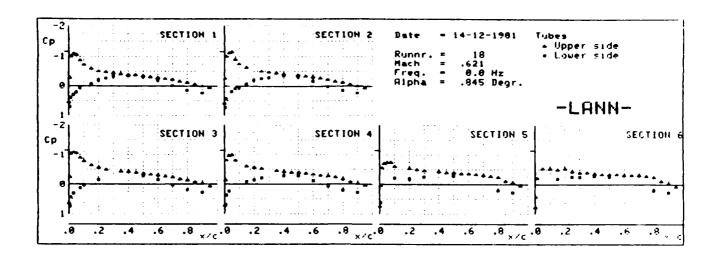


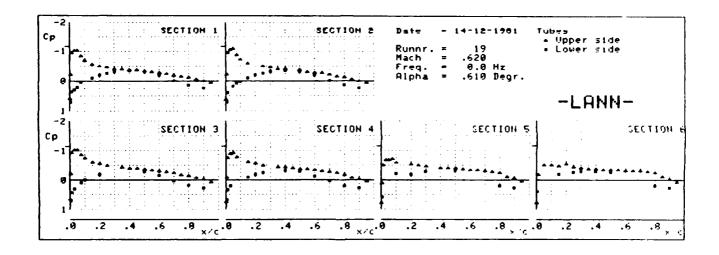
Fig. 1 Wing planform (dimensions in mm)

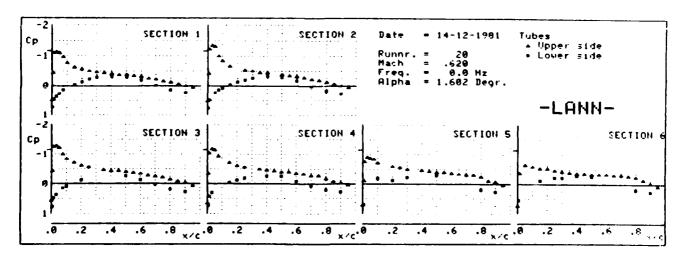


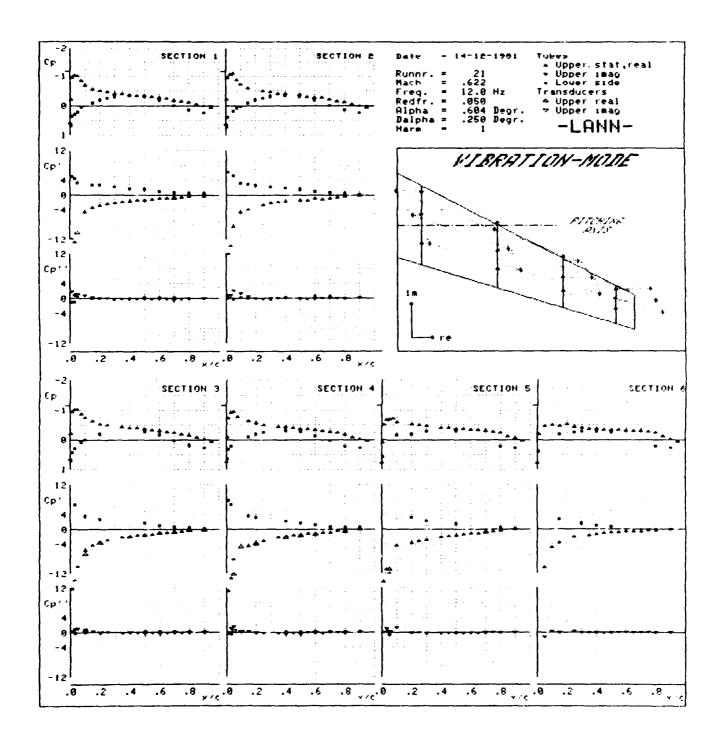


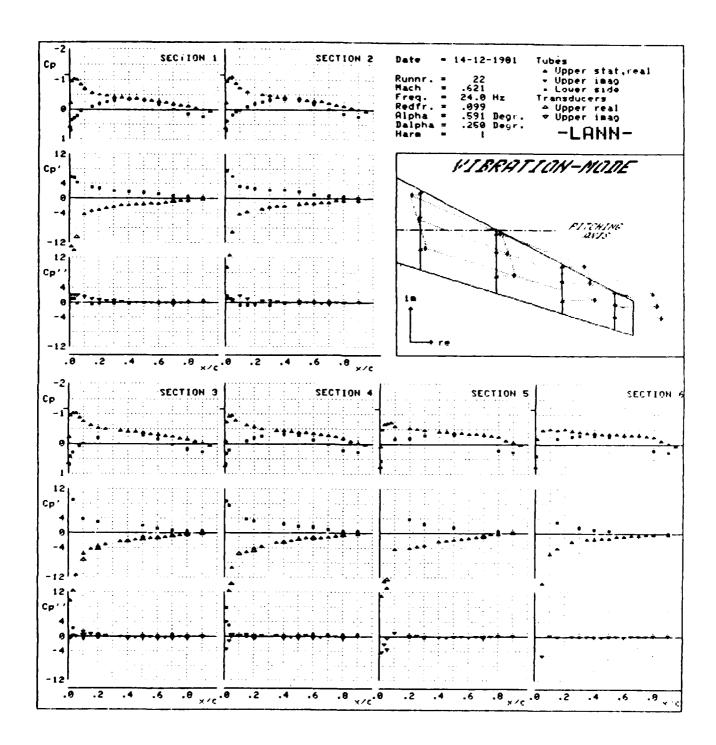


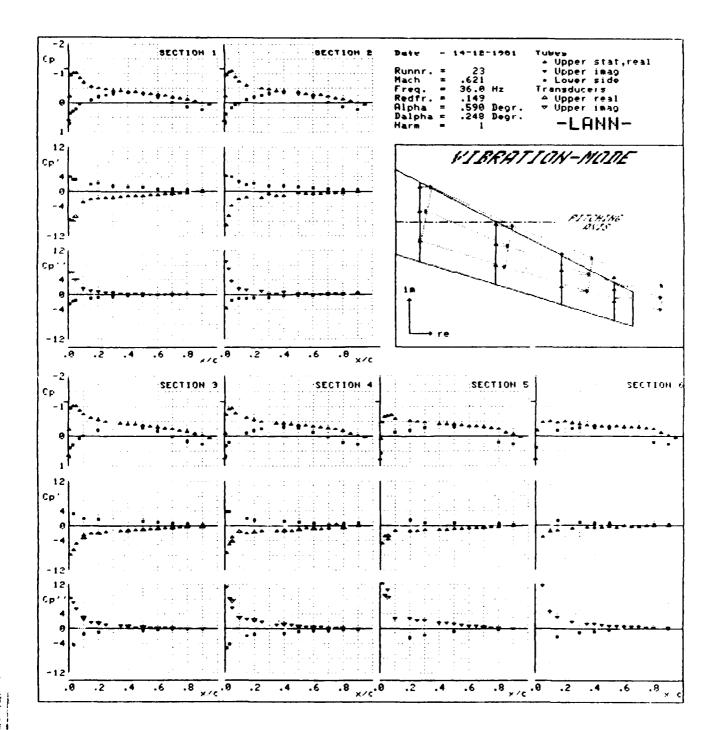


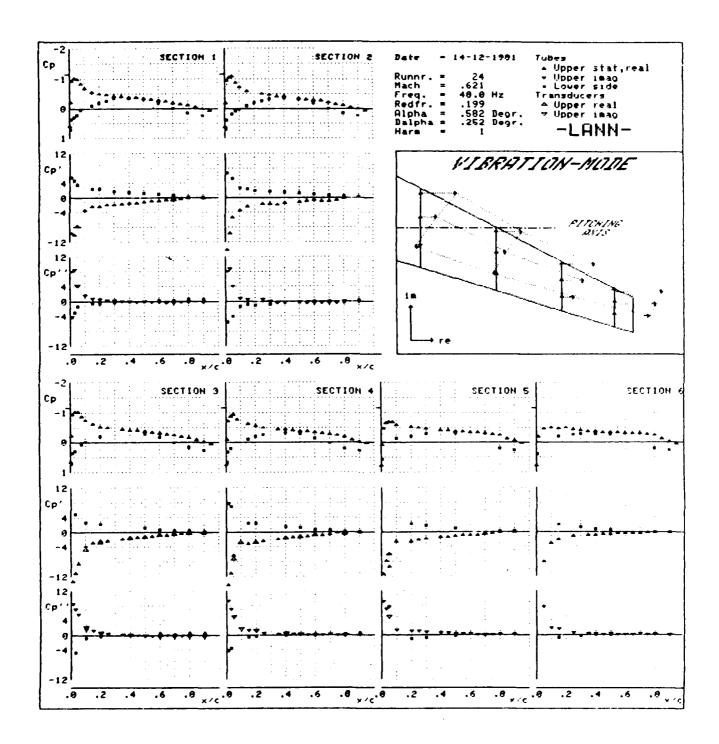


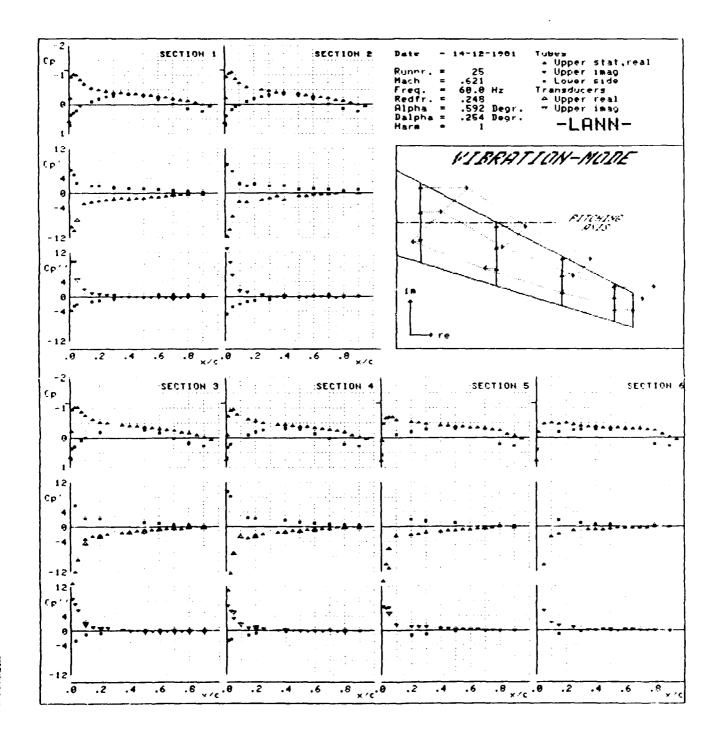


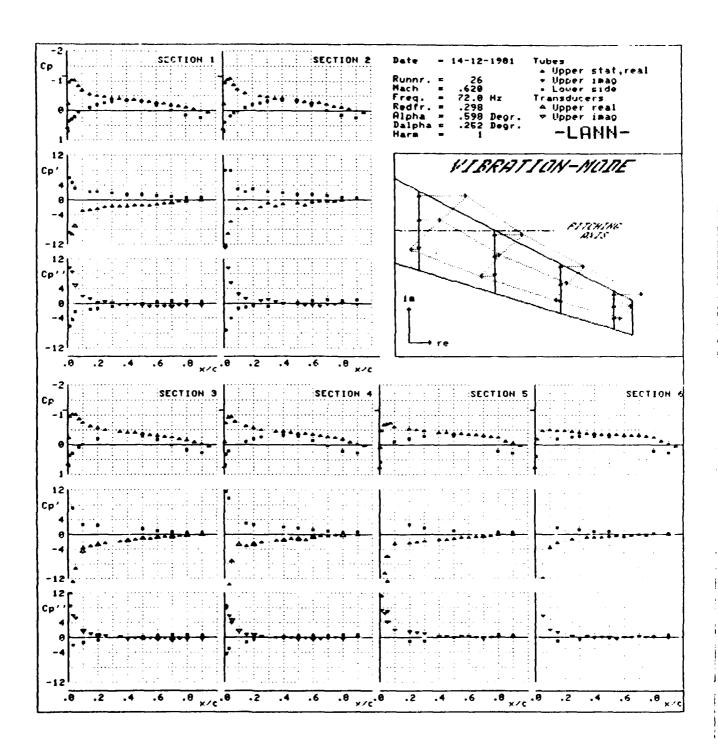


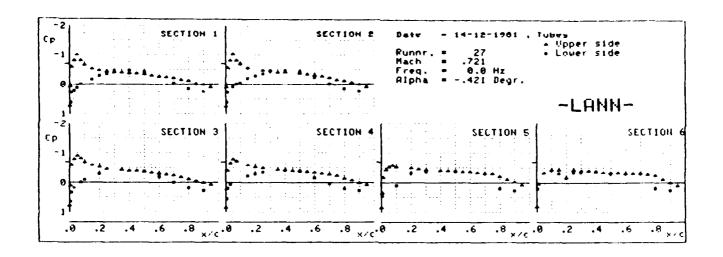


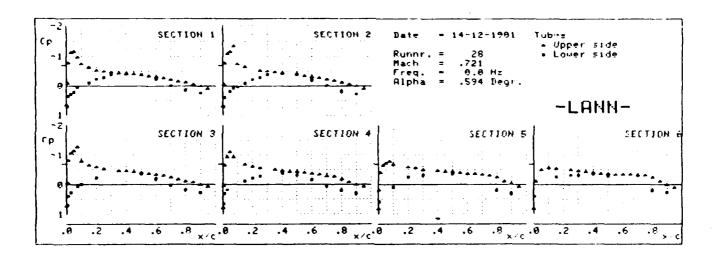


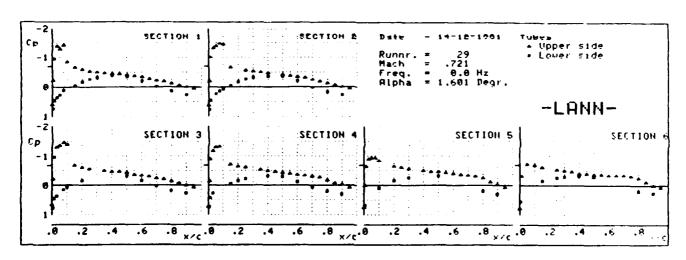


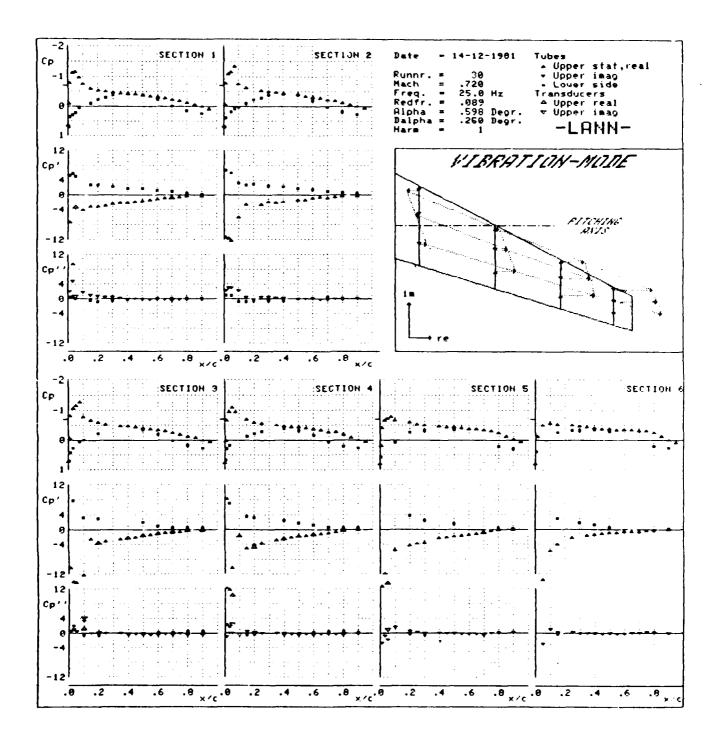


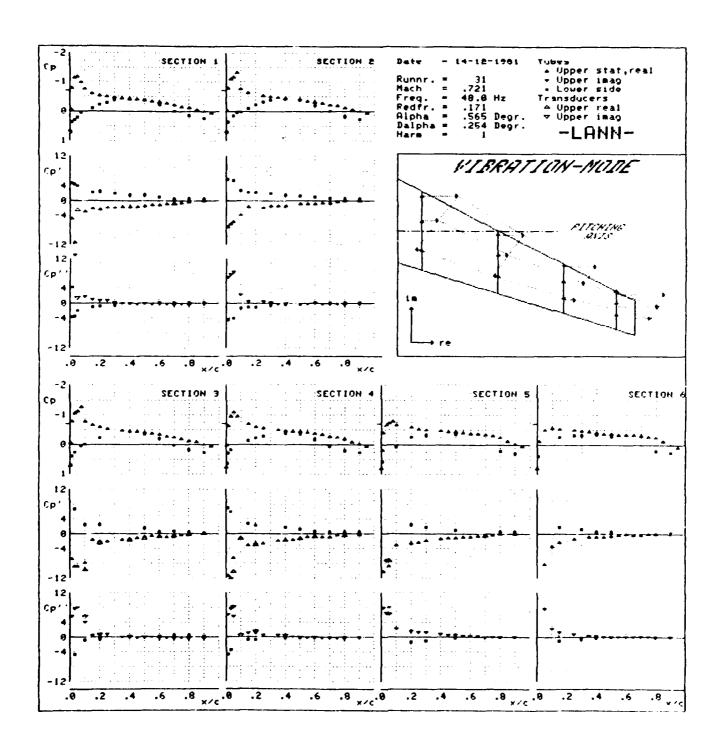


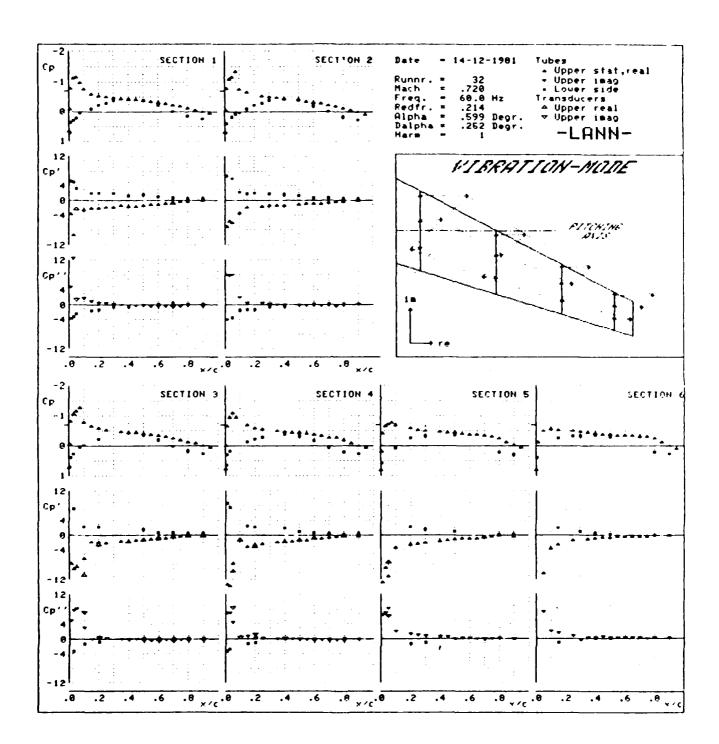


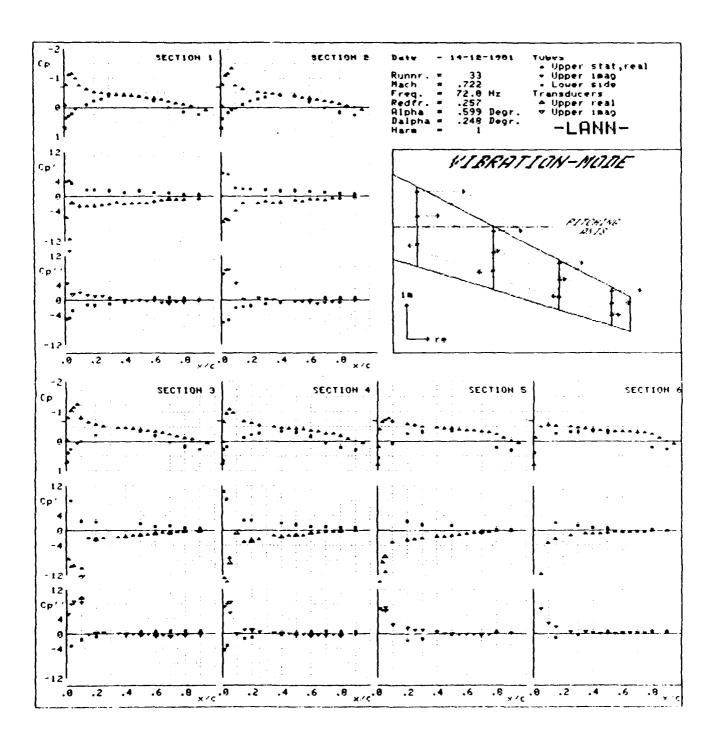


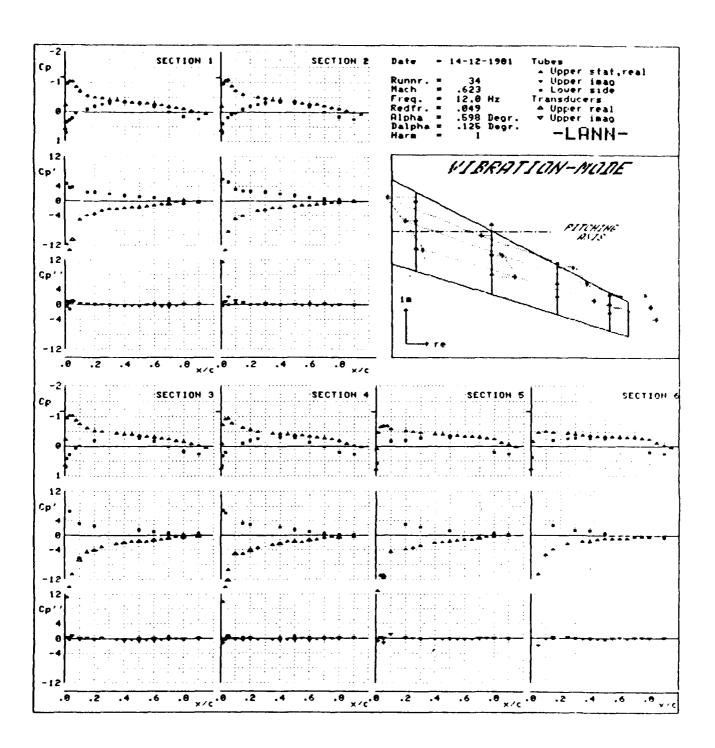


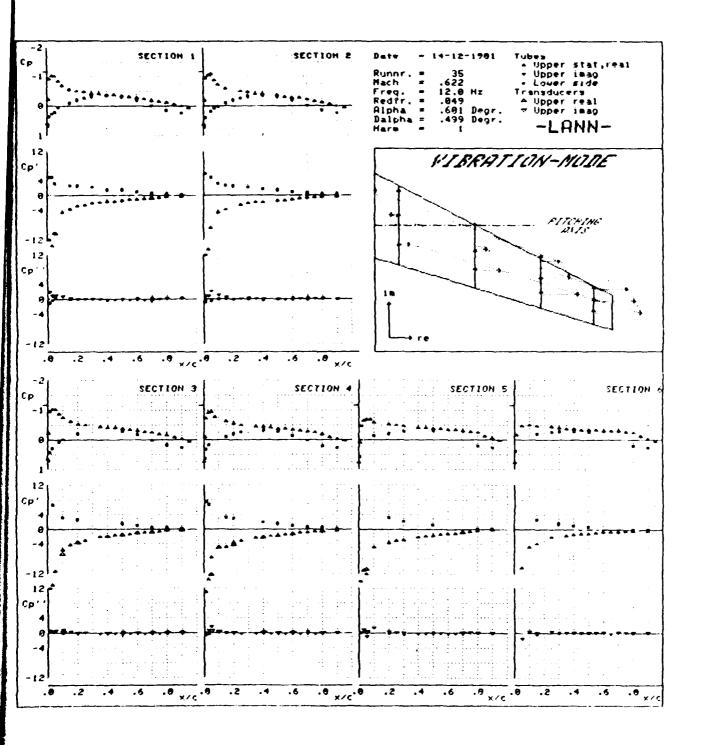


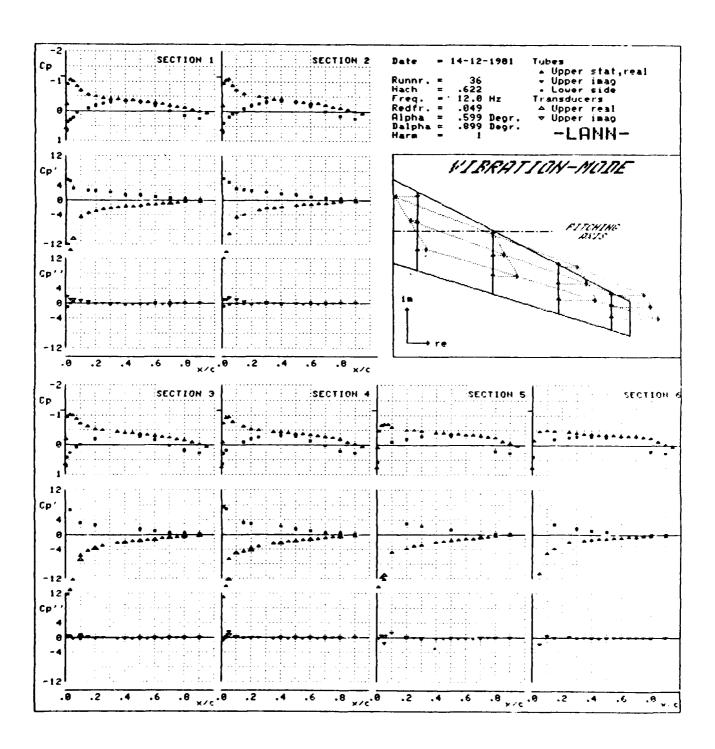


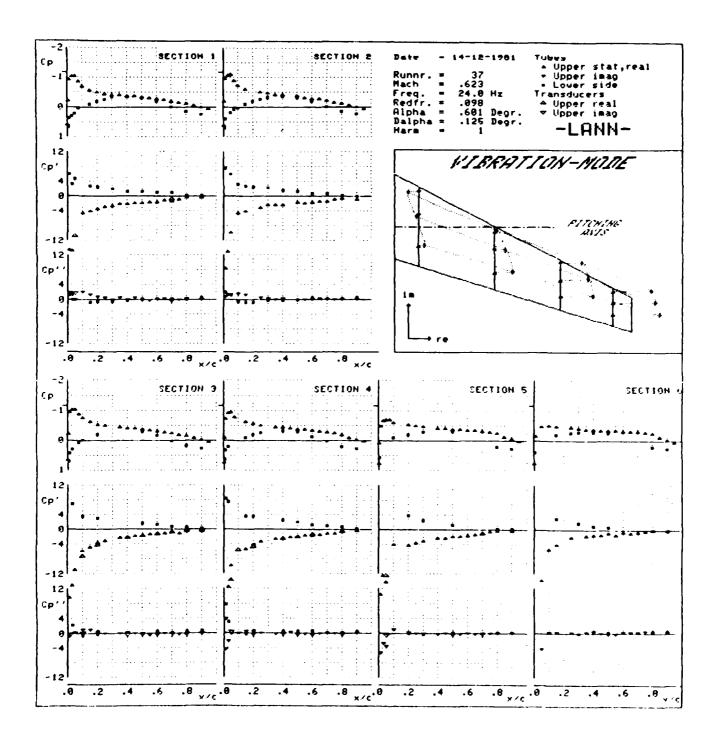


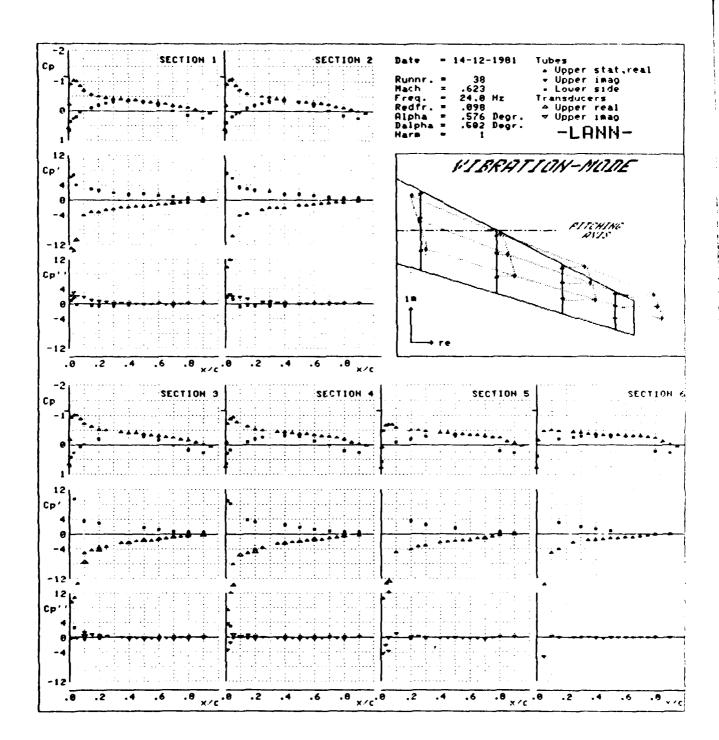


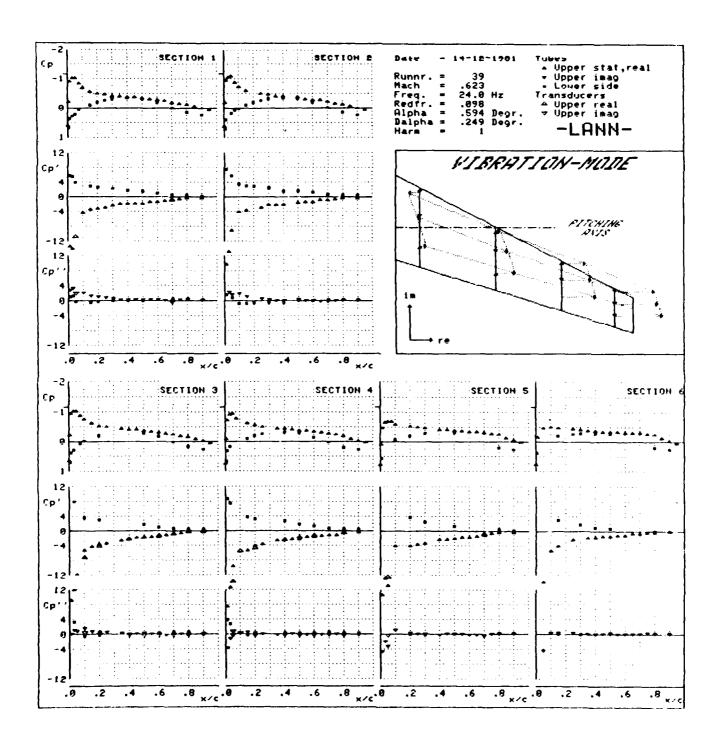


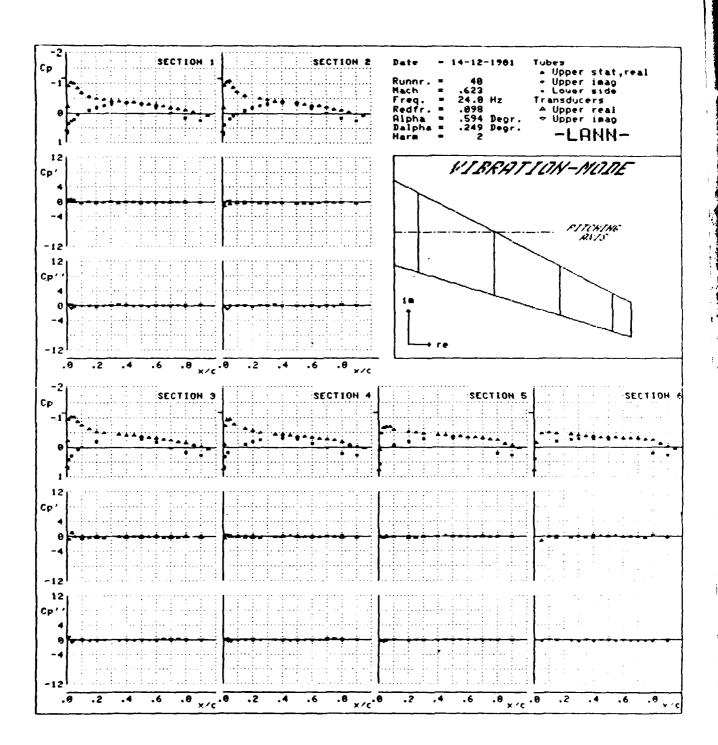


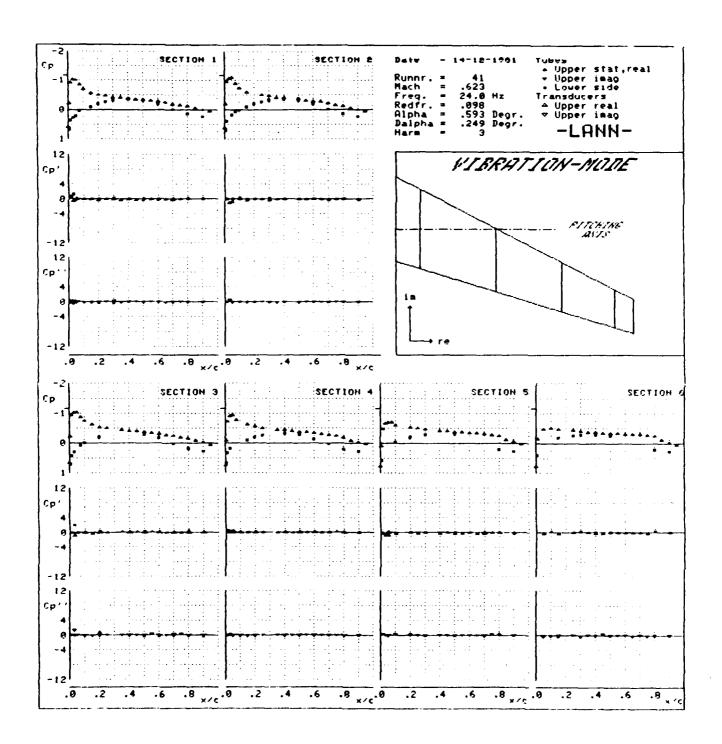


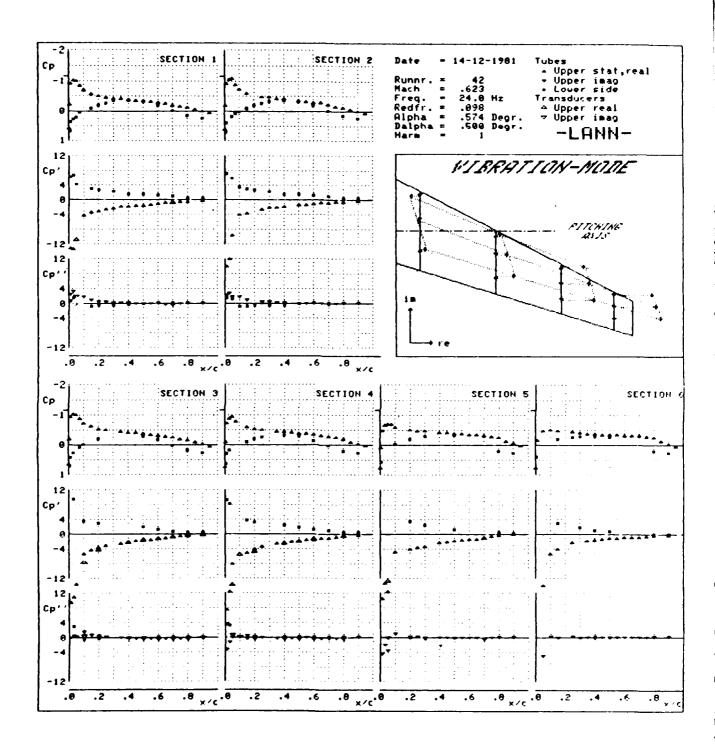


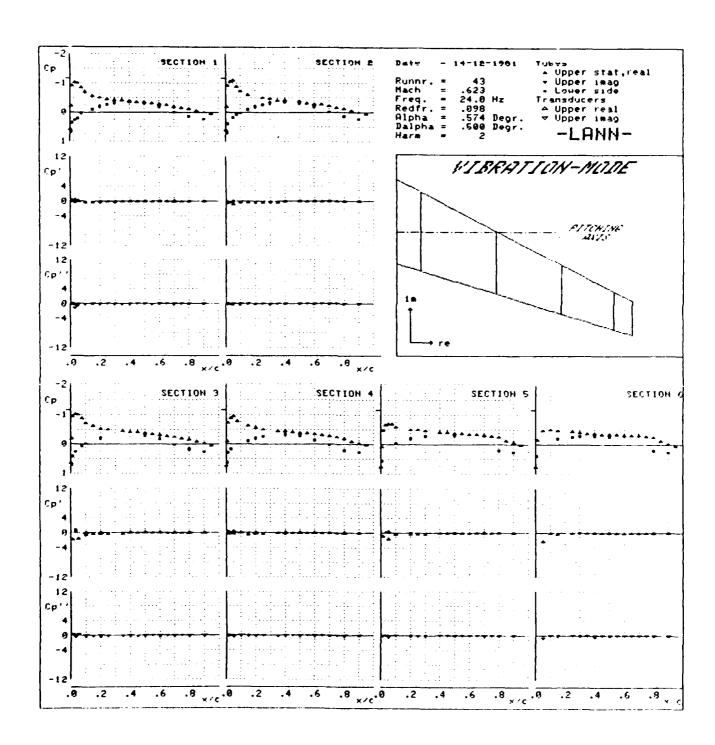


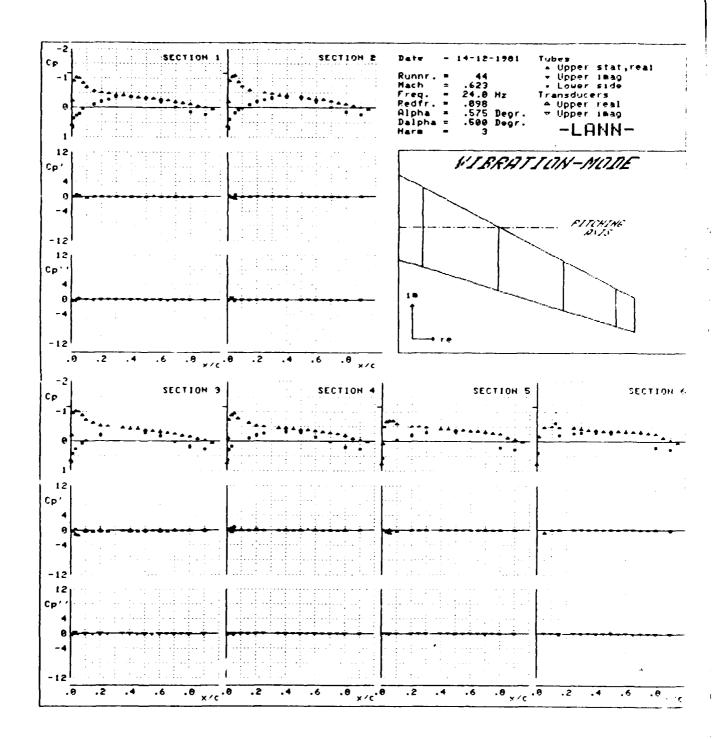


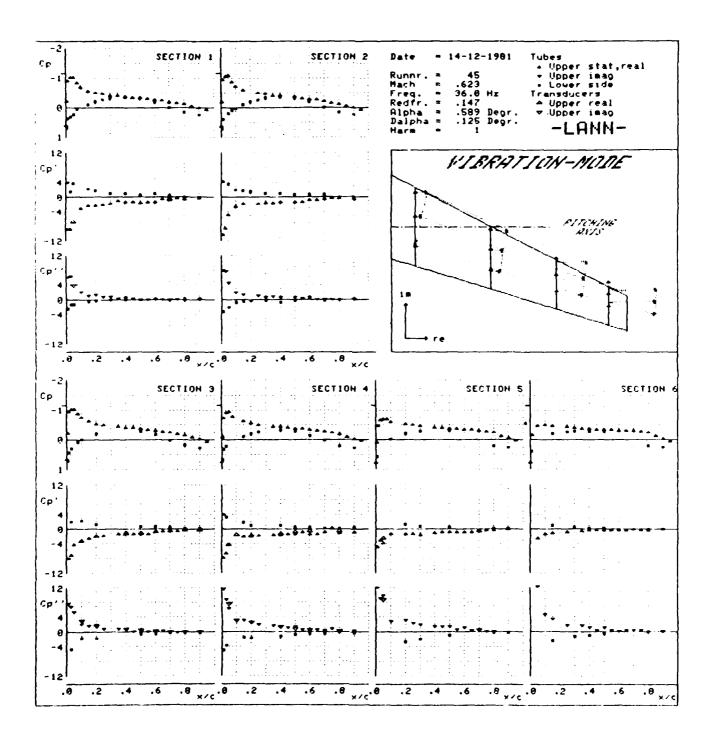


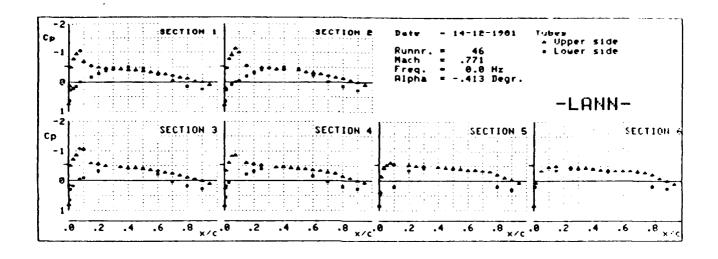


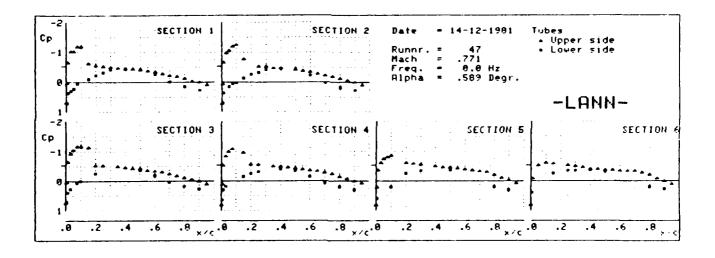


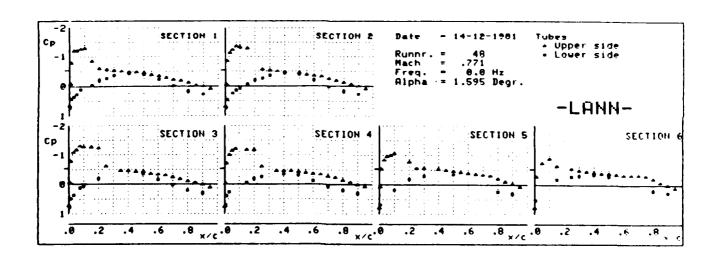


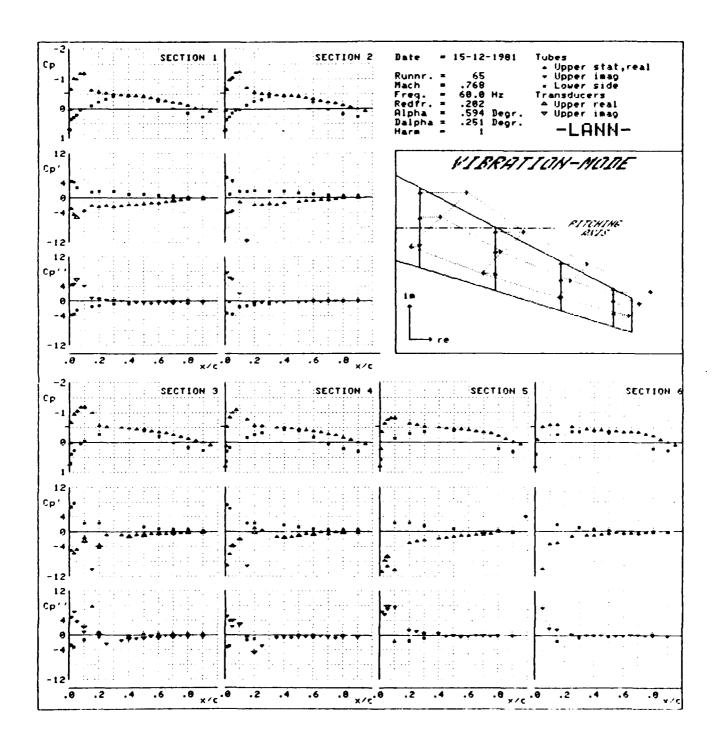


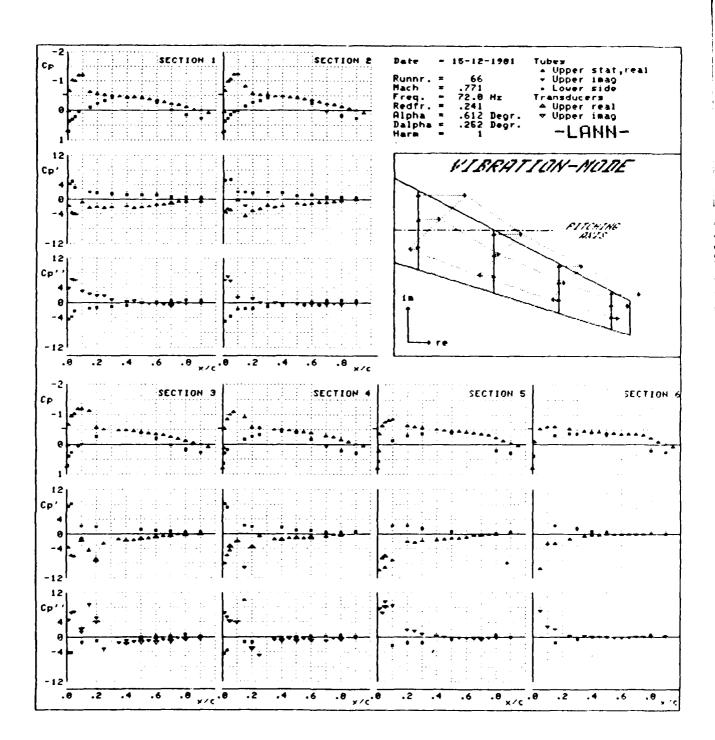


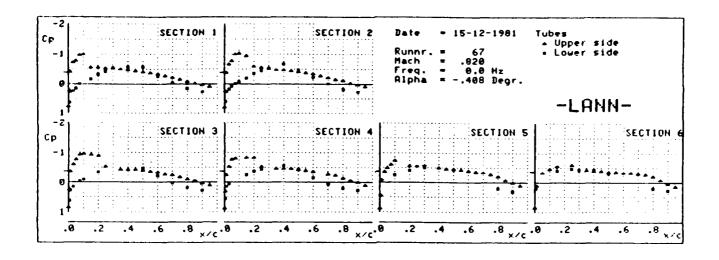


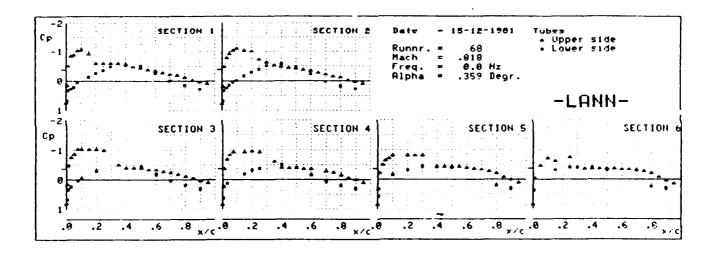


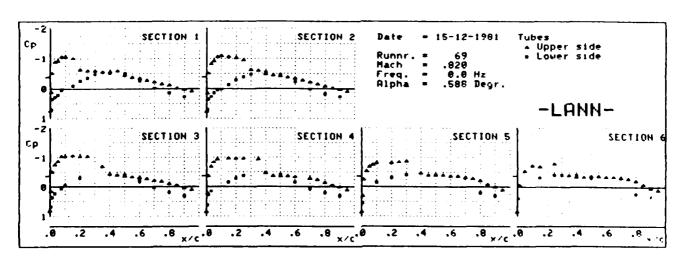


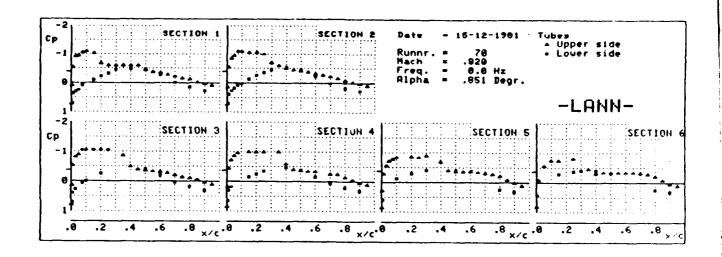


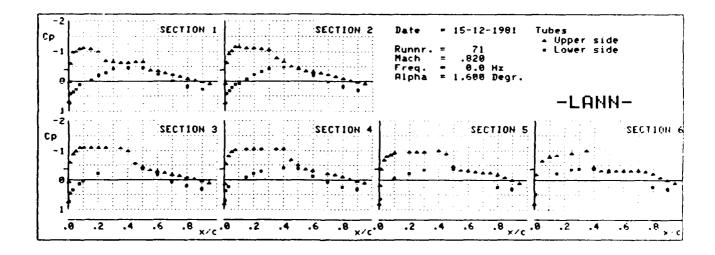


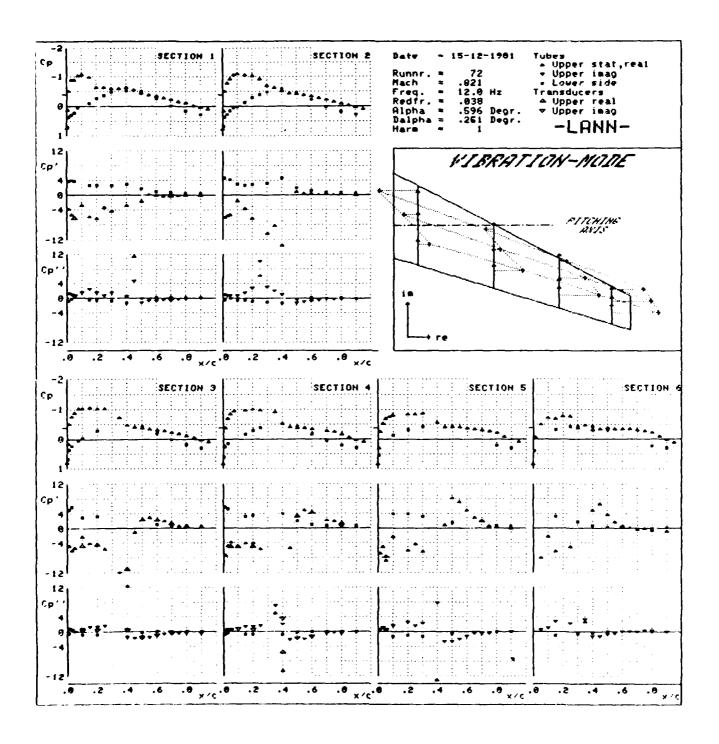


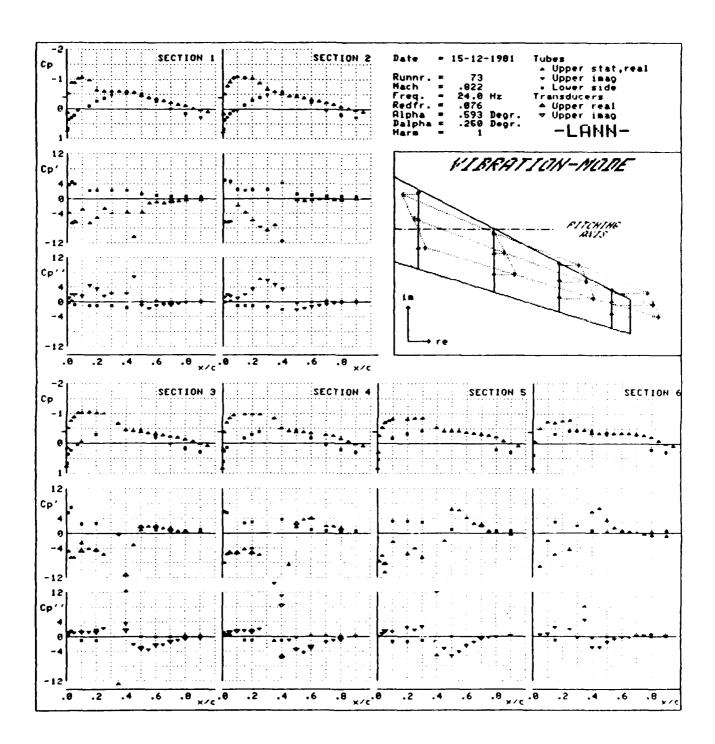


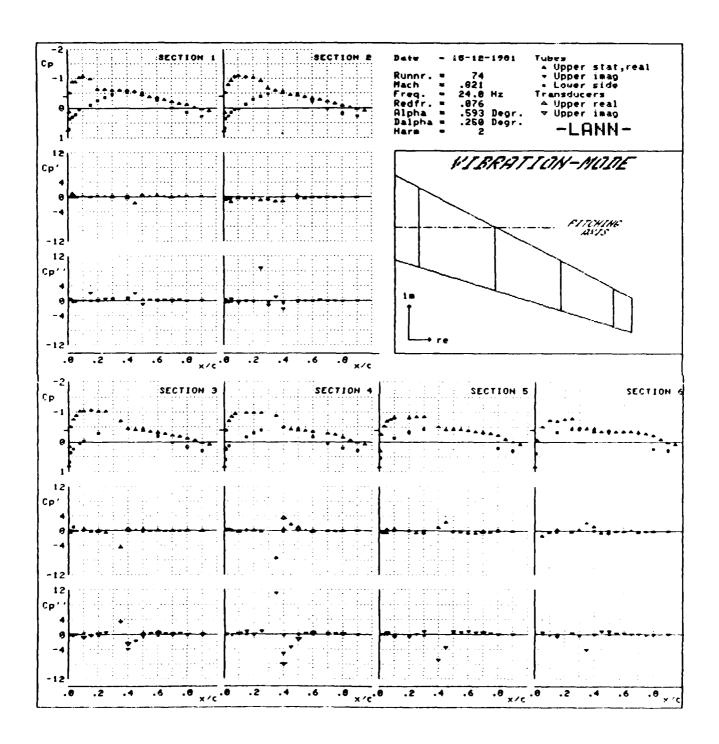


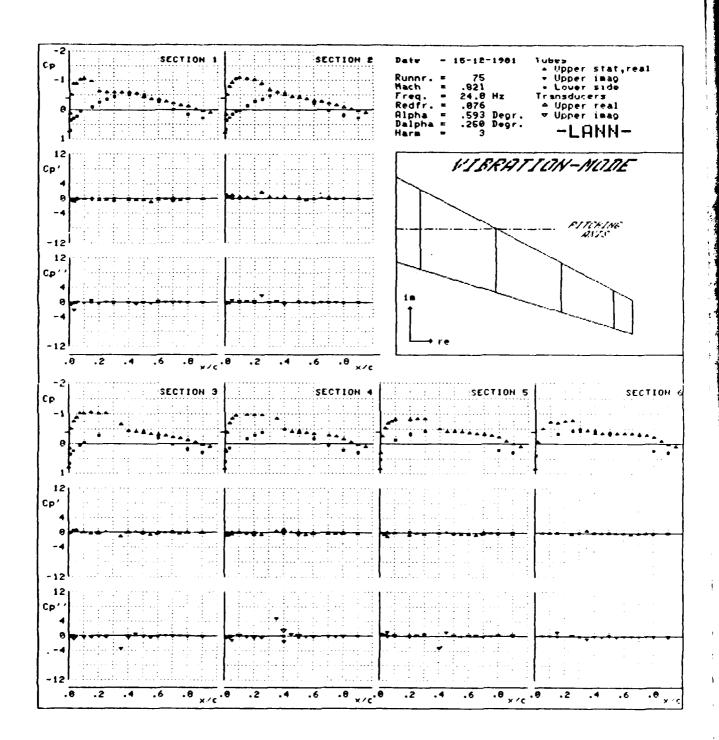


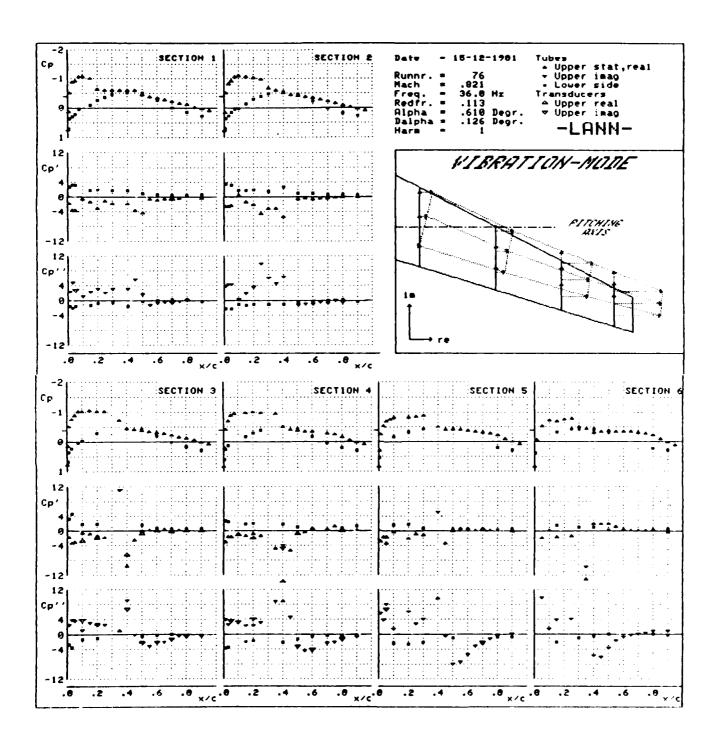


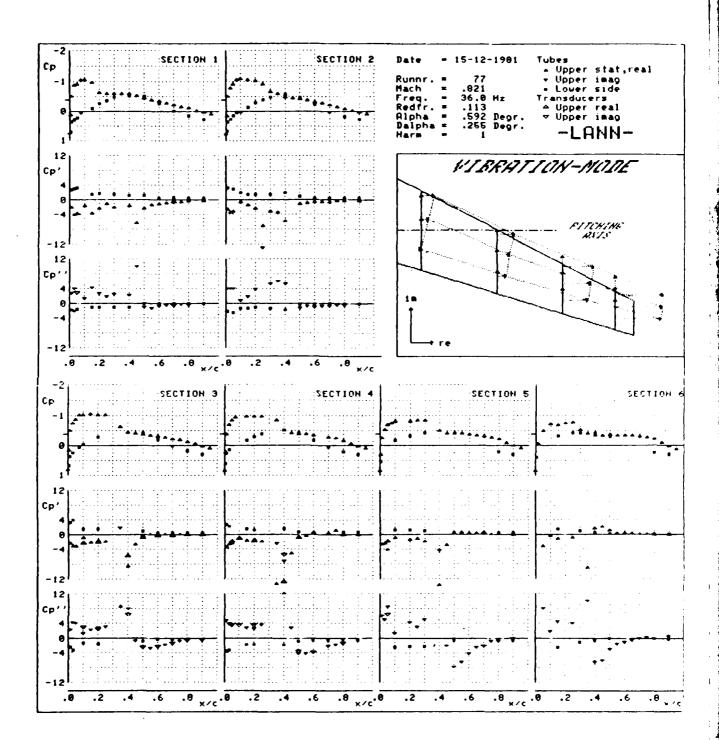


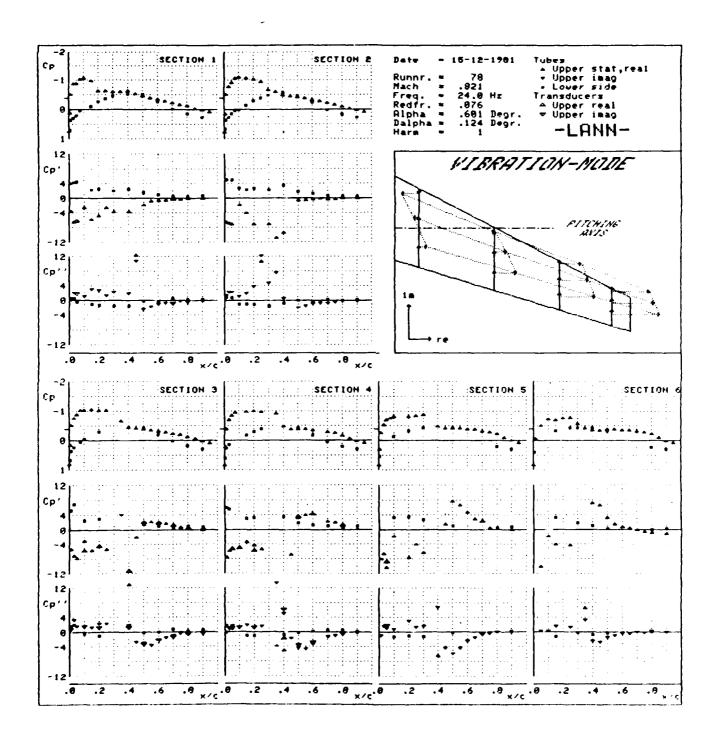


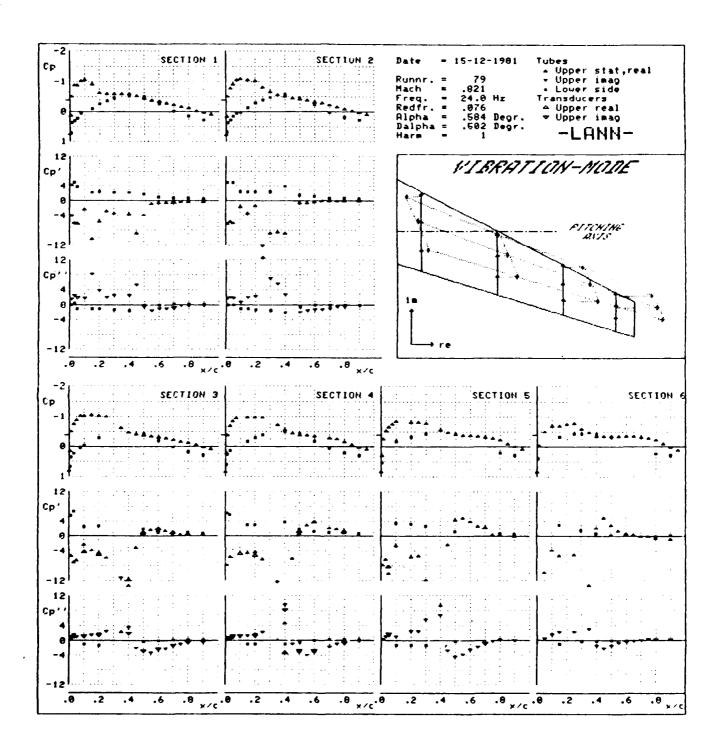


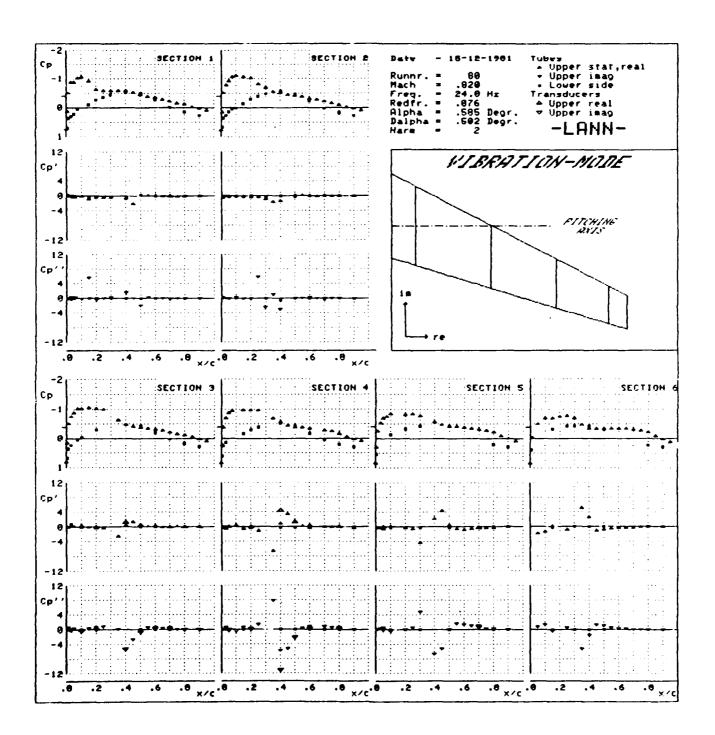


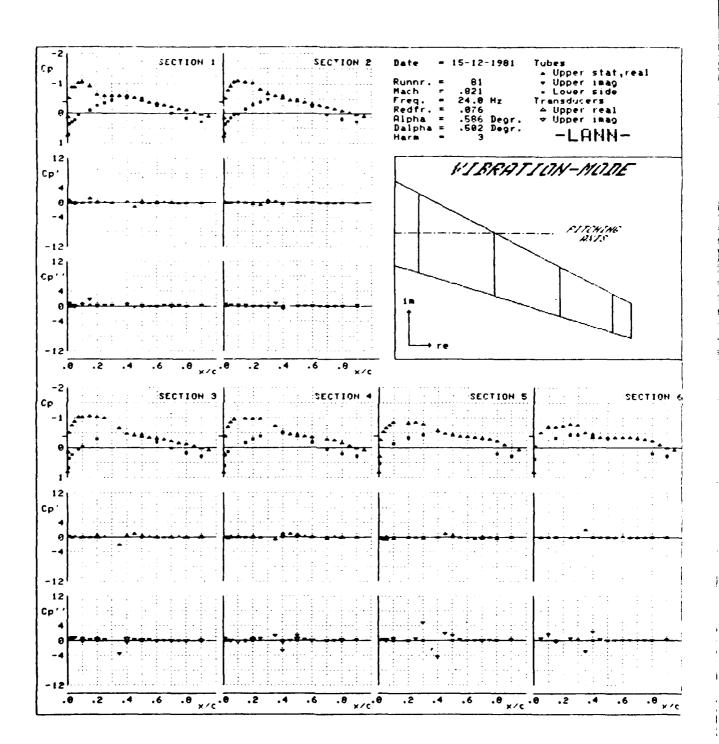


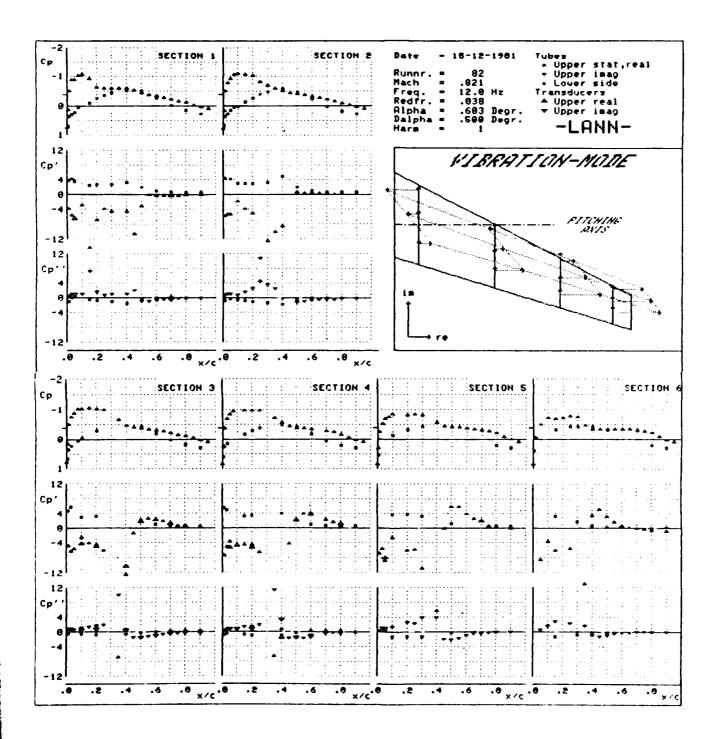


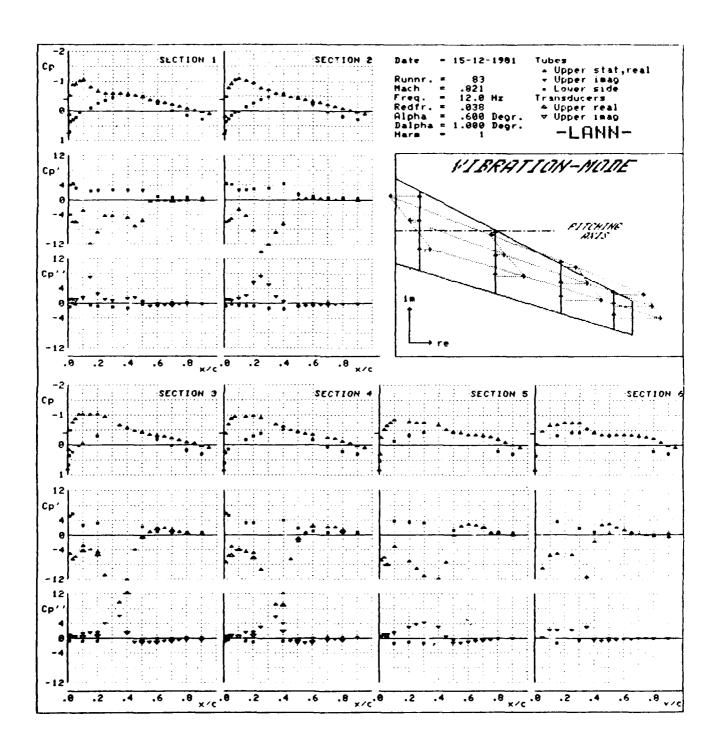


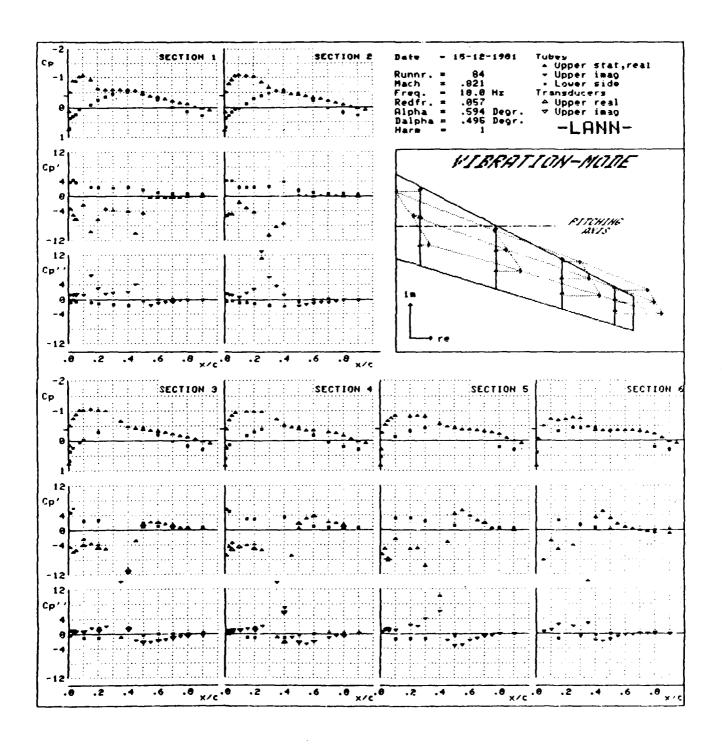


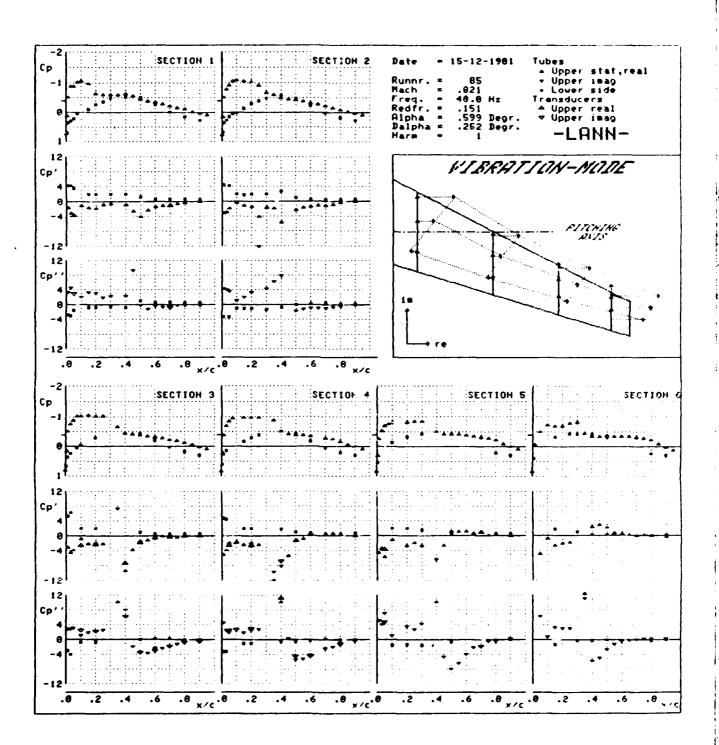


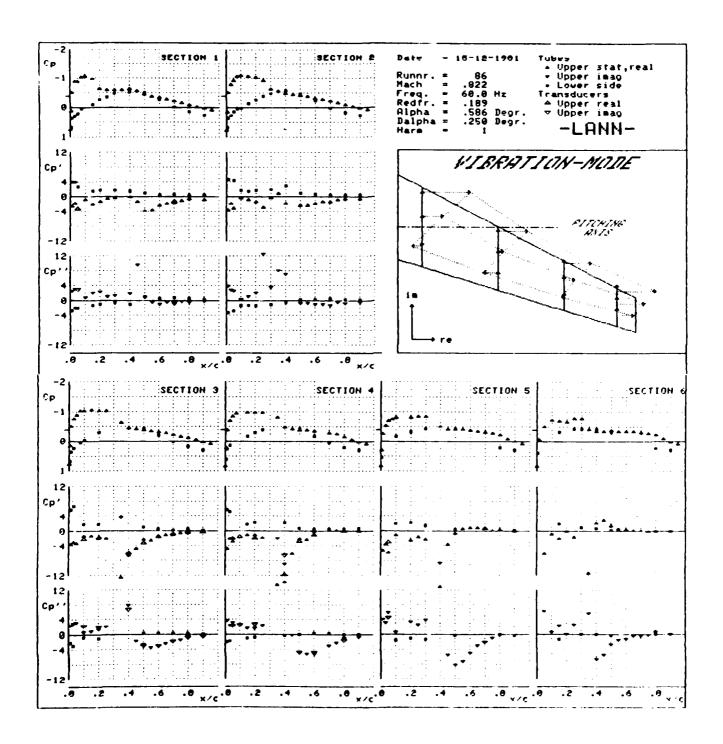


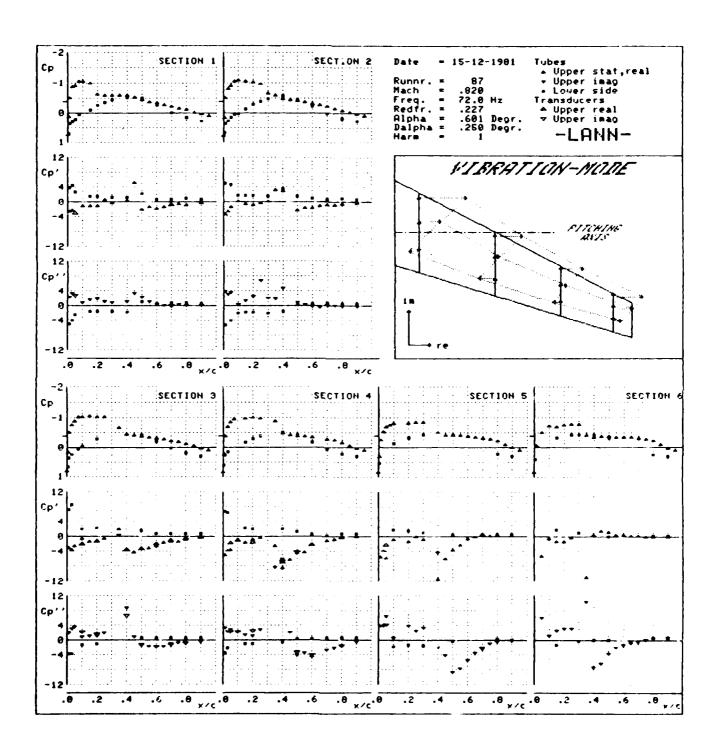


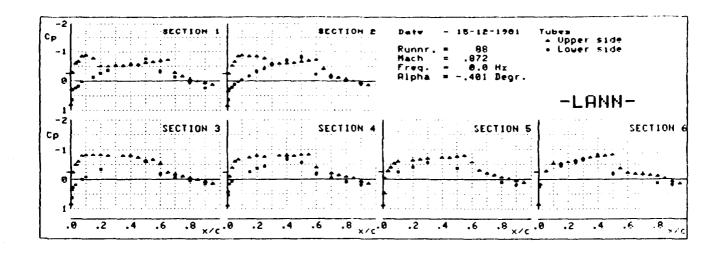


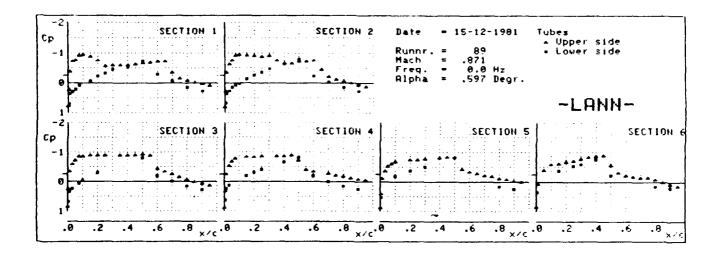


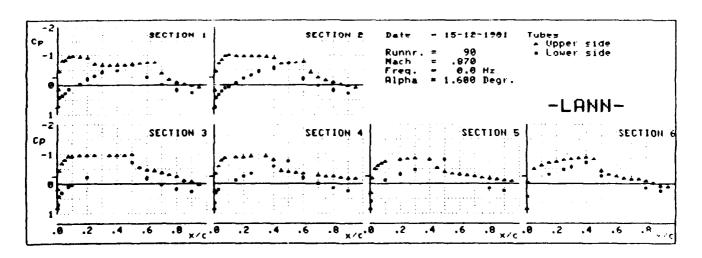


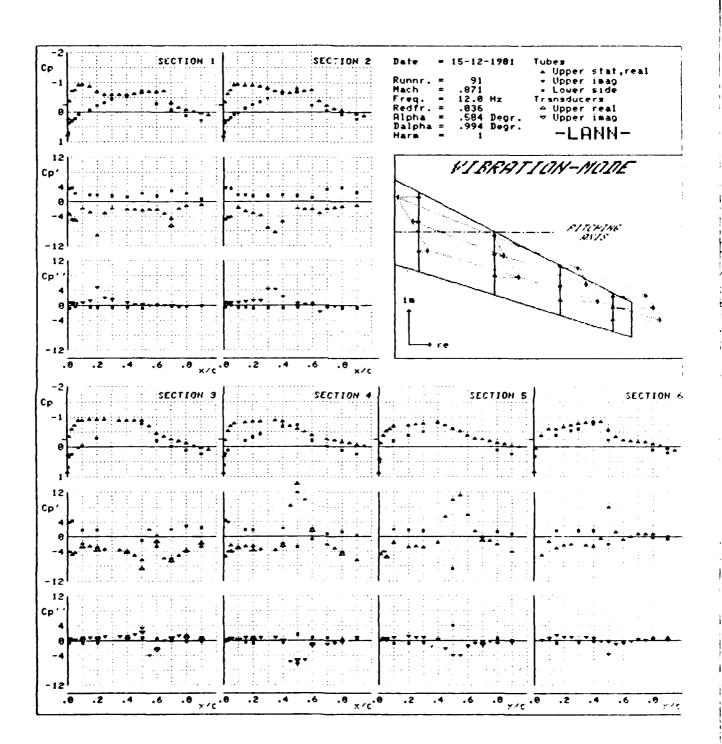


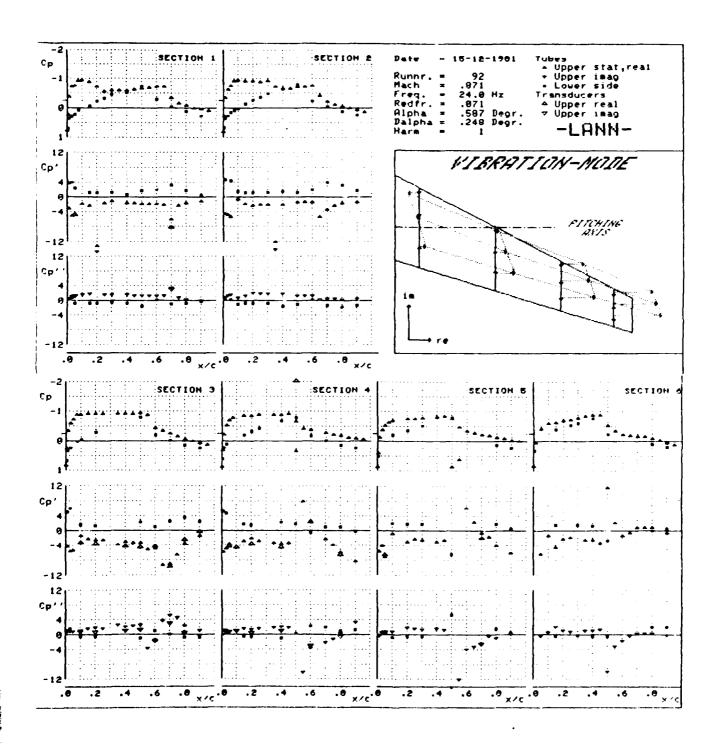


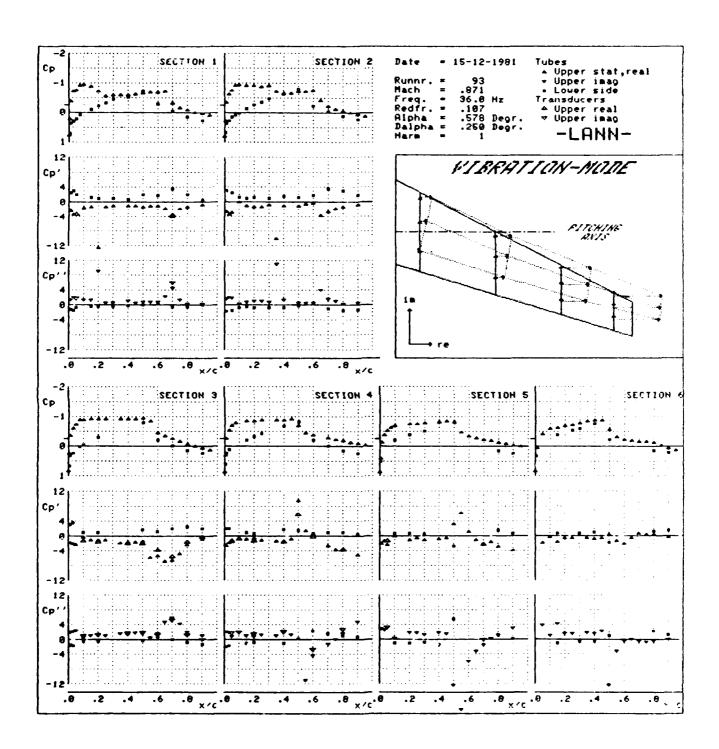


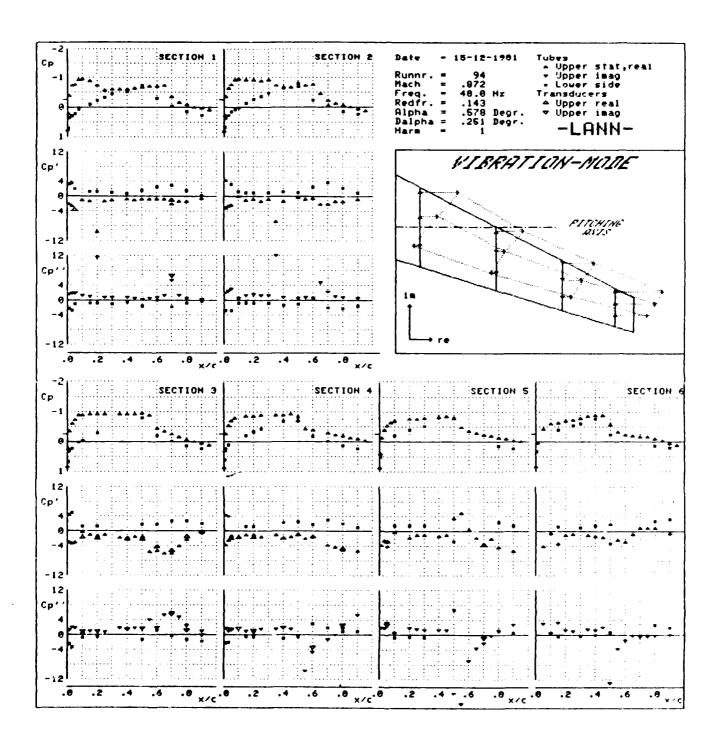


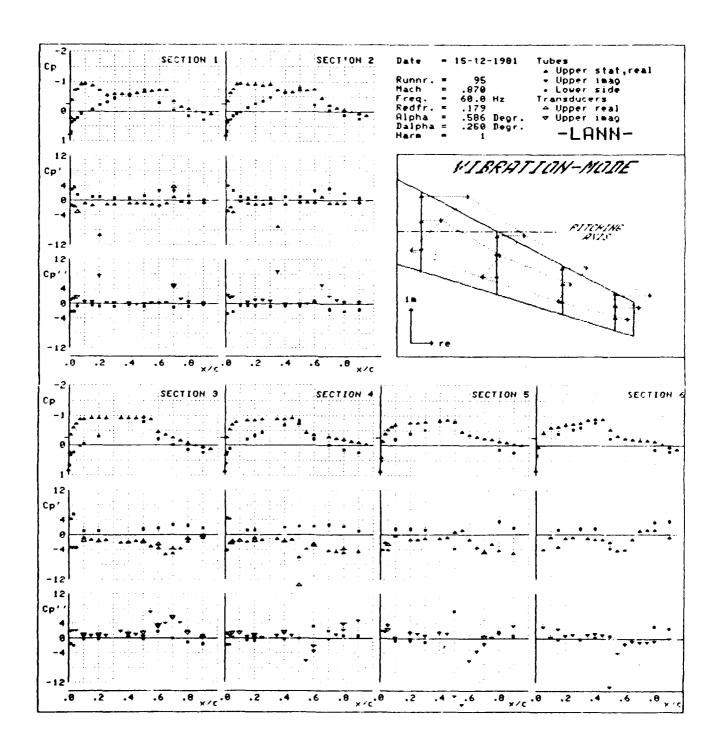


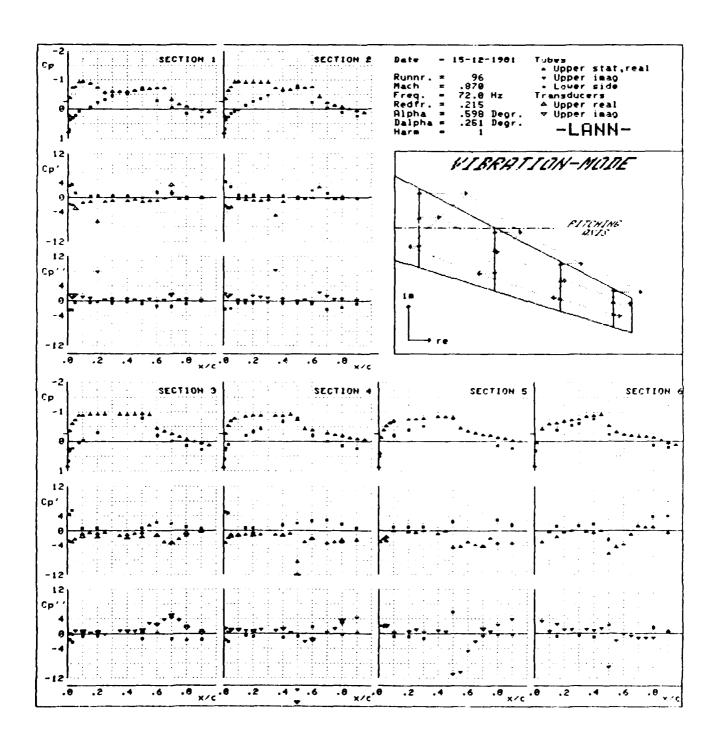


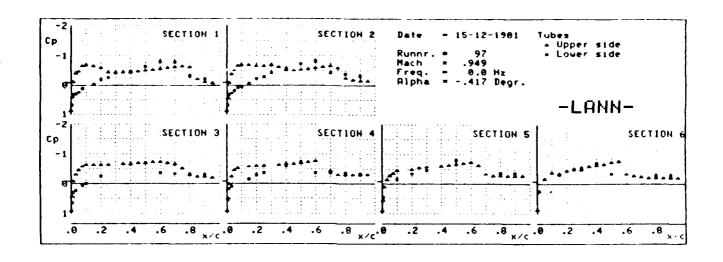


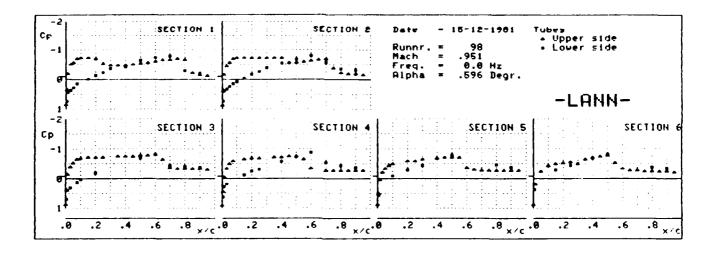


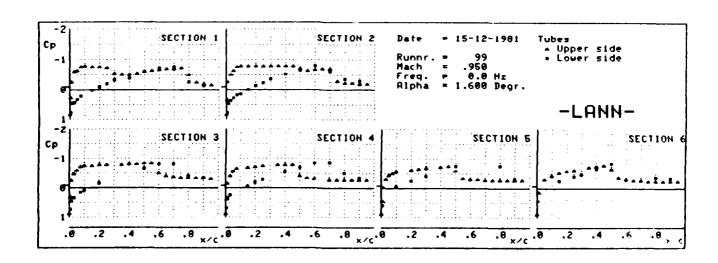


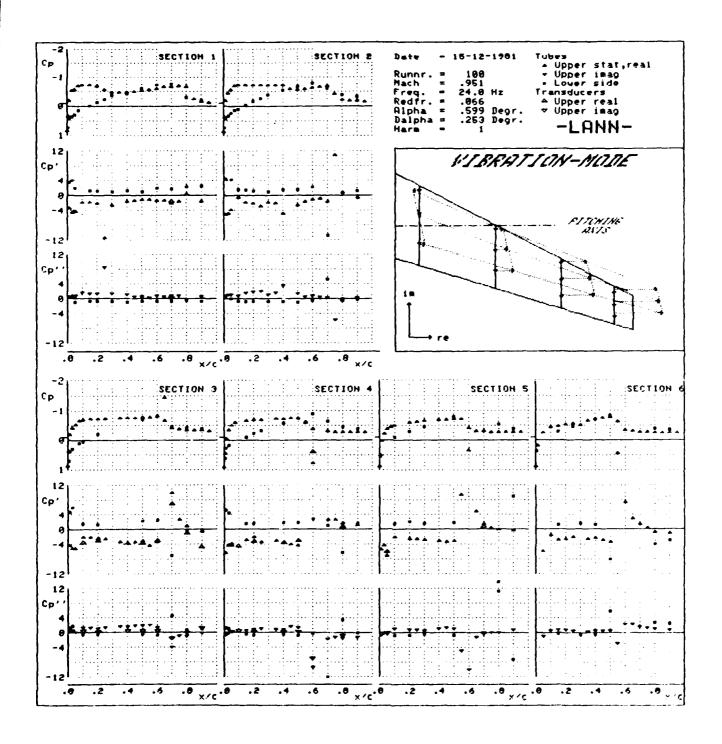


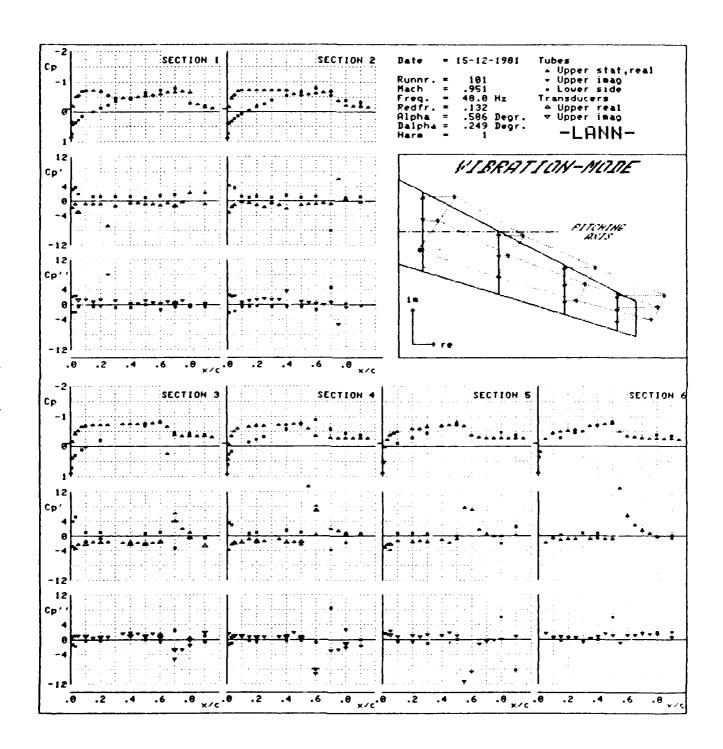


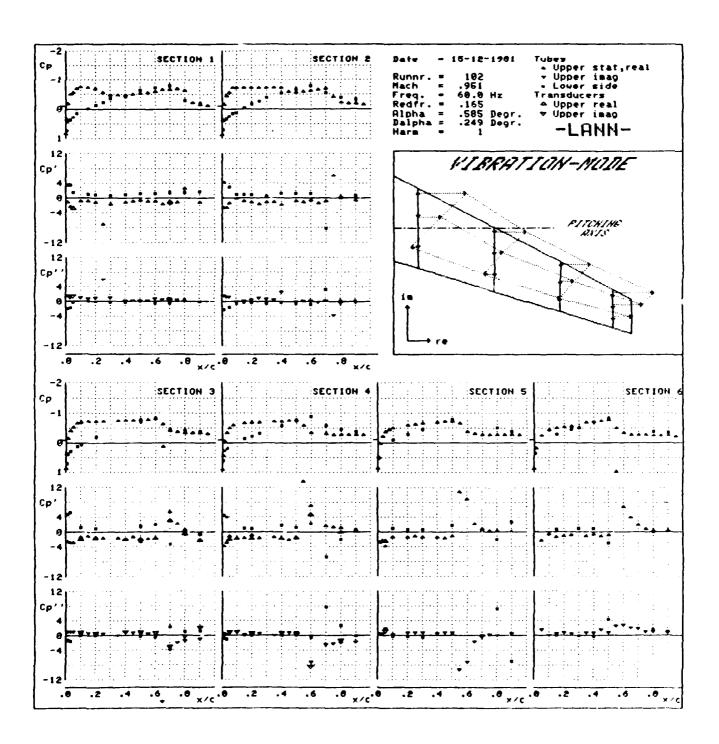


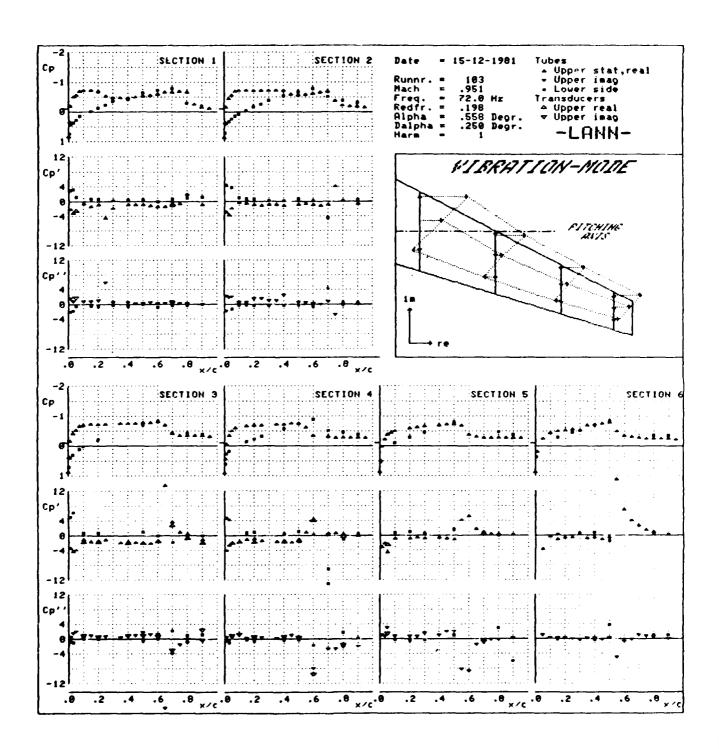


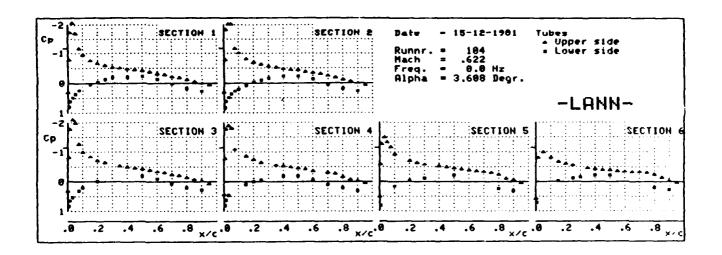


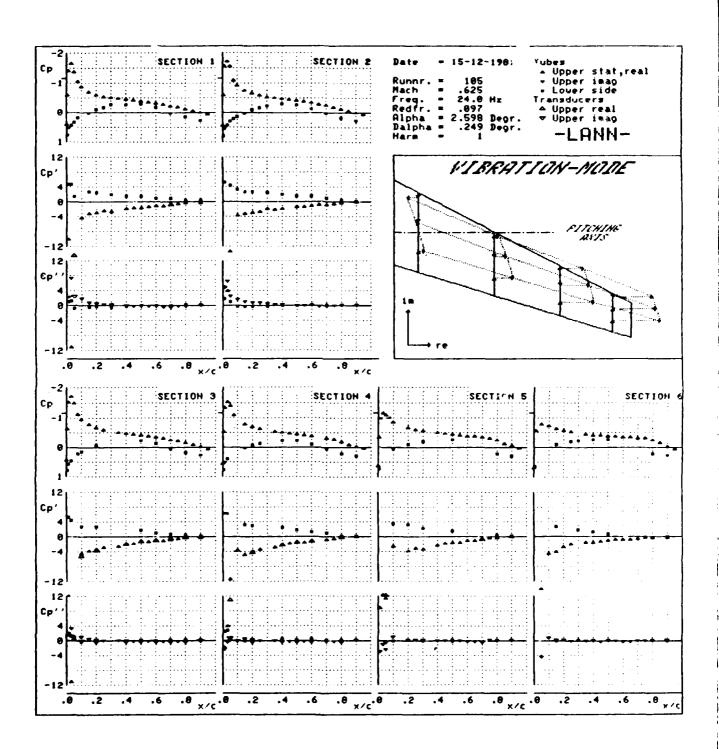


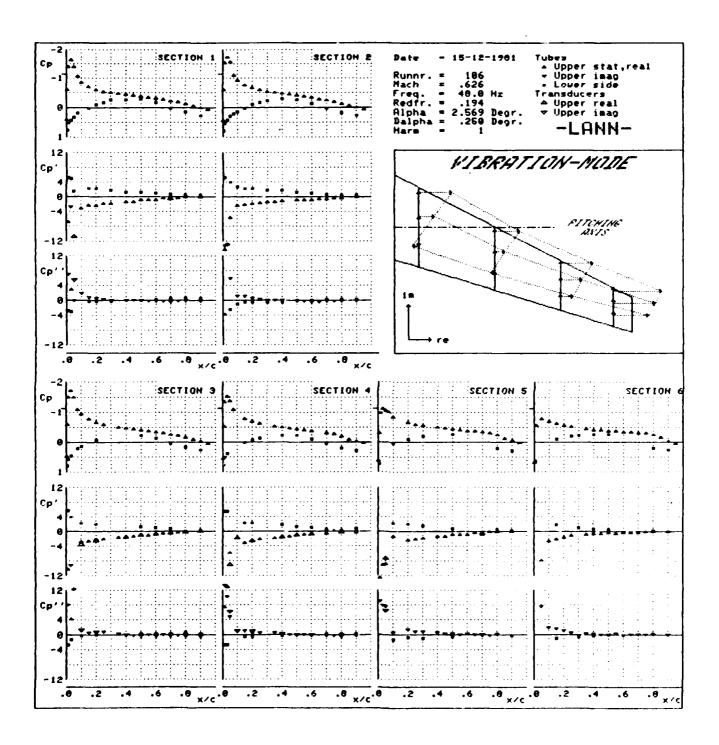


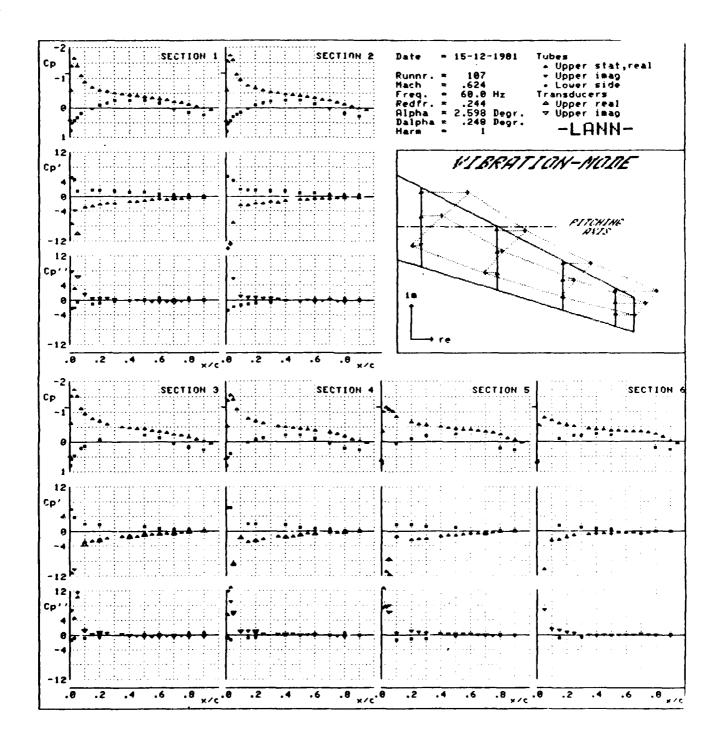


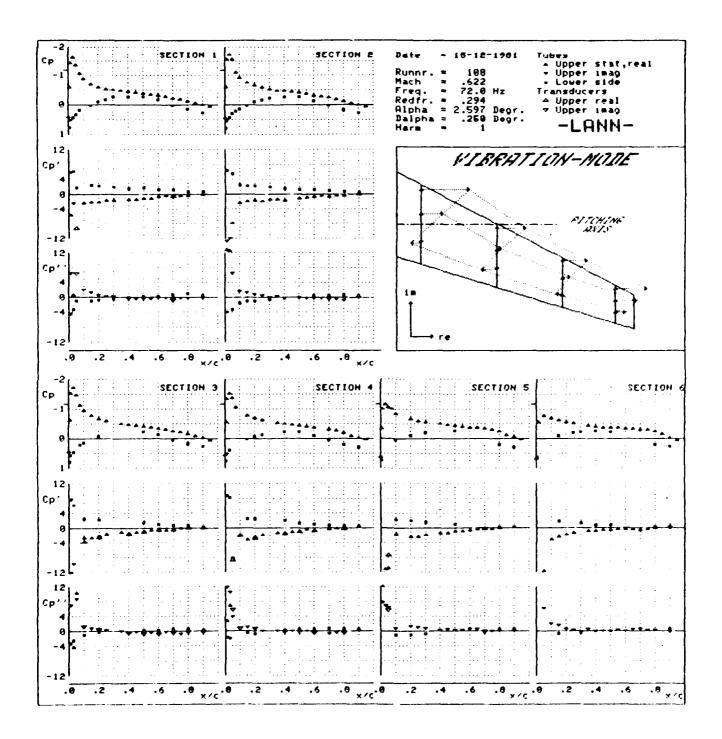


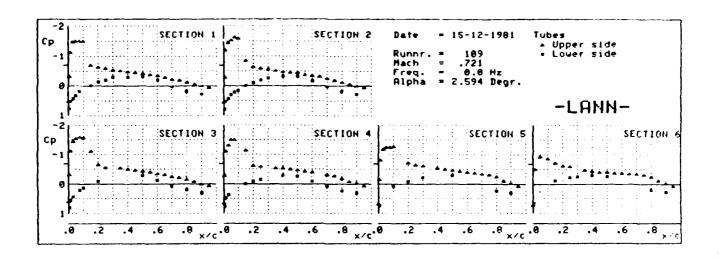


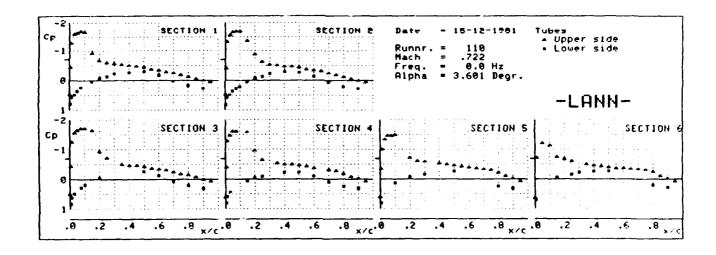


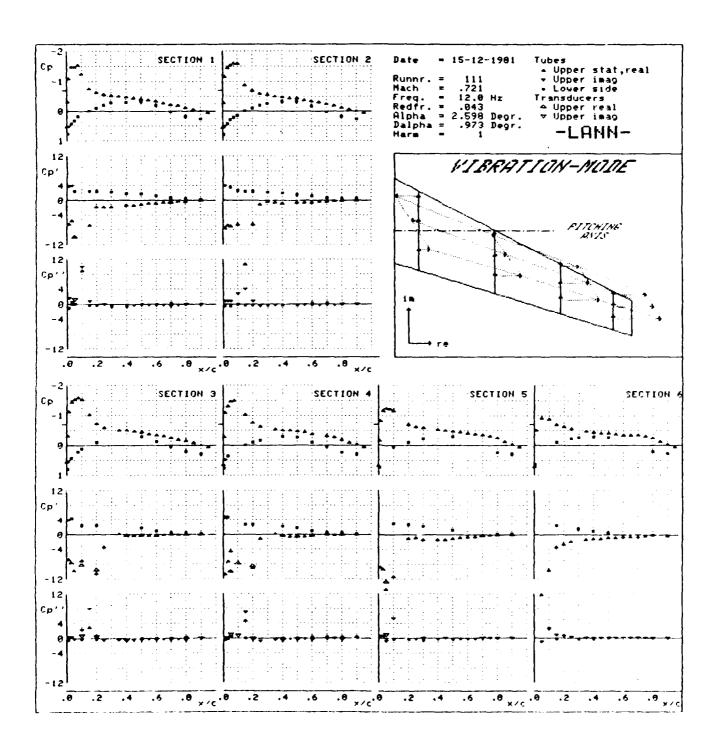


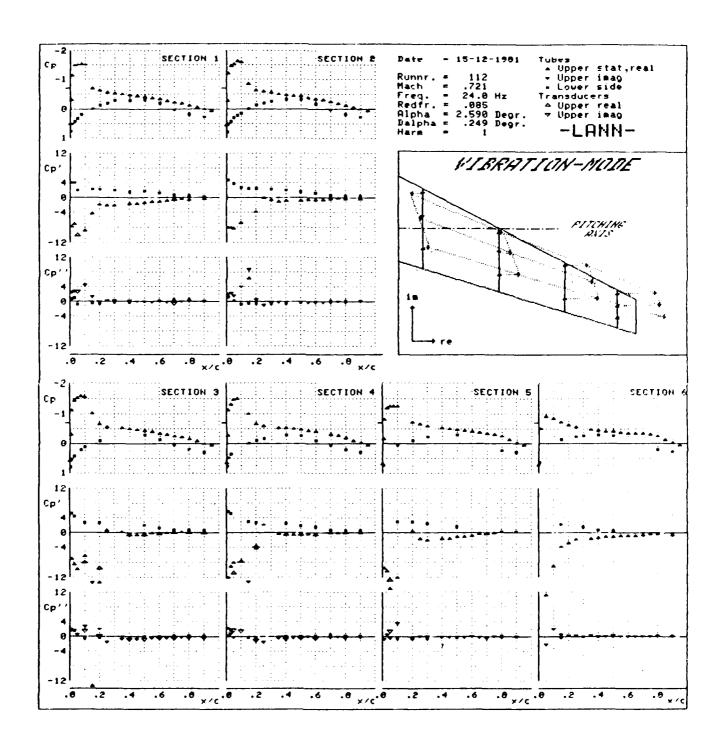


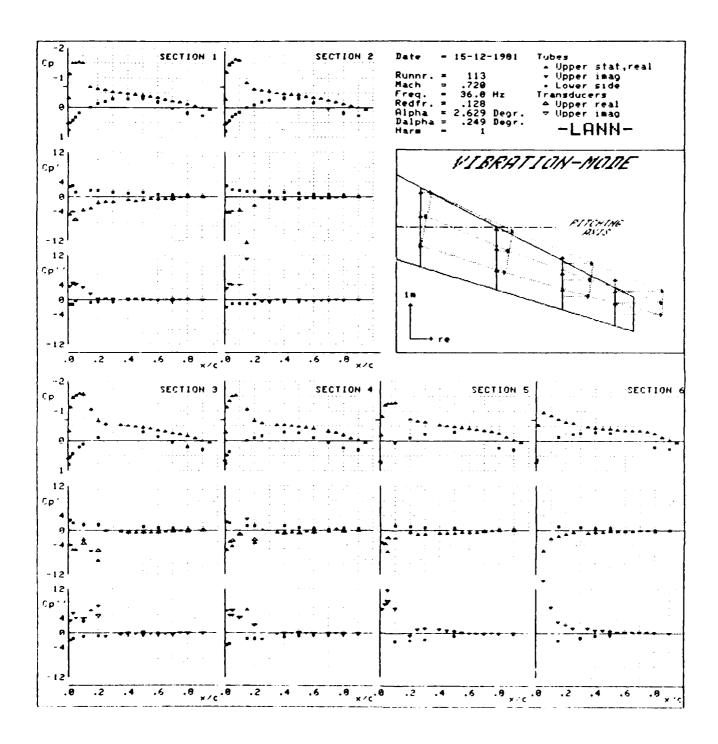


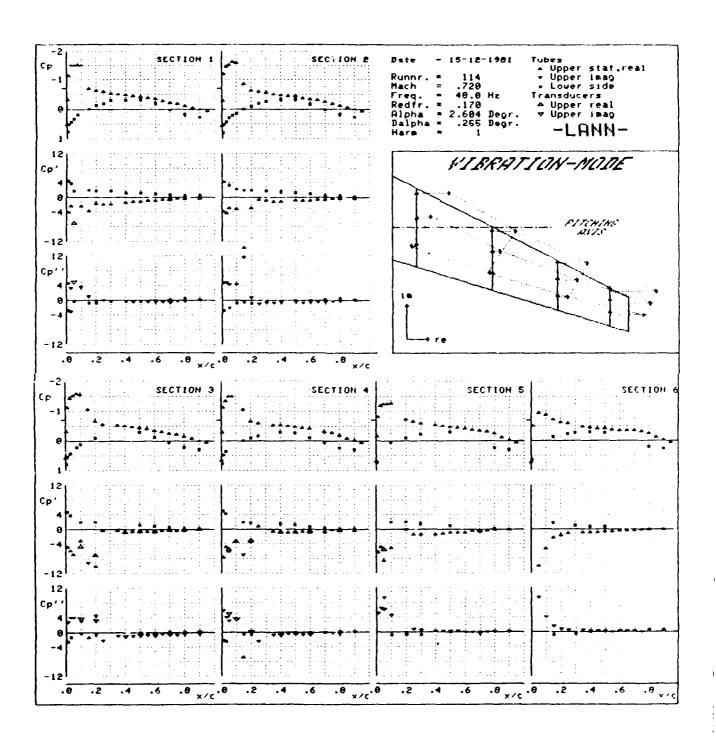


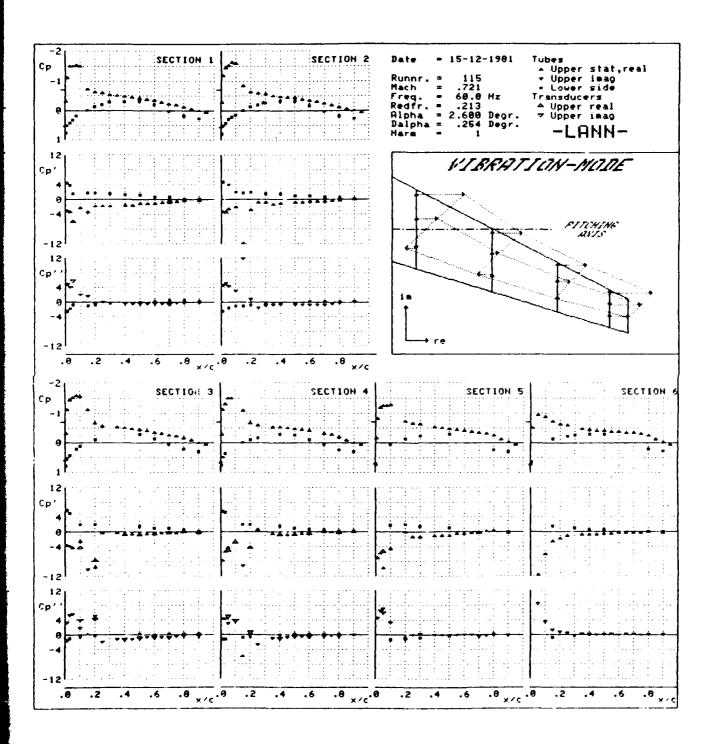


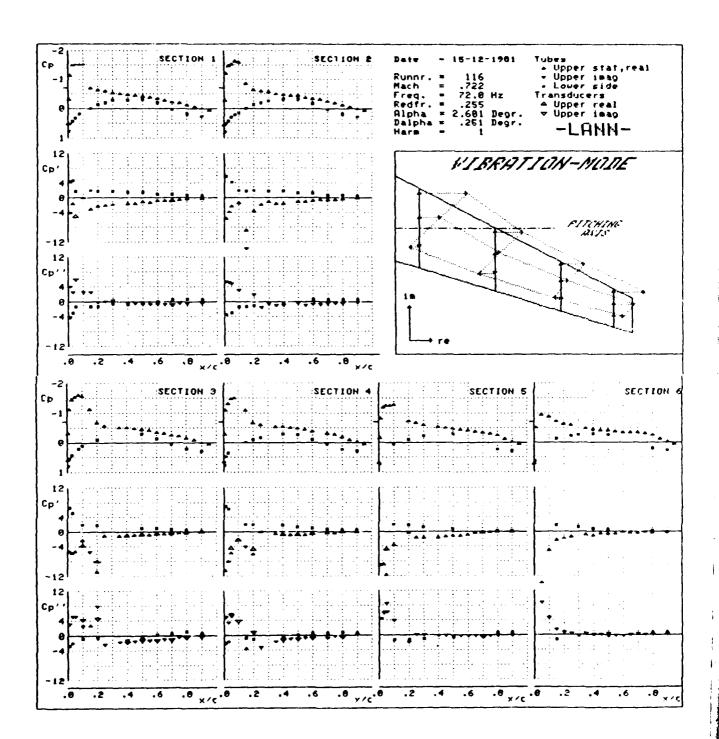


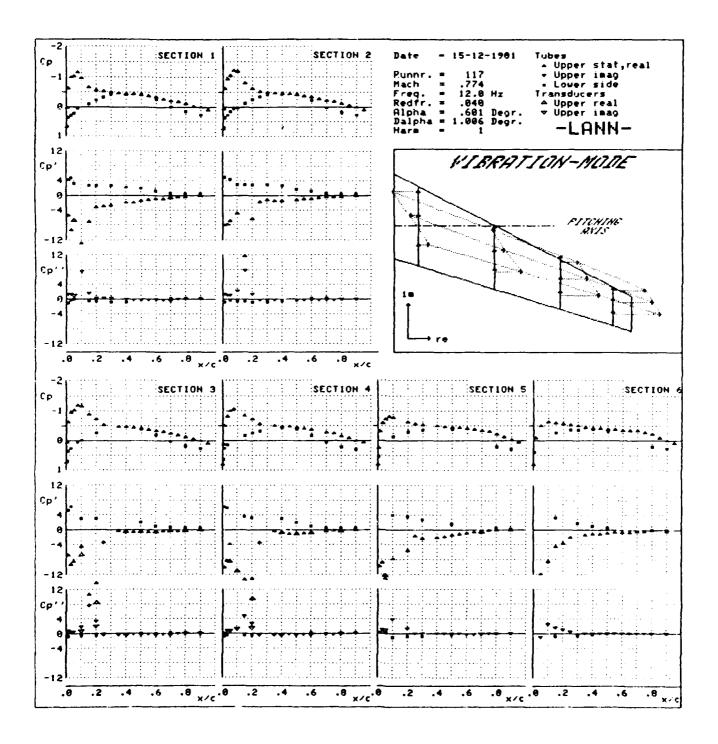


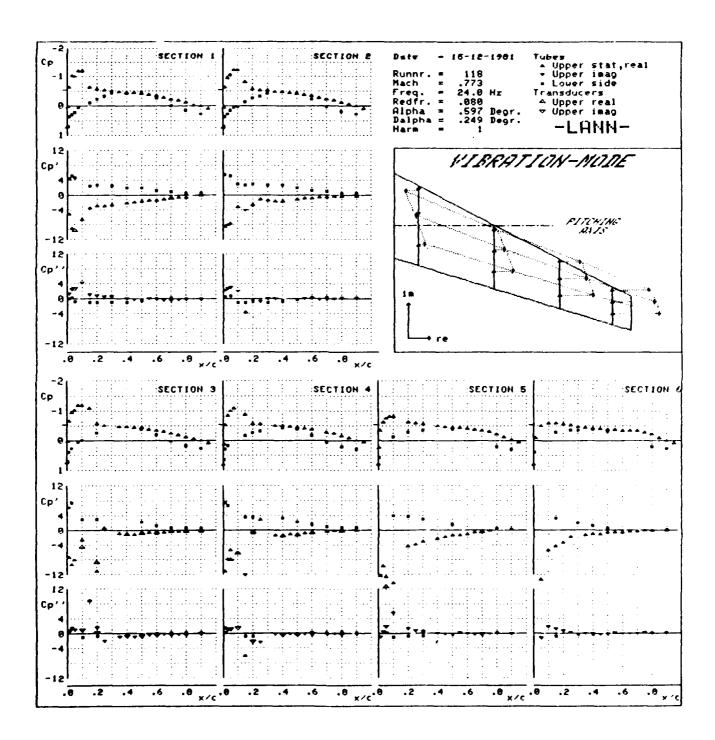


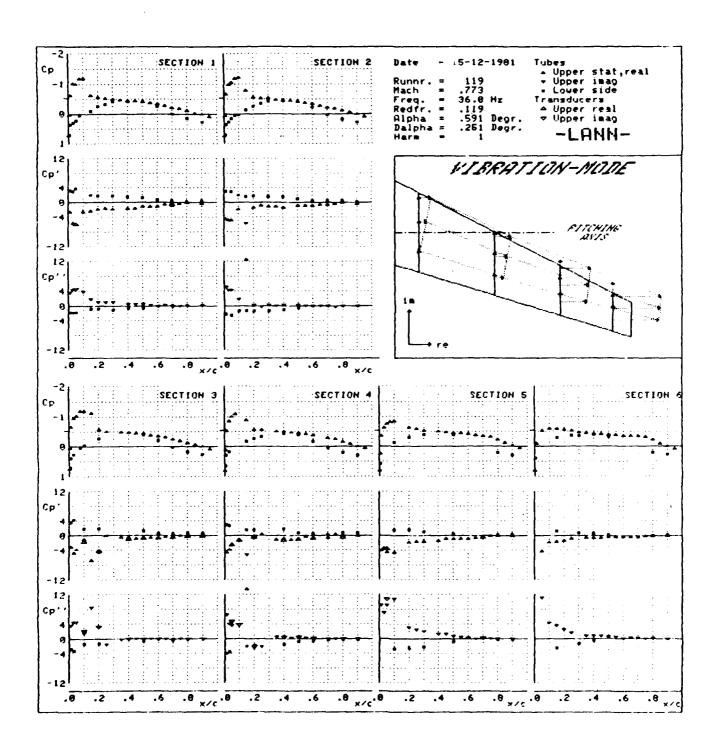


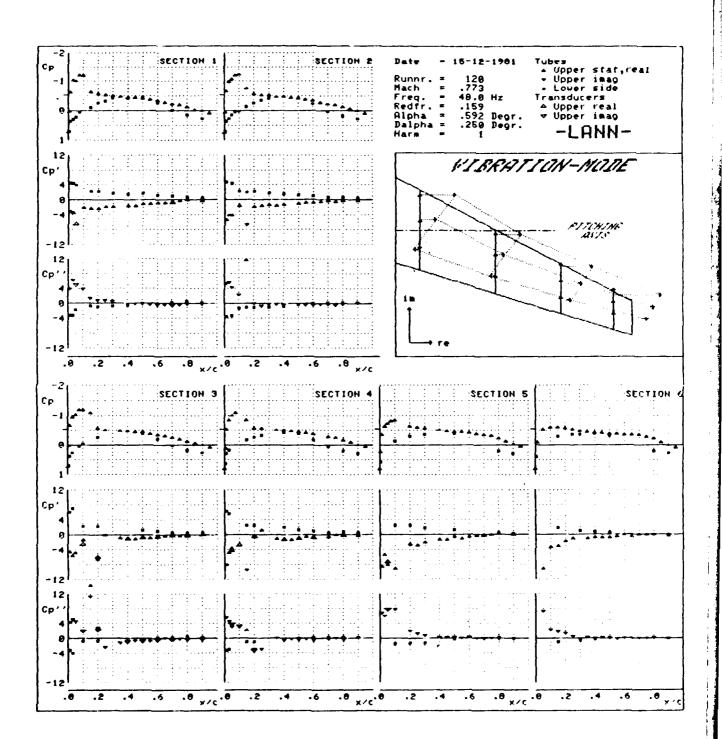


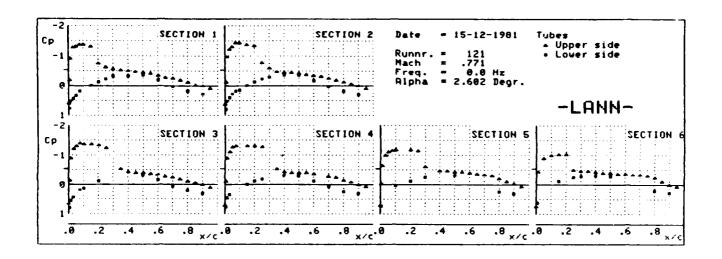


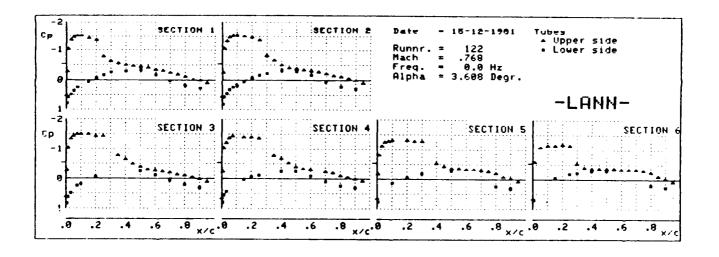


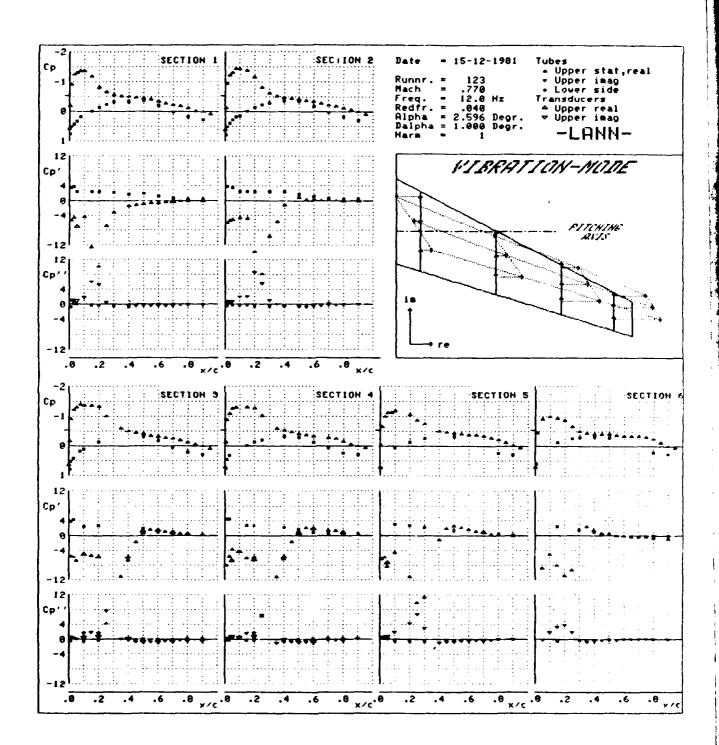


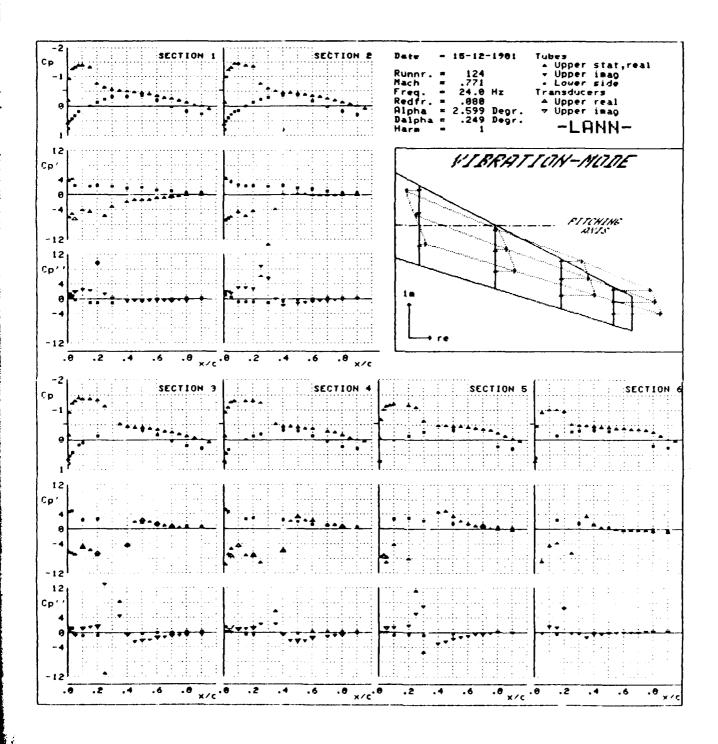


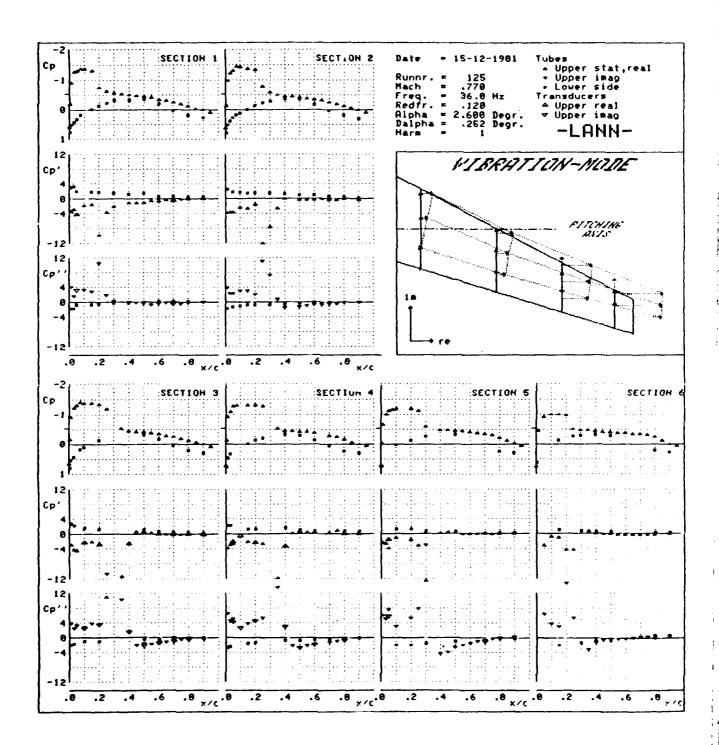


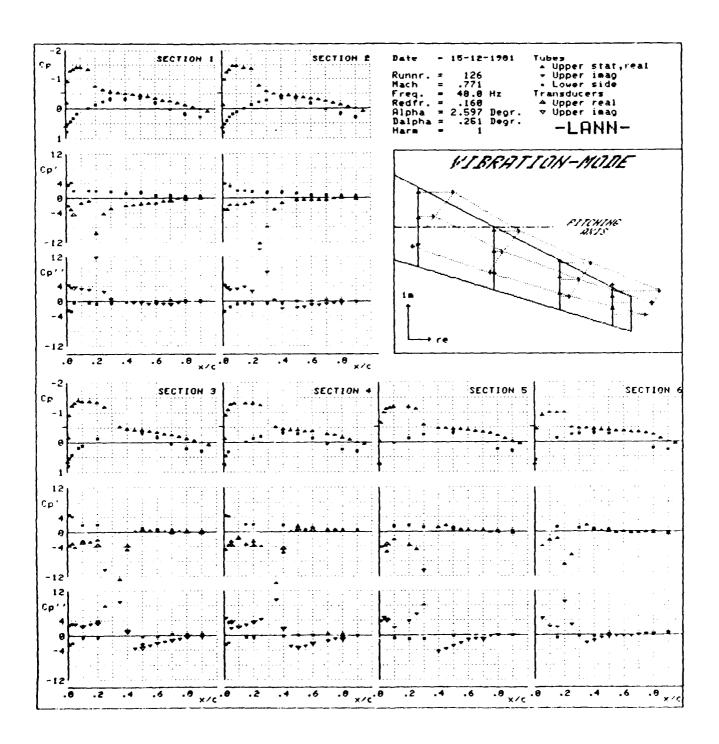


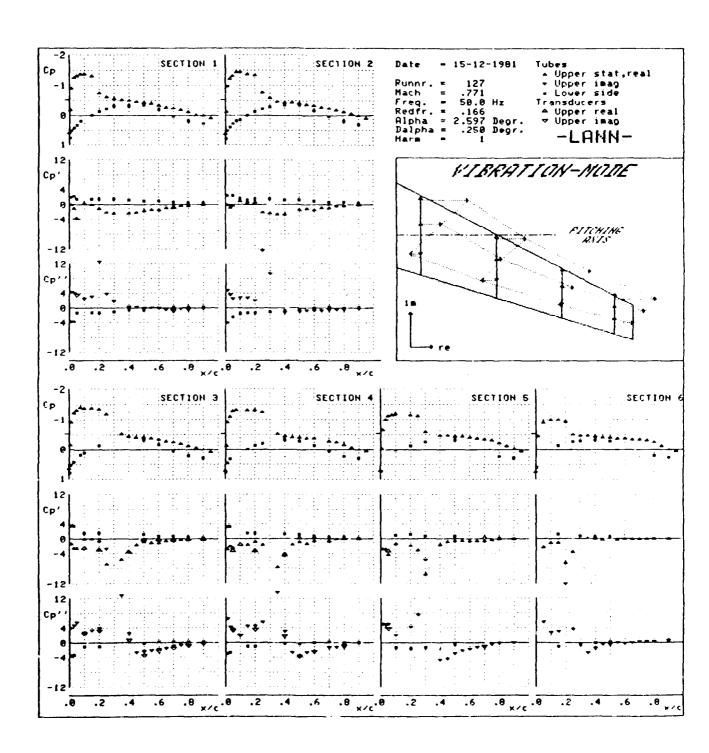


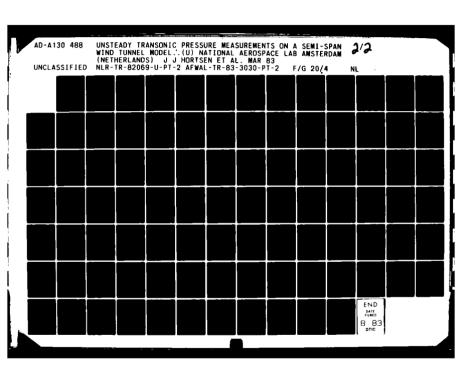


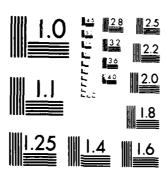




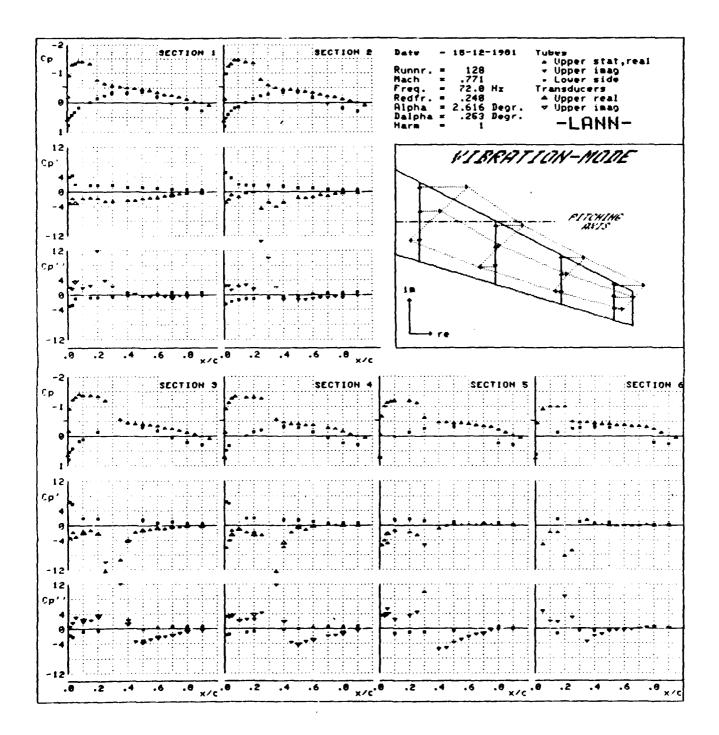


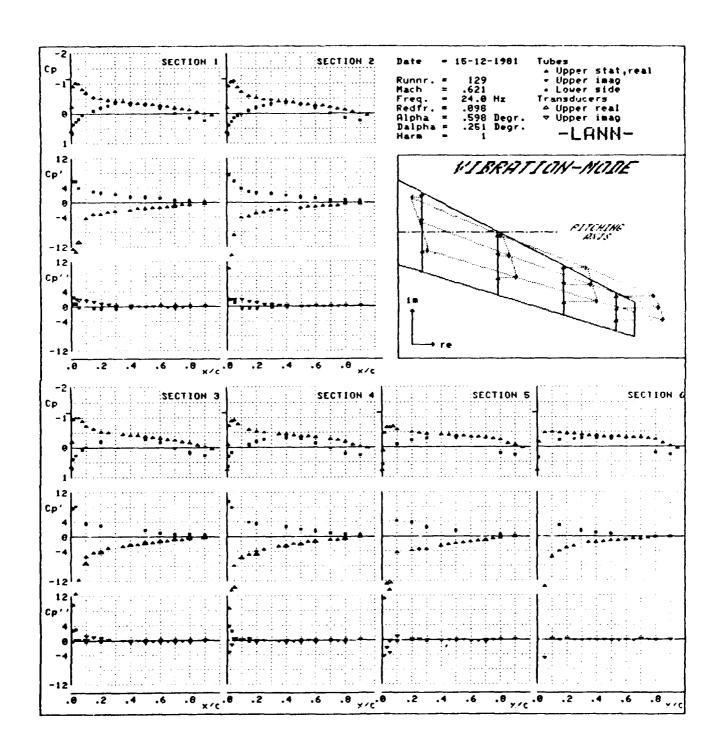


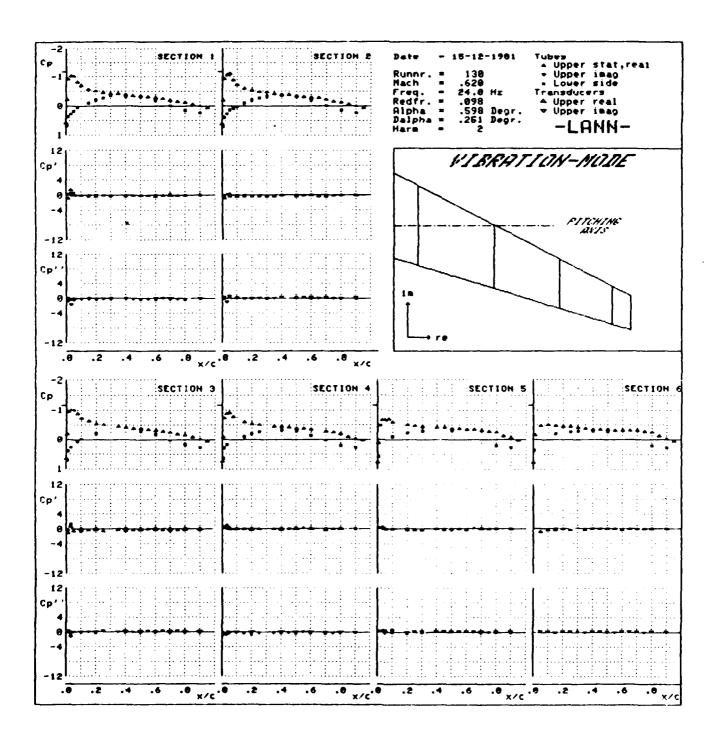


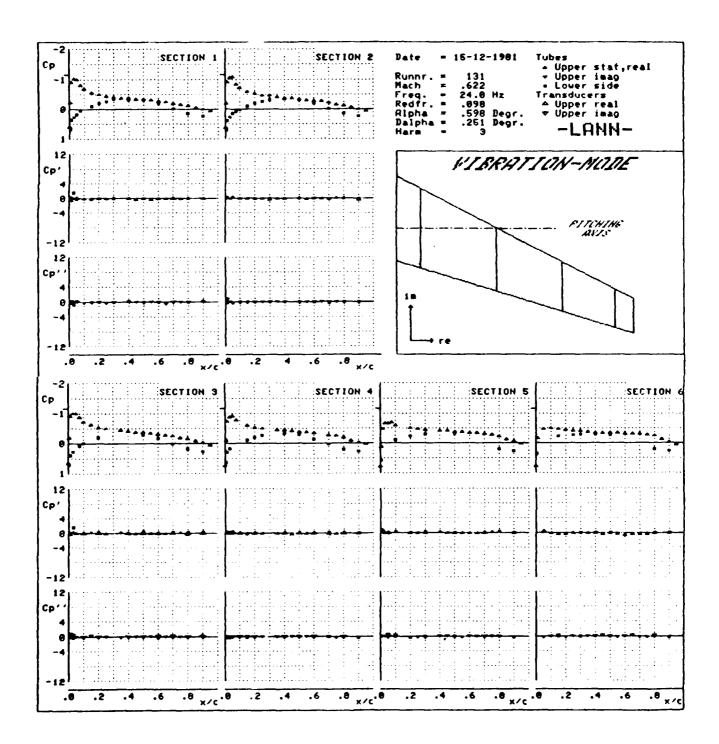


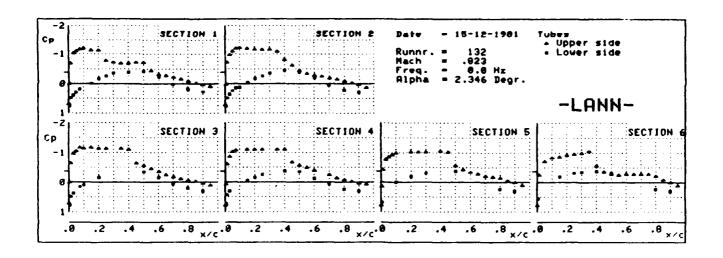
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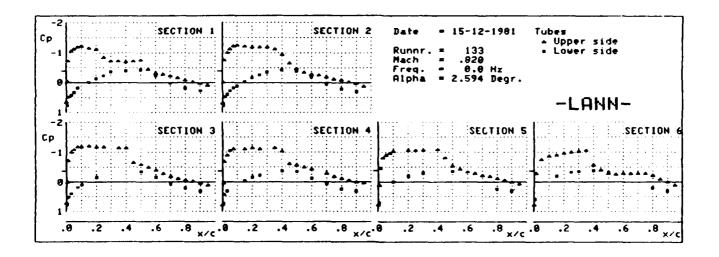


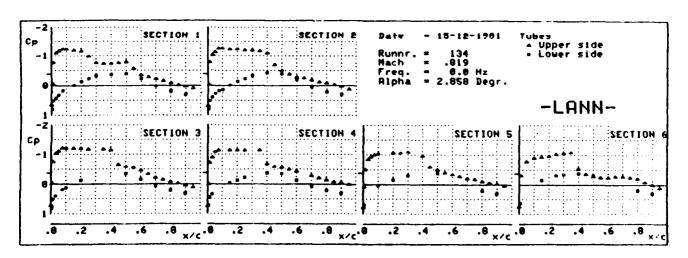


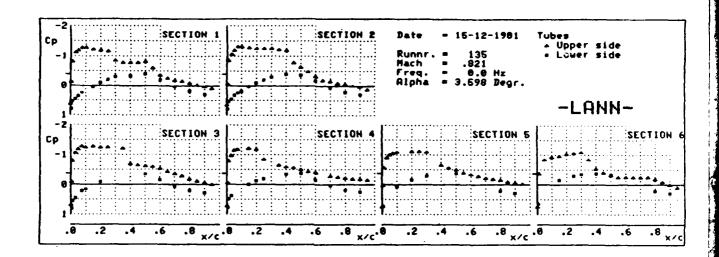


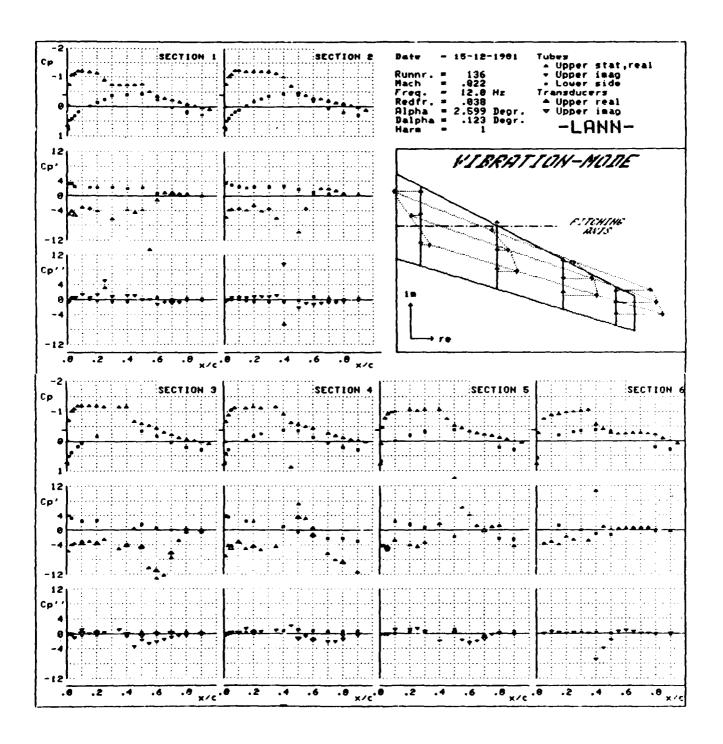


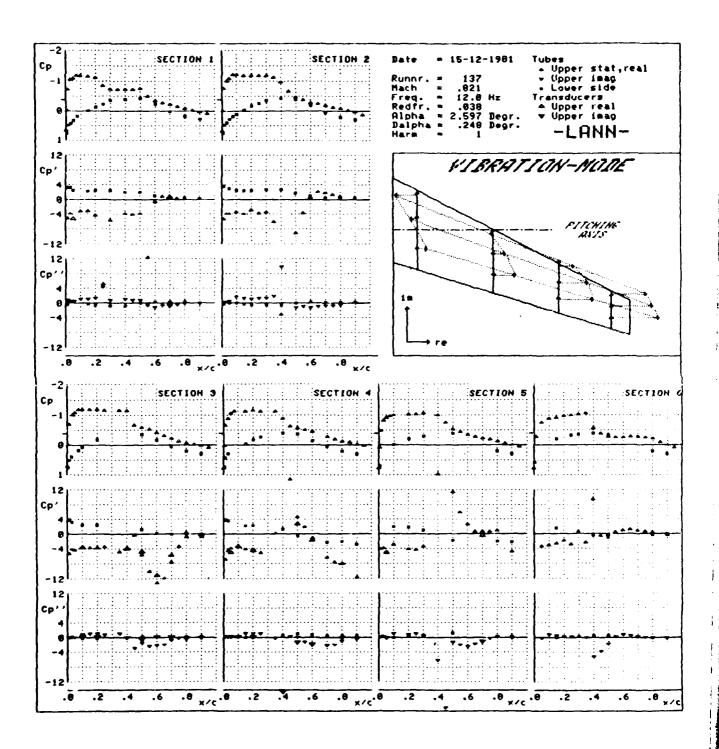


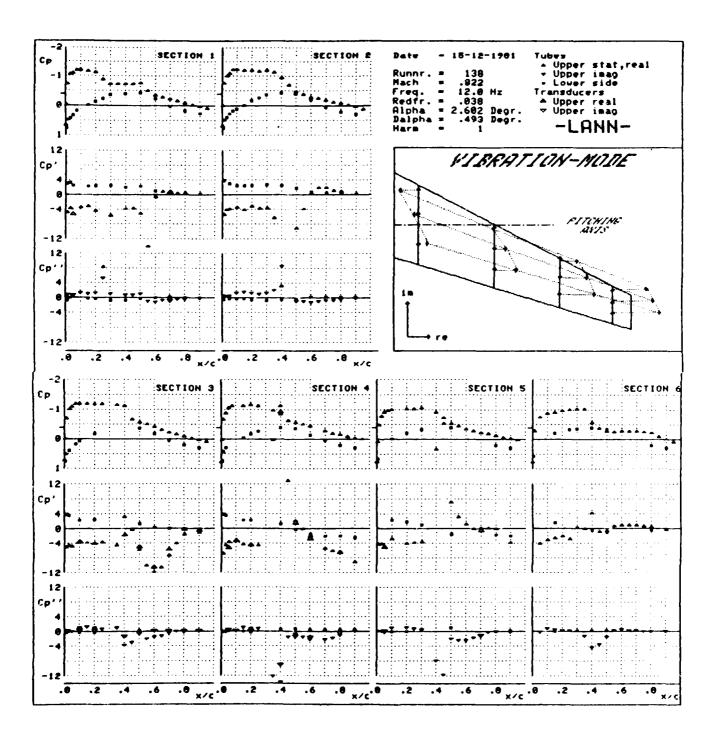


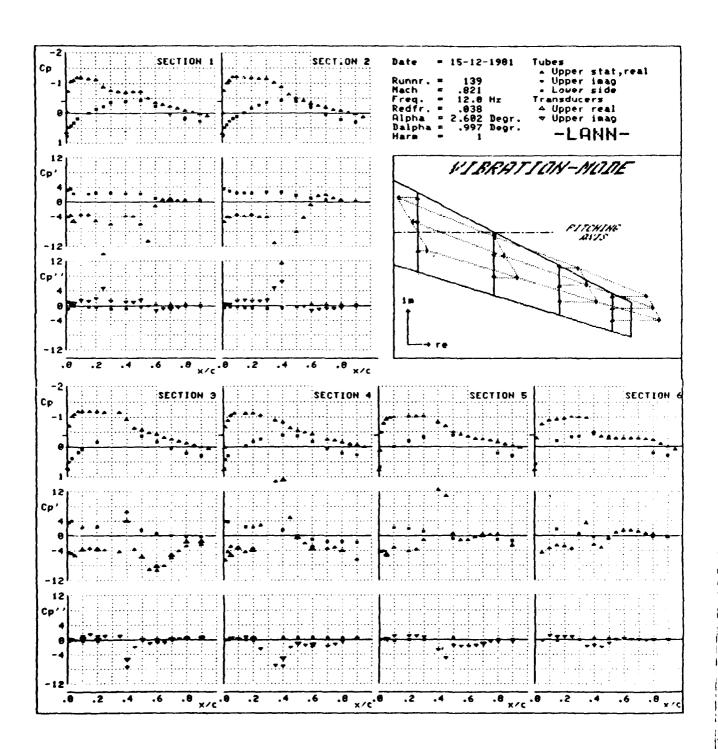


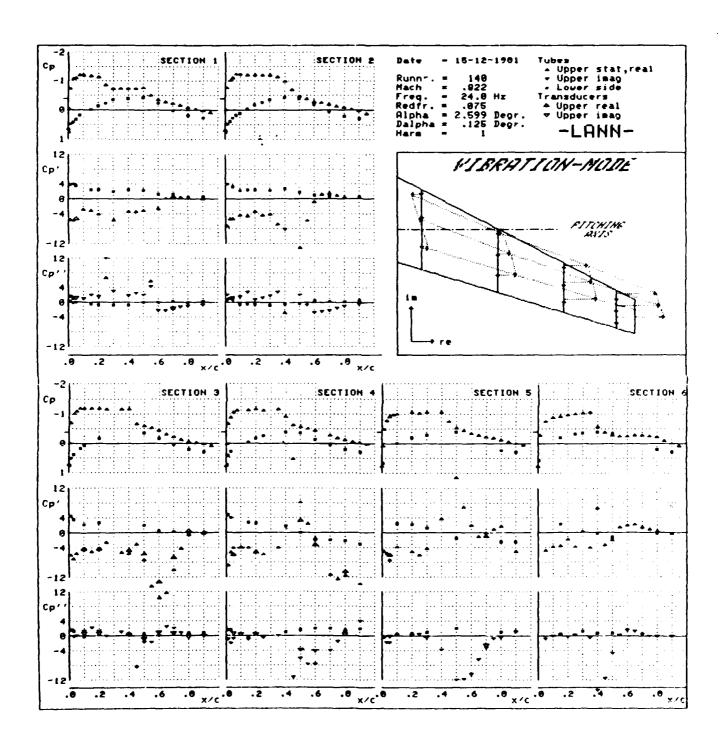


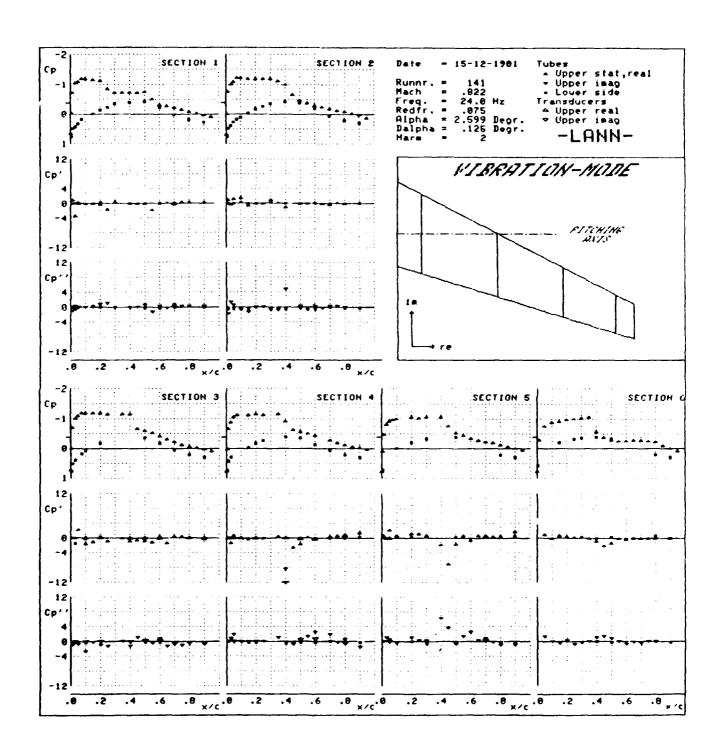


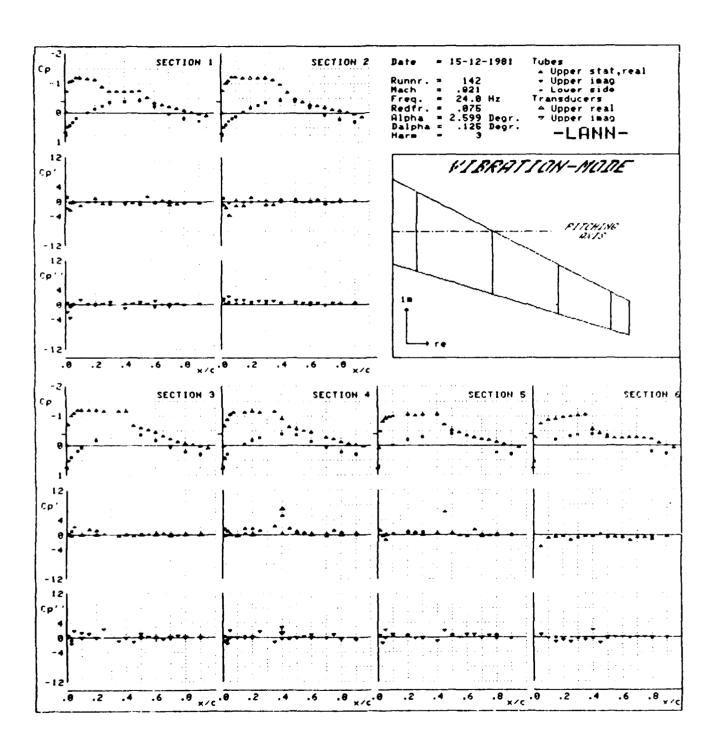


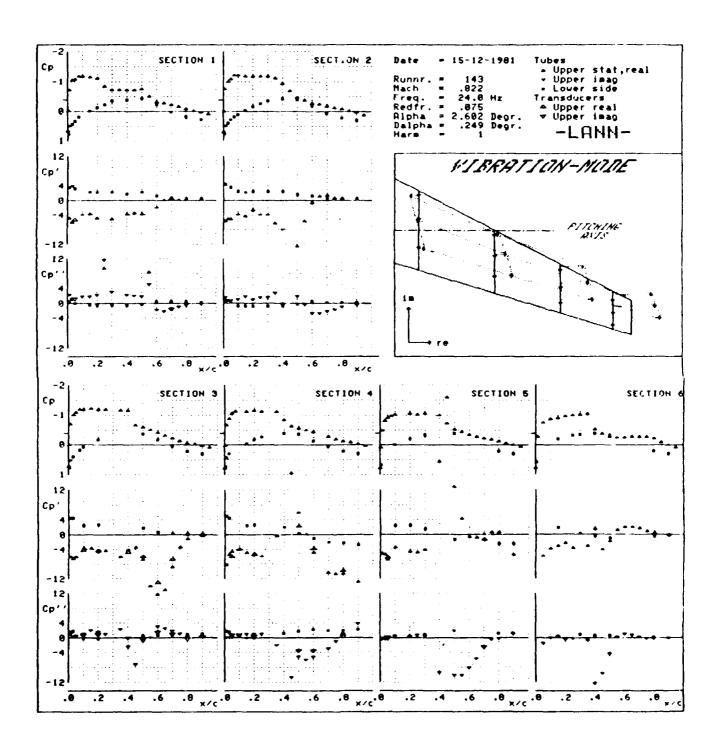


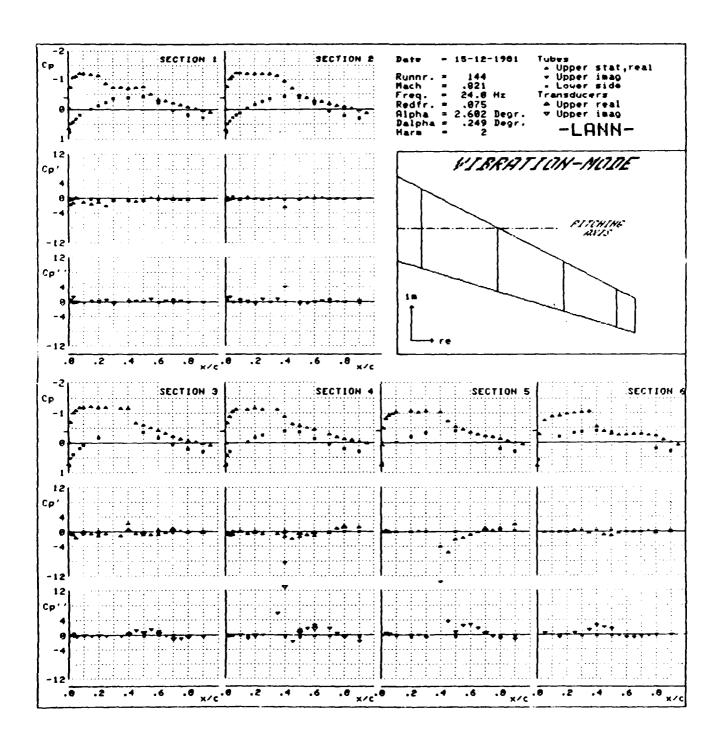


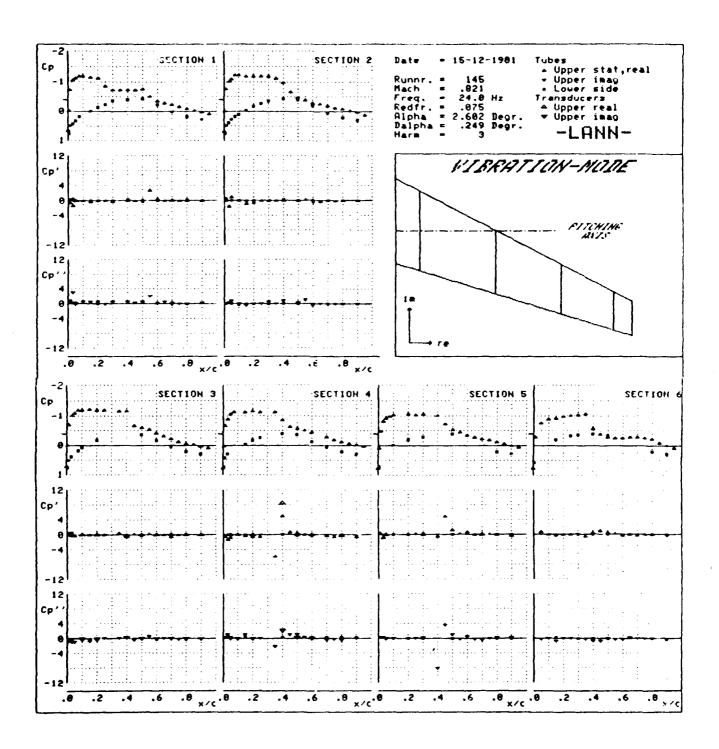


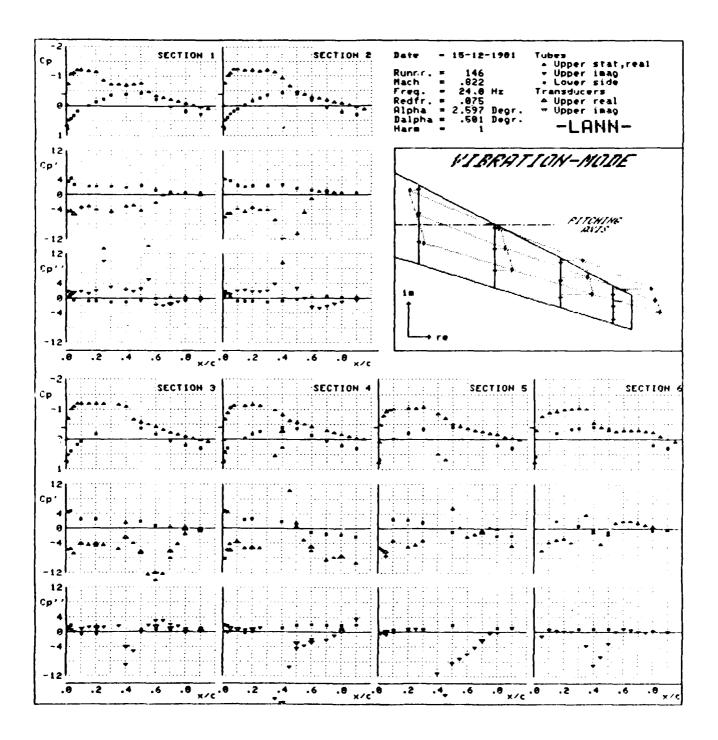


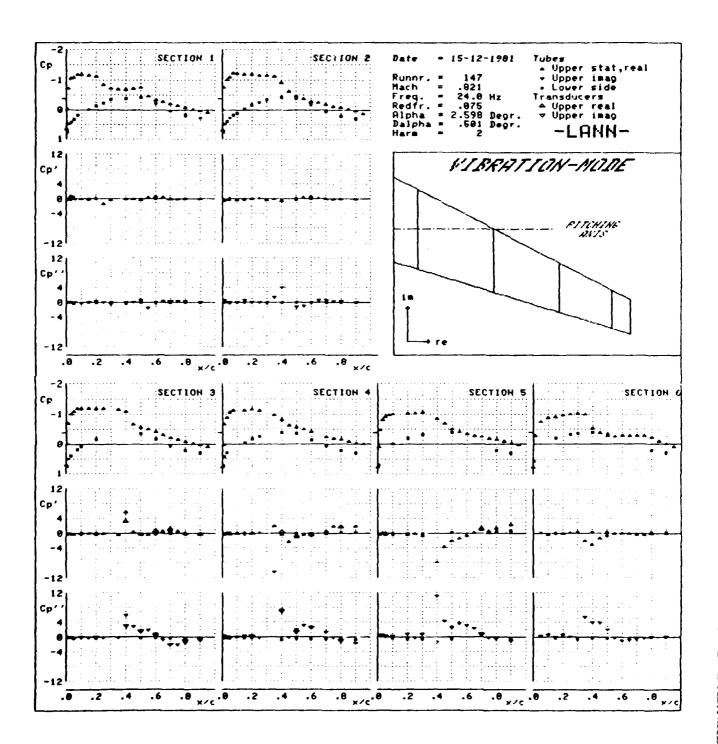


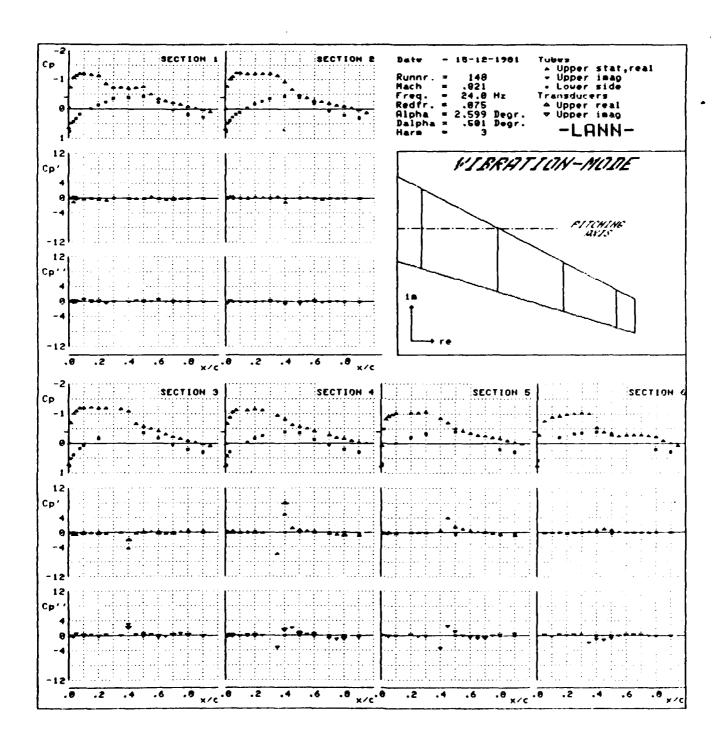


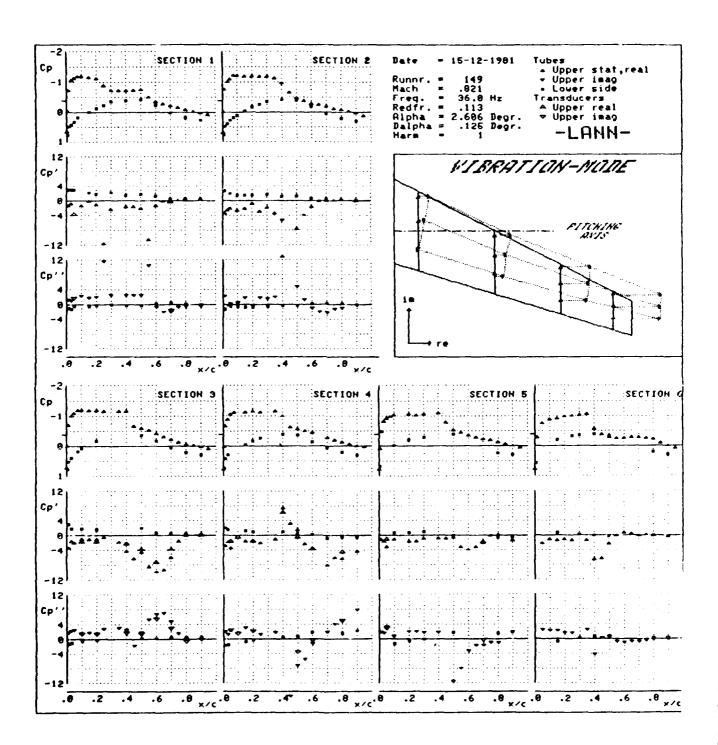


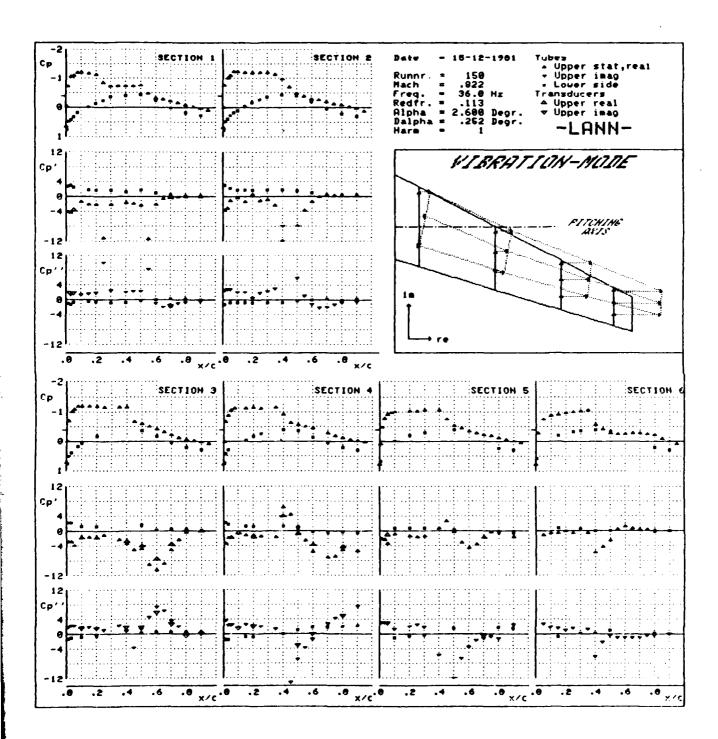


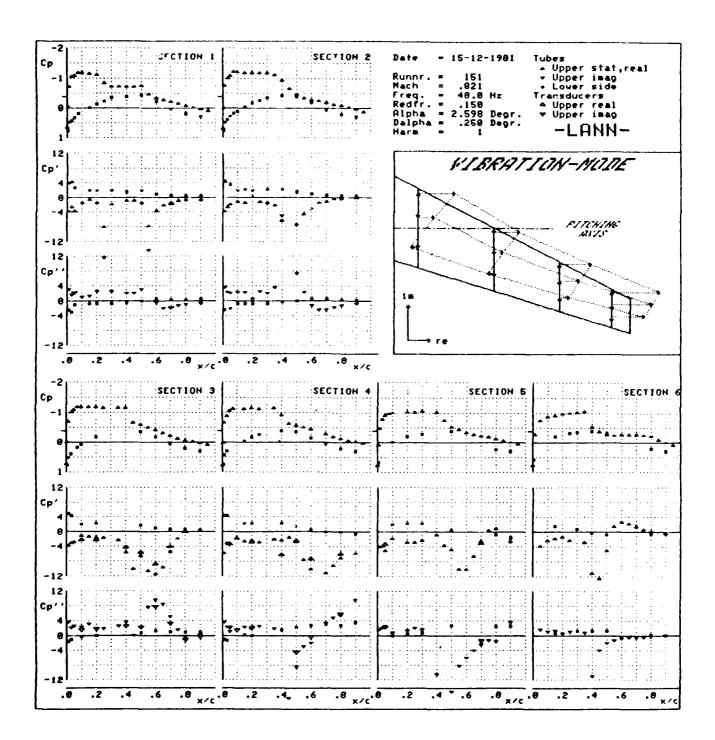


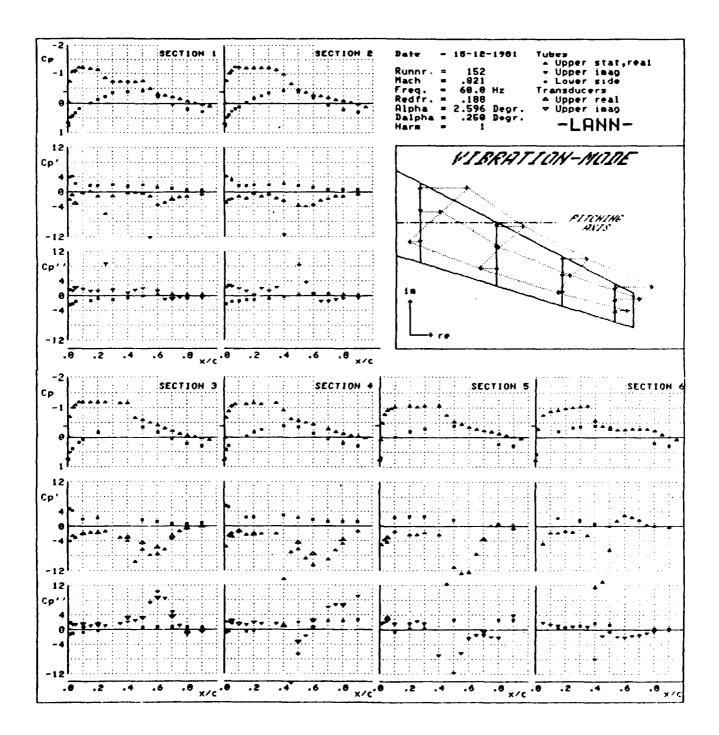


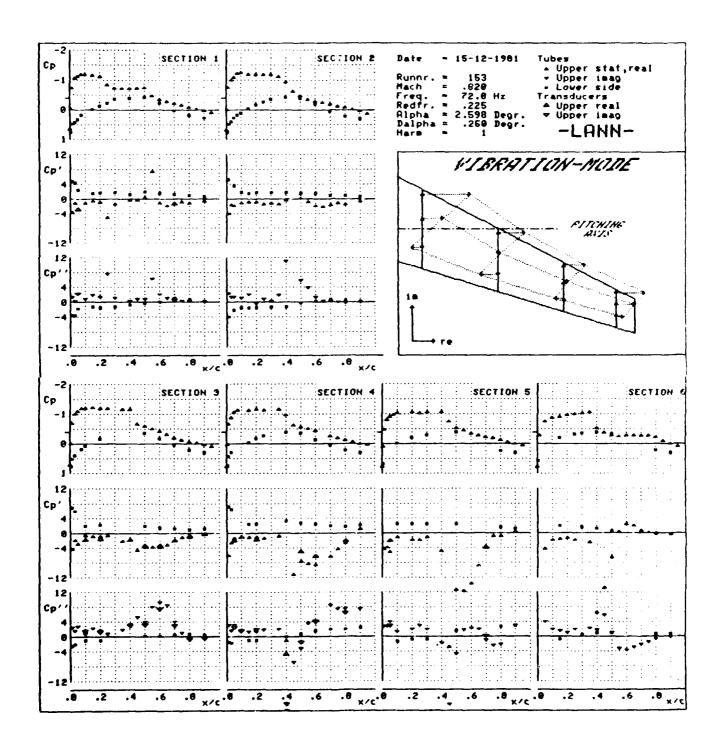


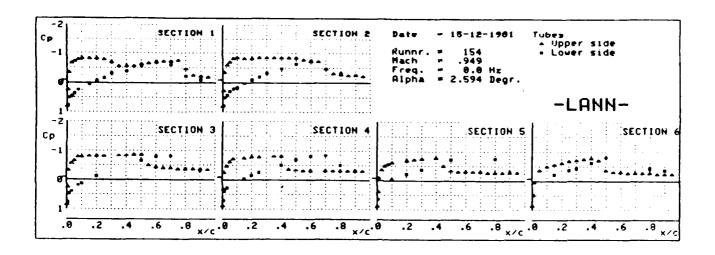


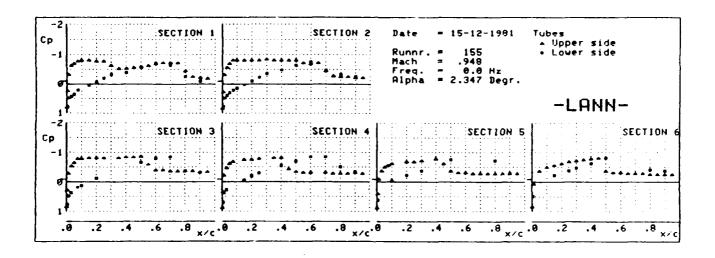


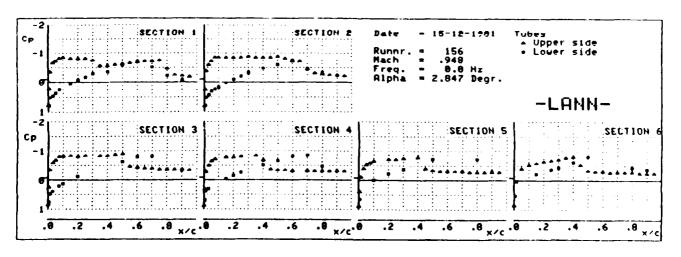


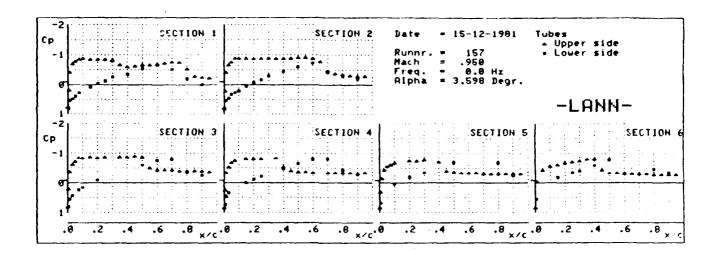


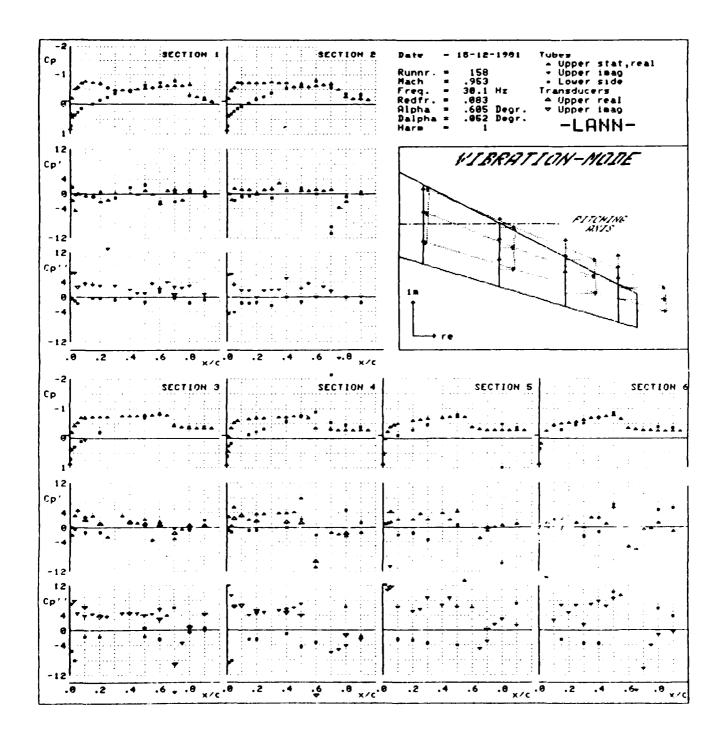


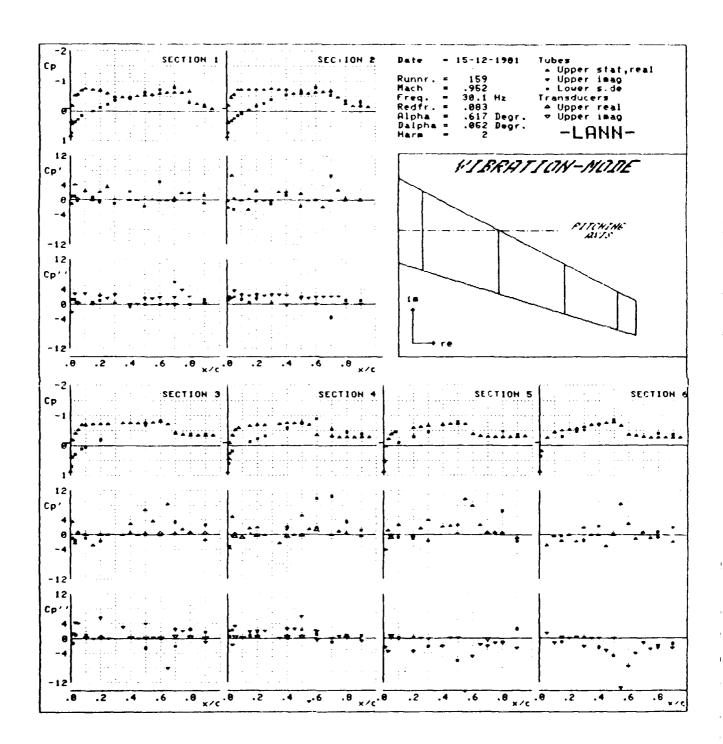


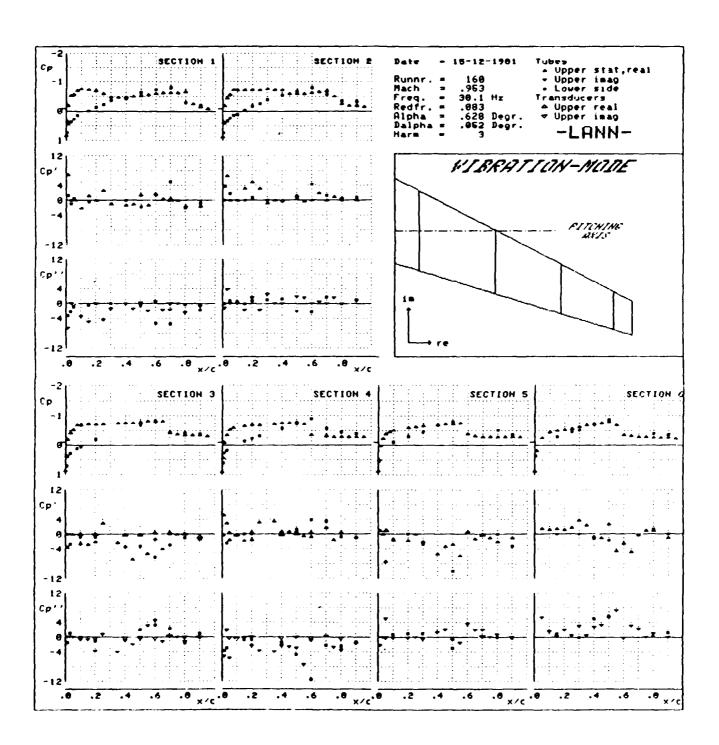


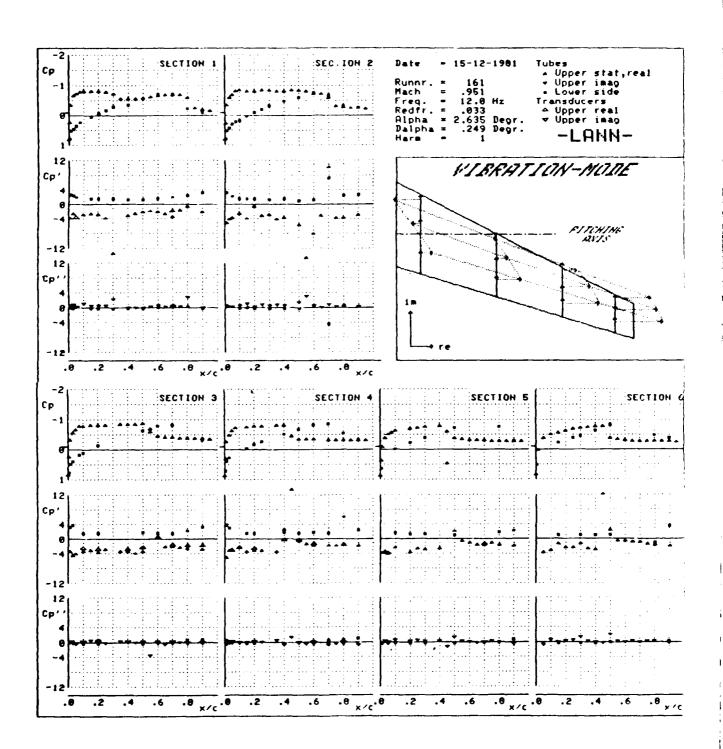


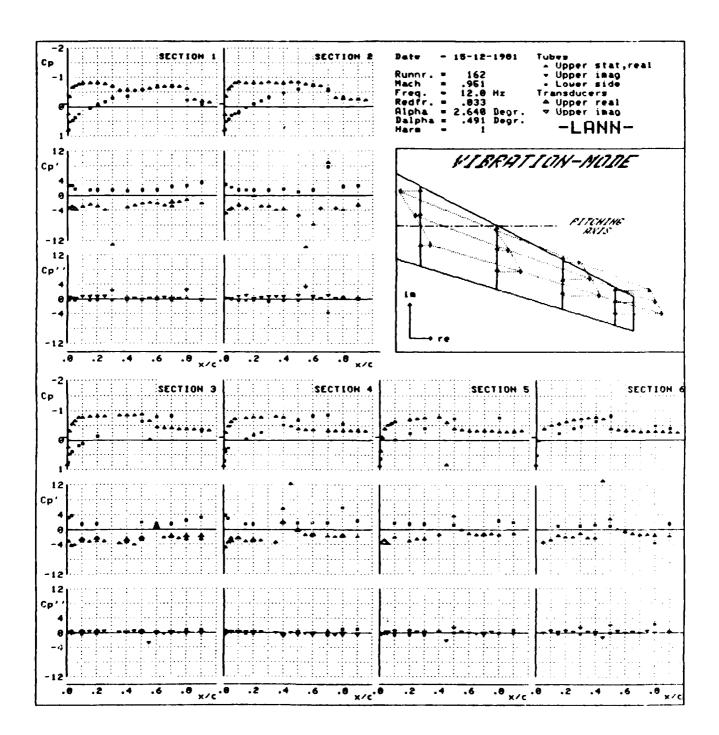


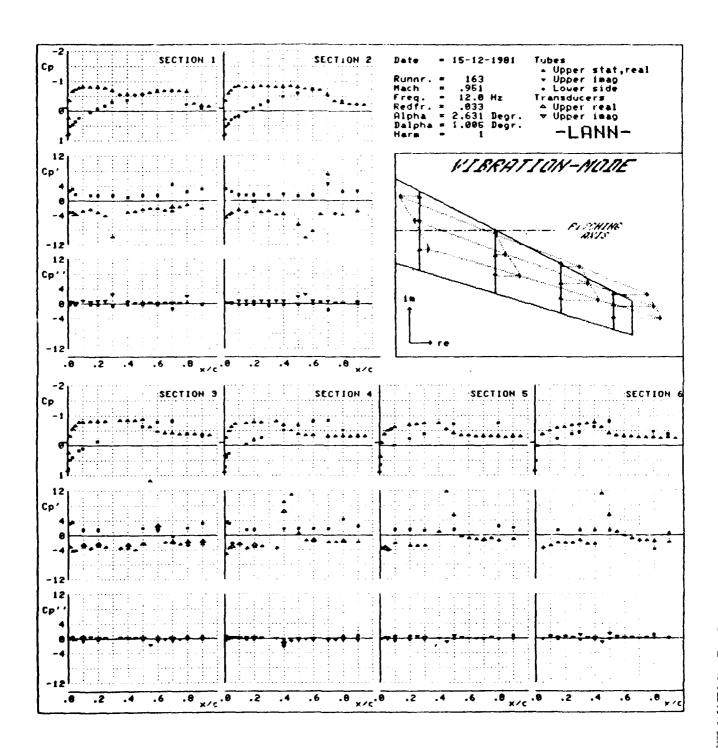


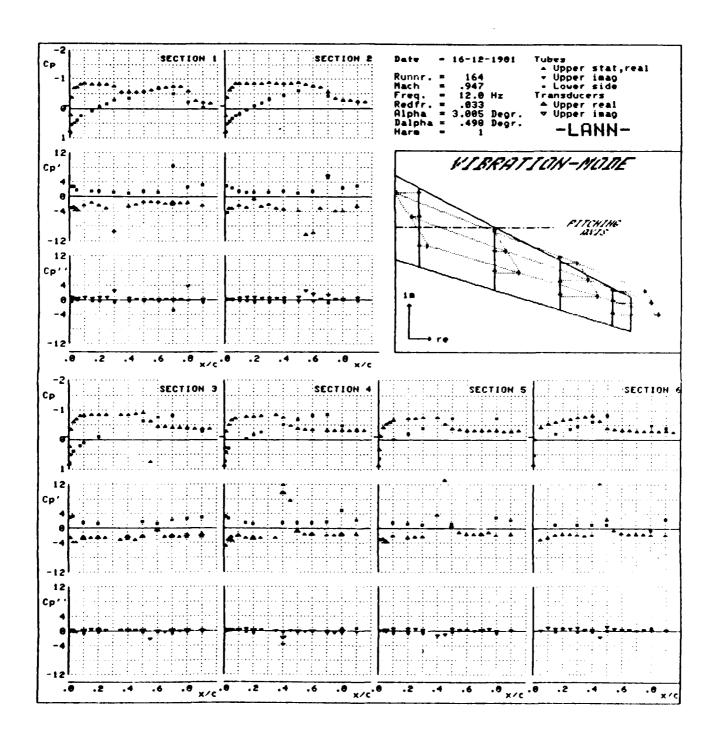


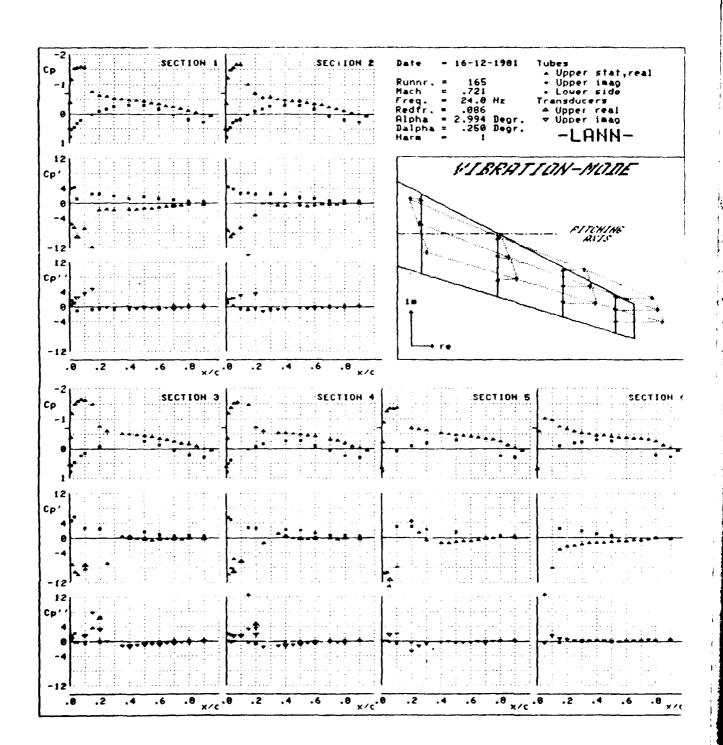


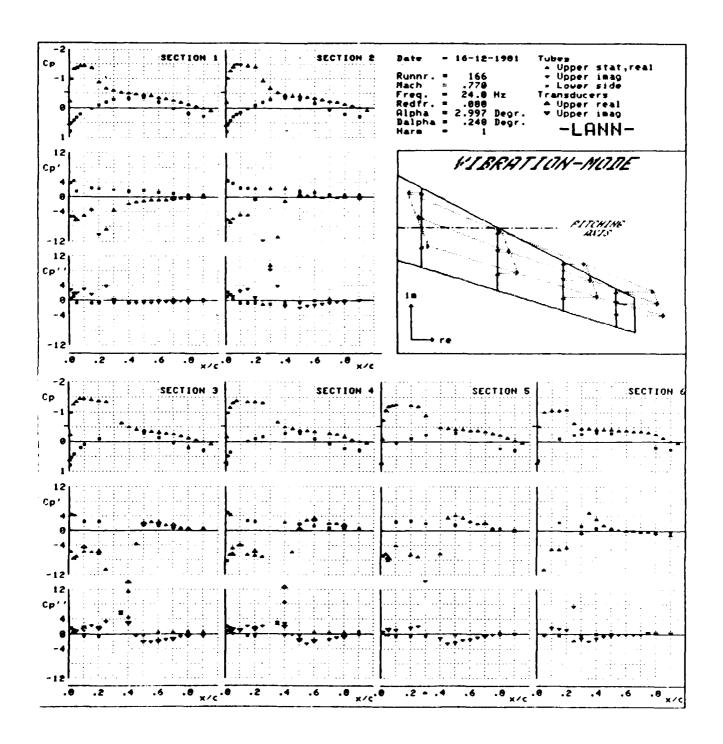


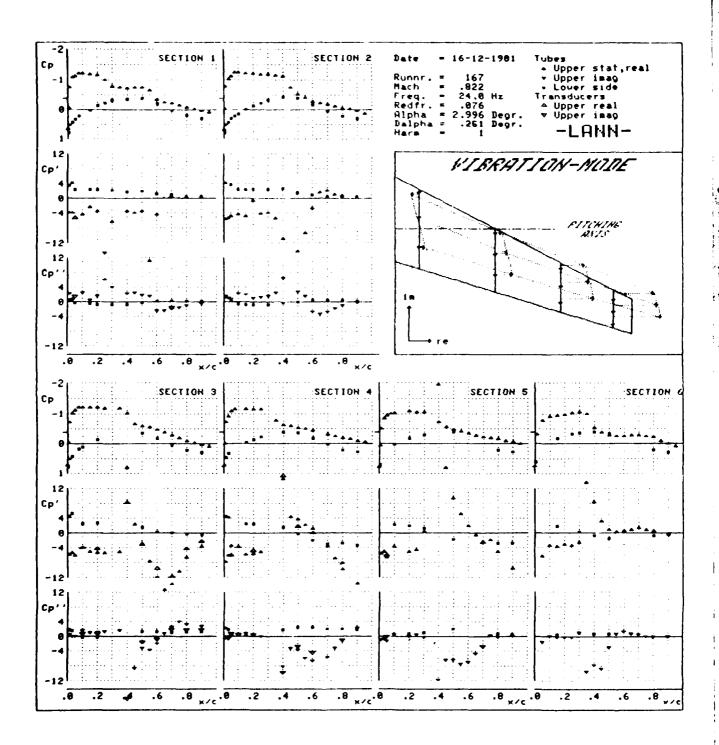


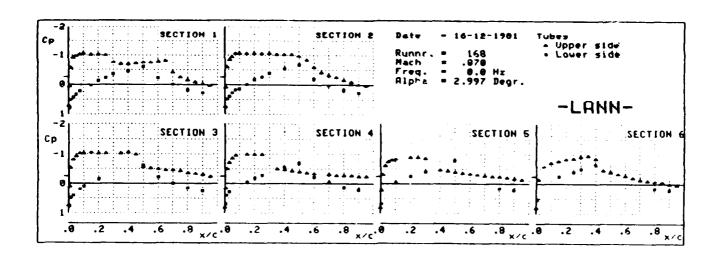


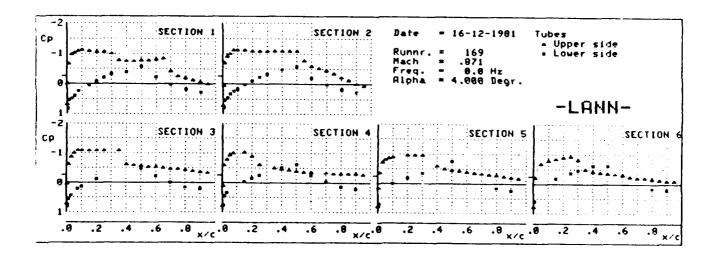


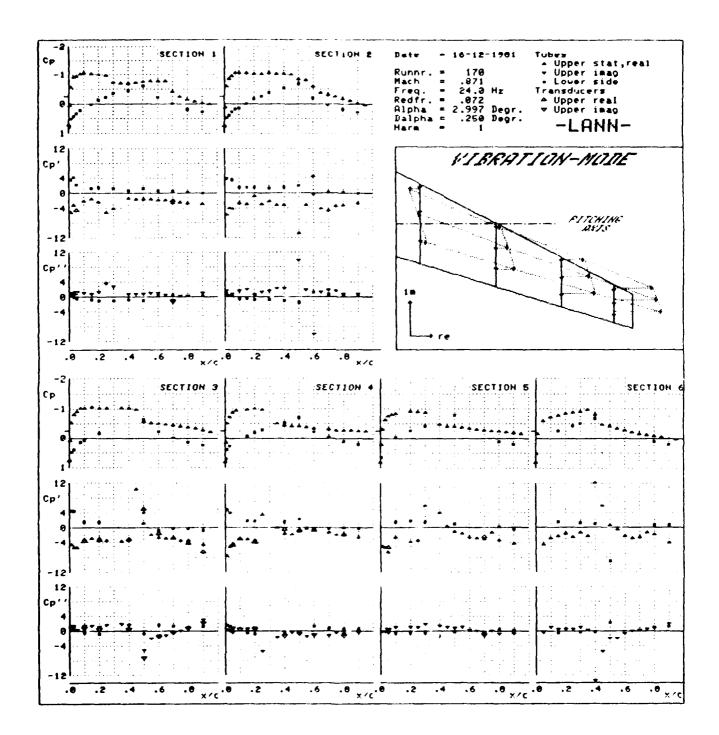


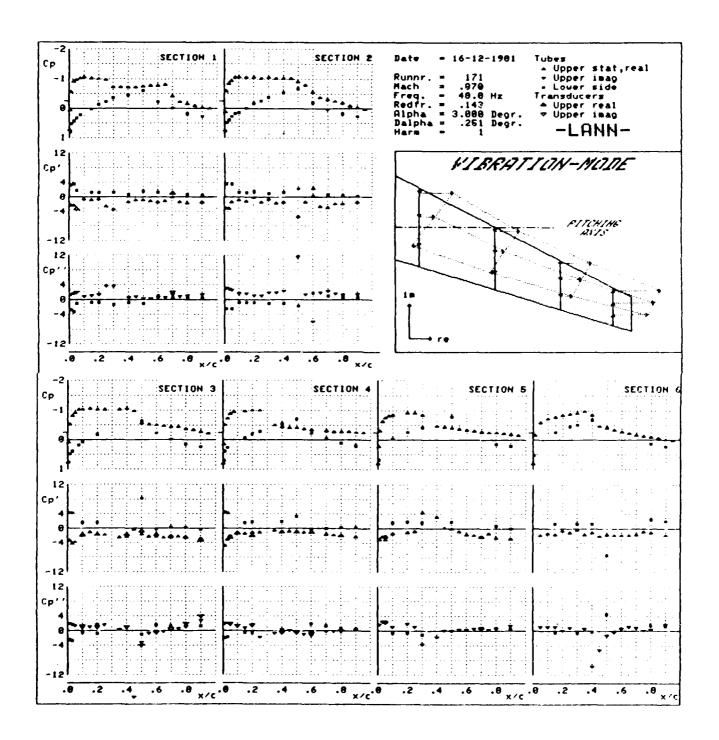


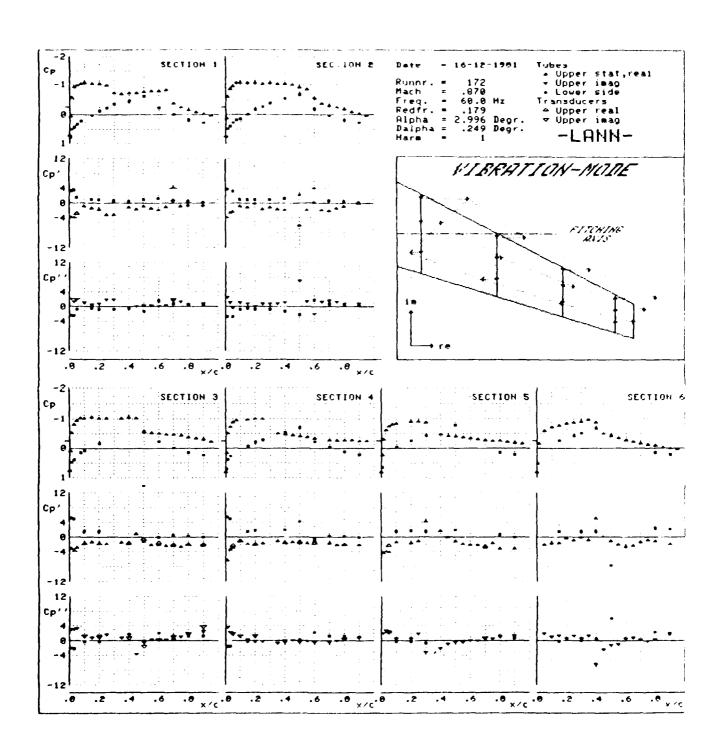


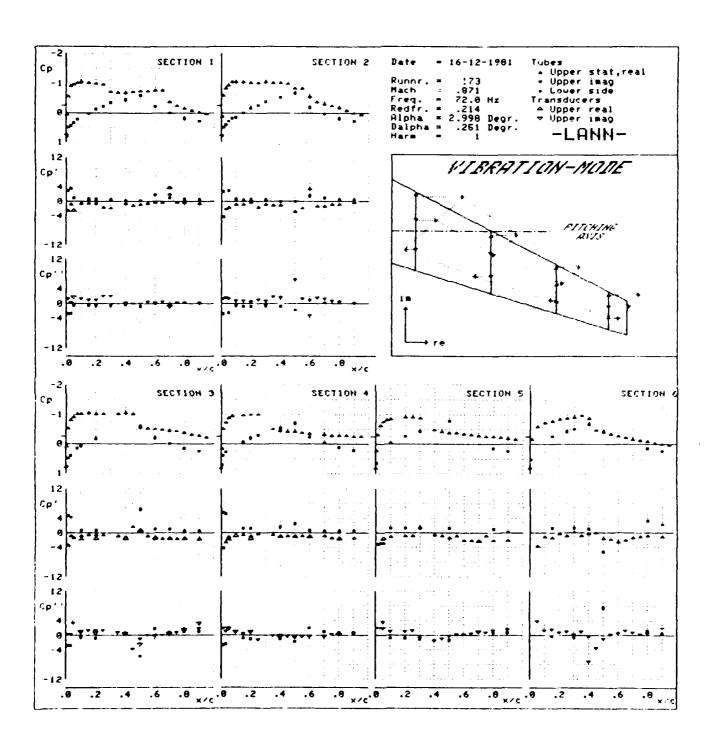


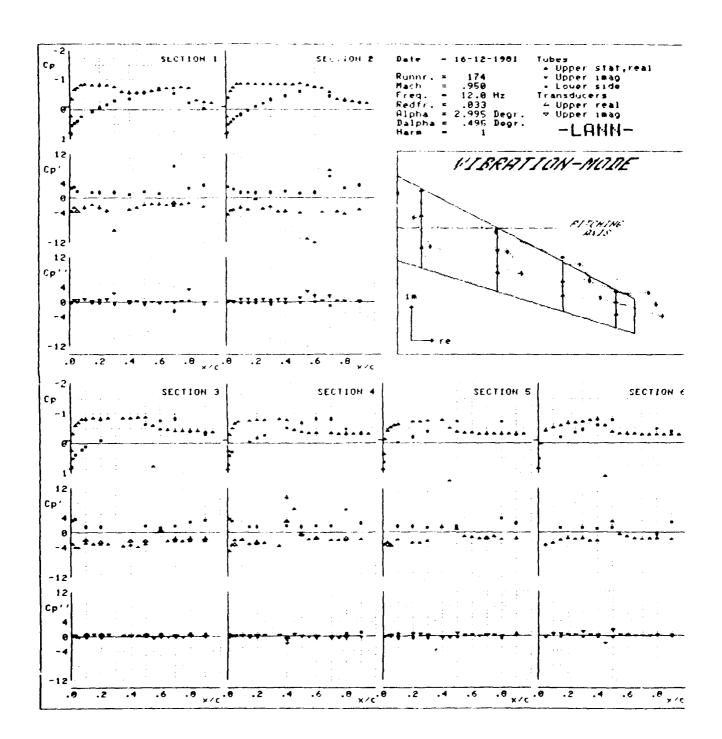


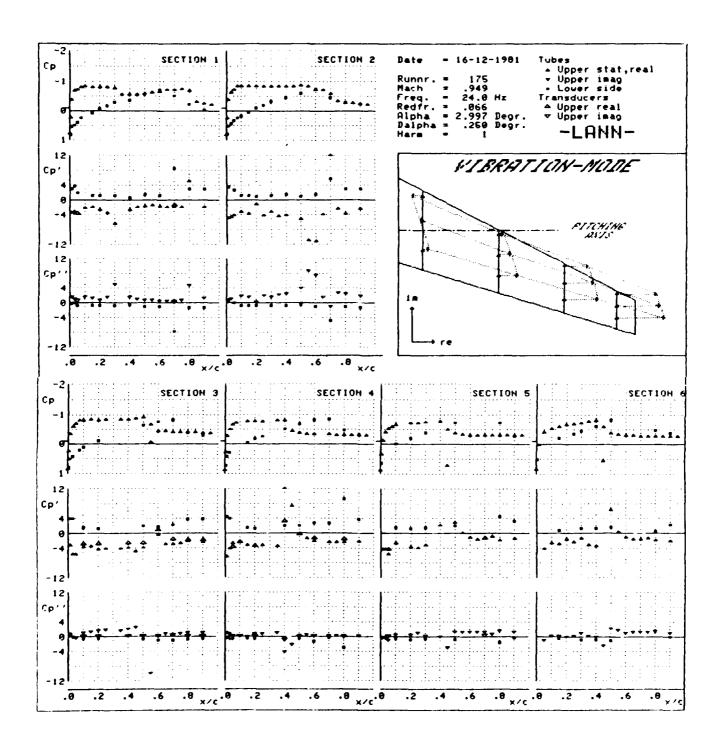


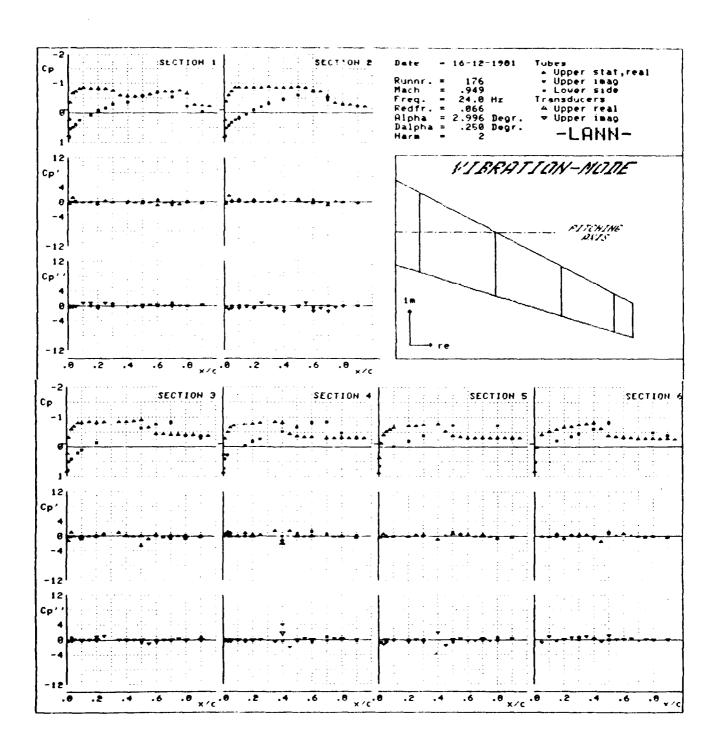


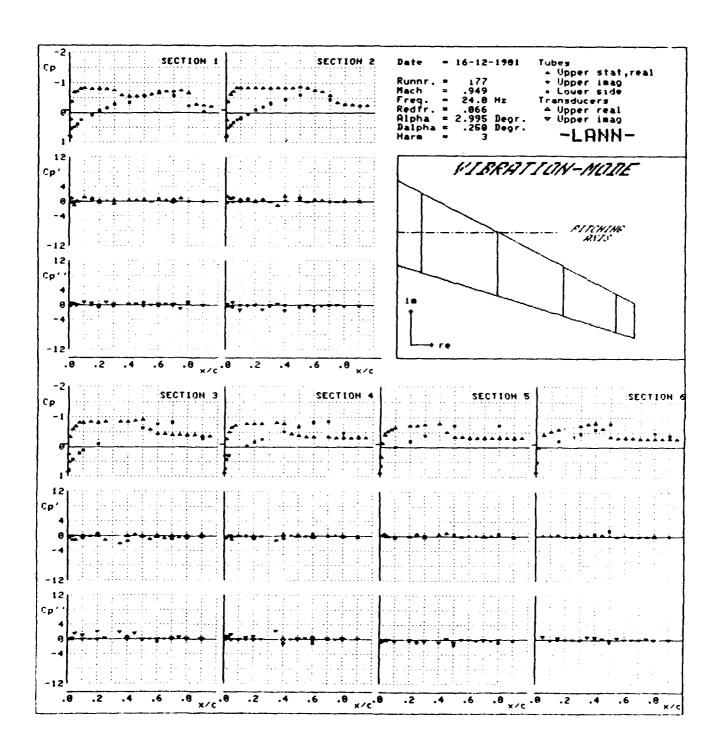


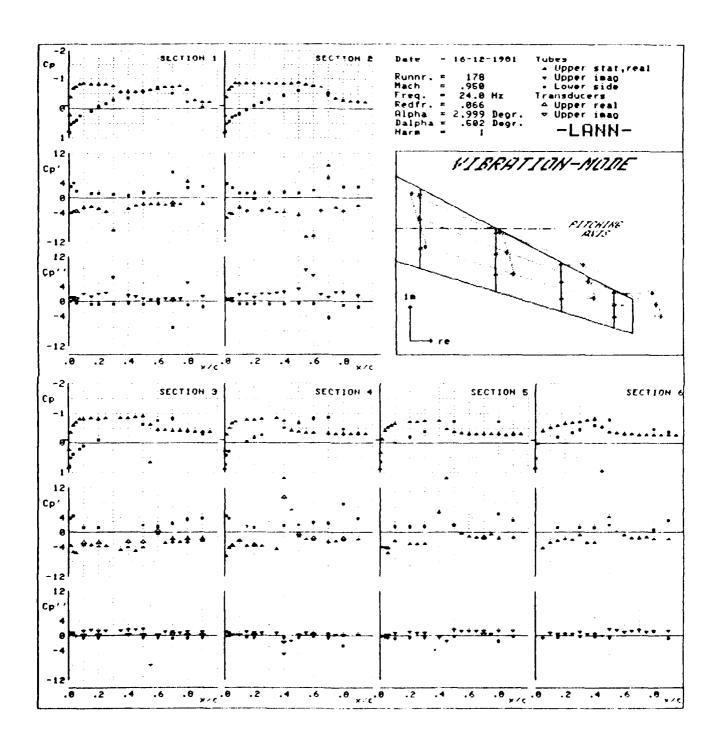


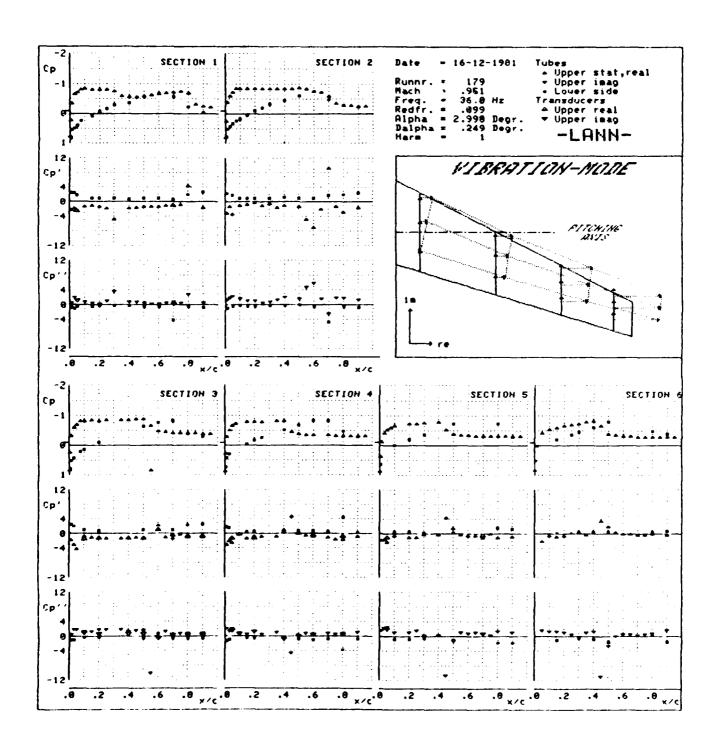


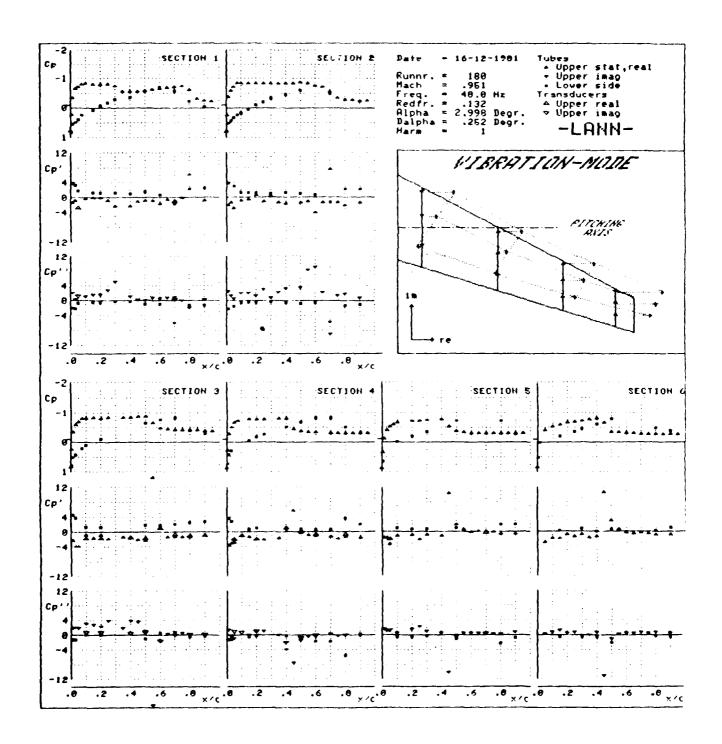


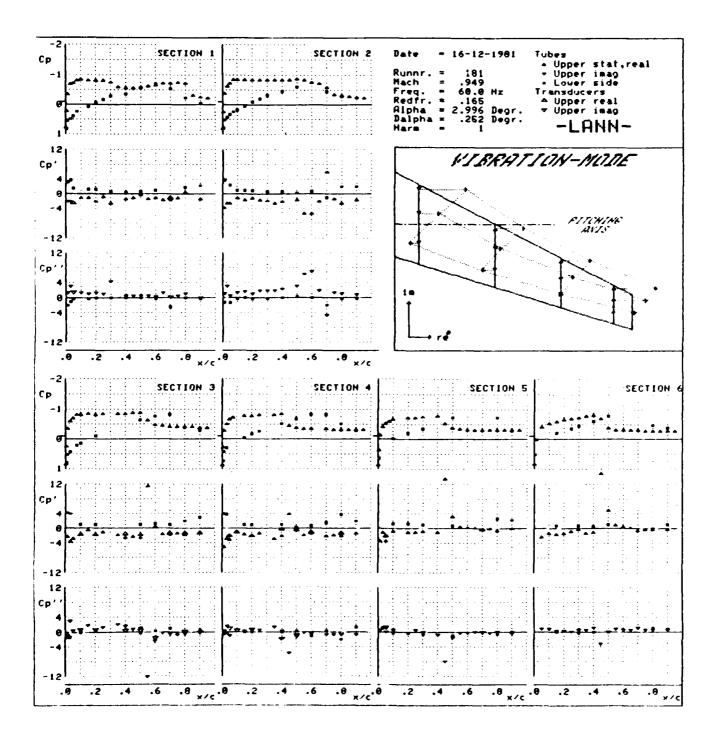


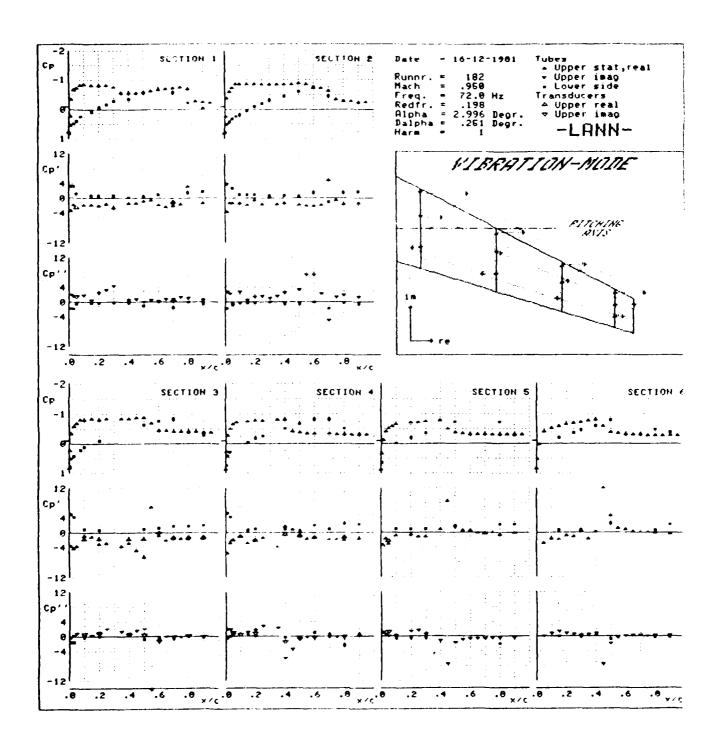


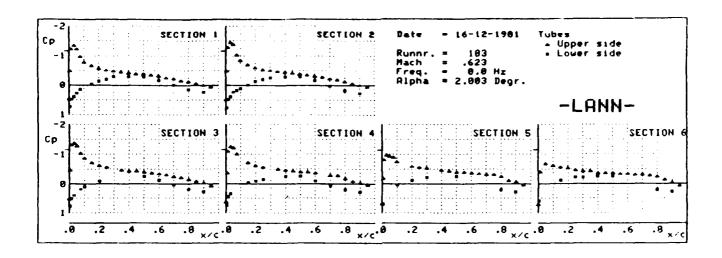


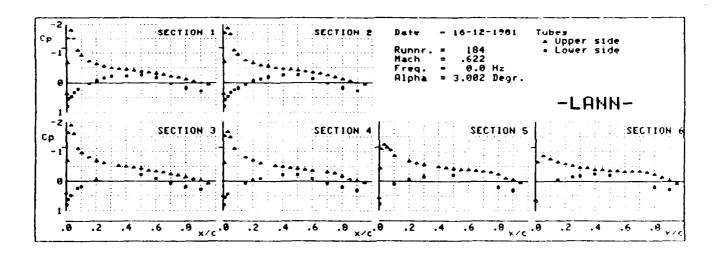


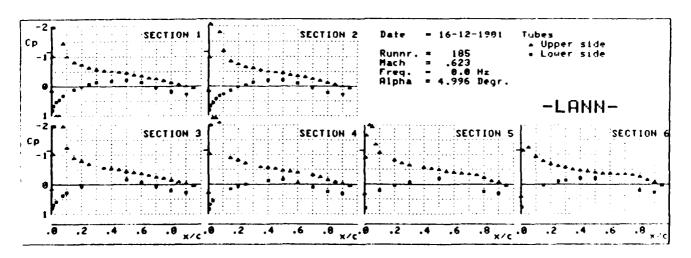


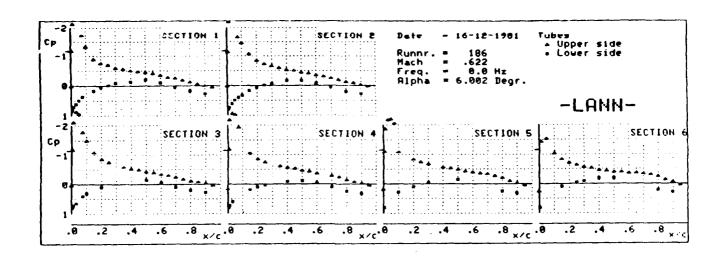


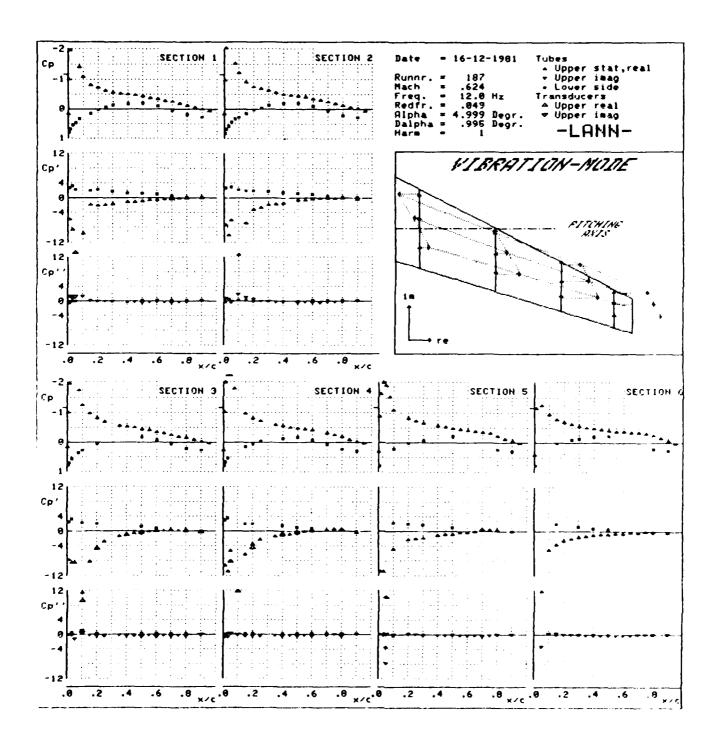


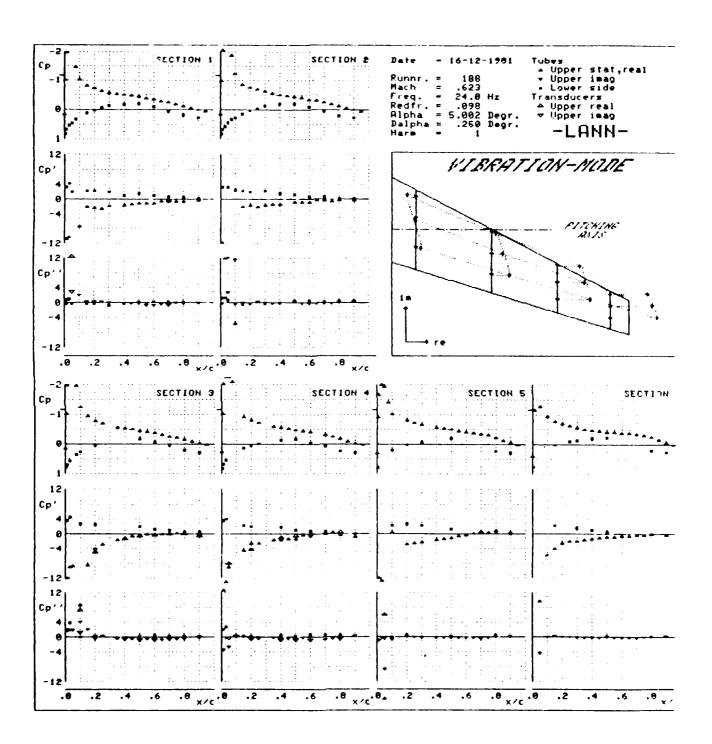


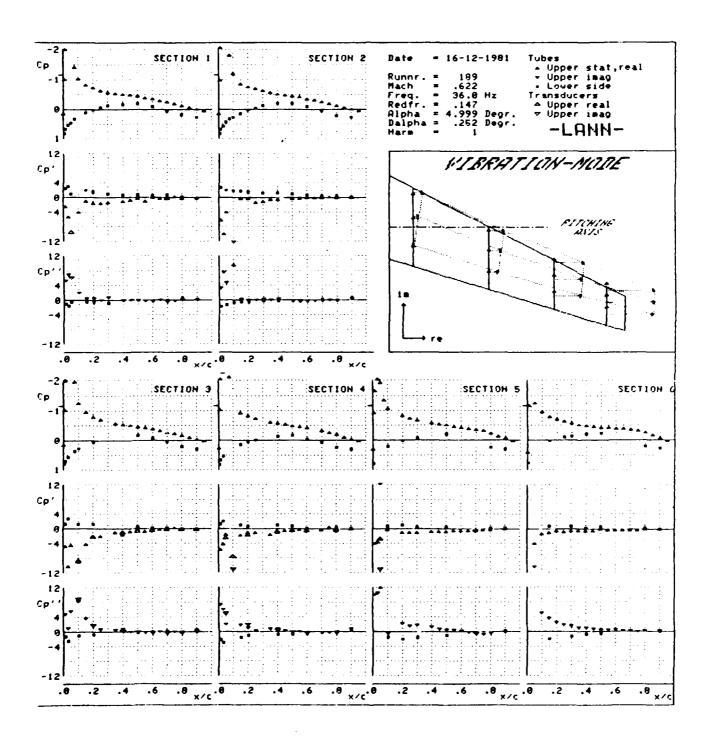


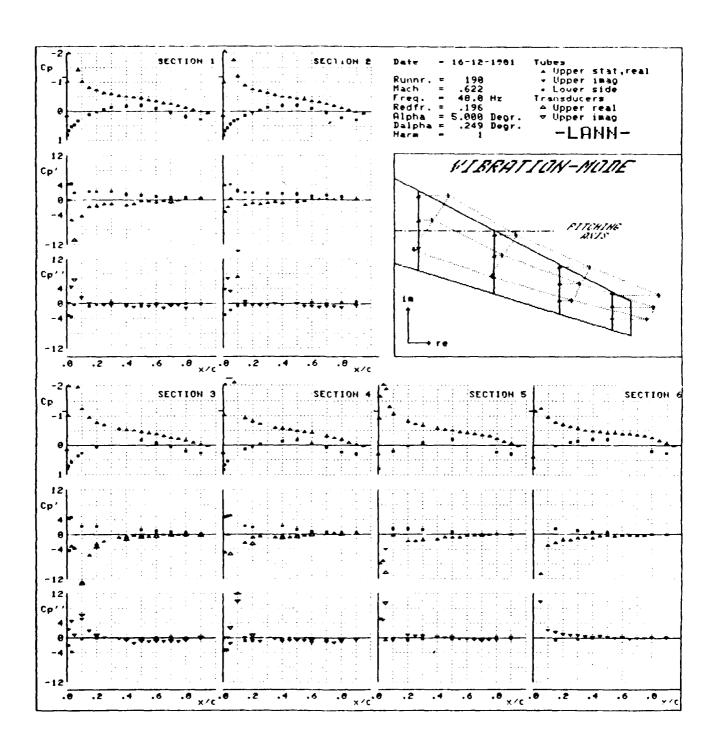


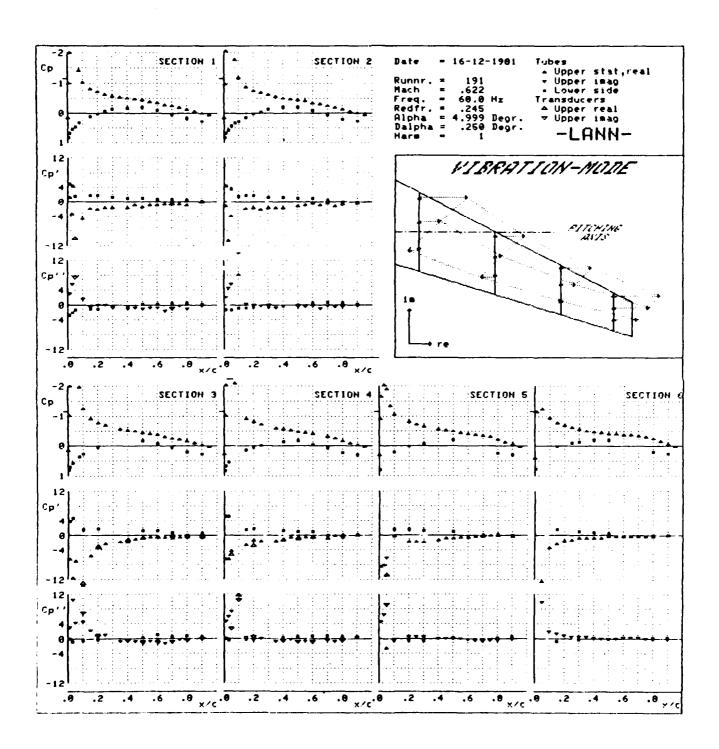


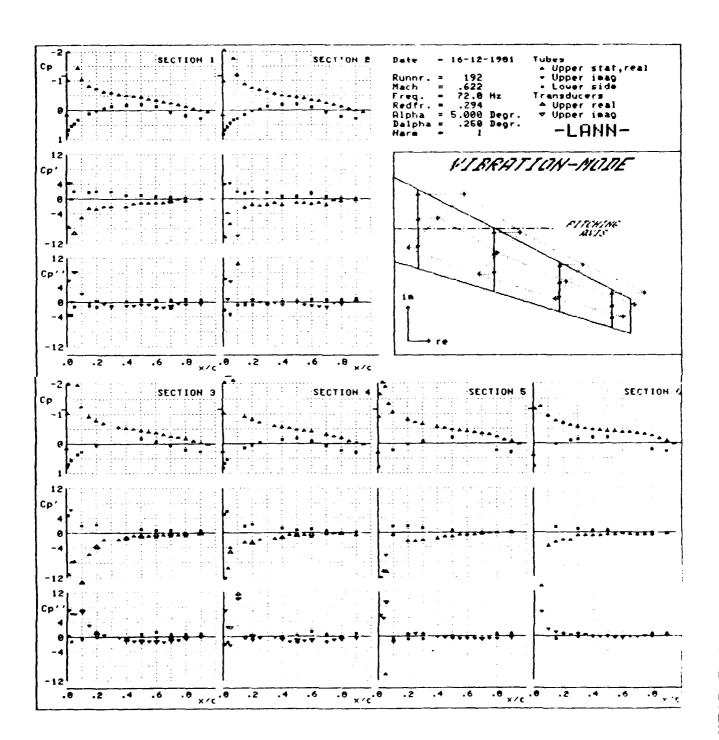


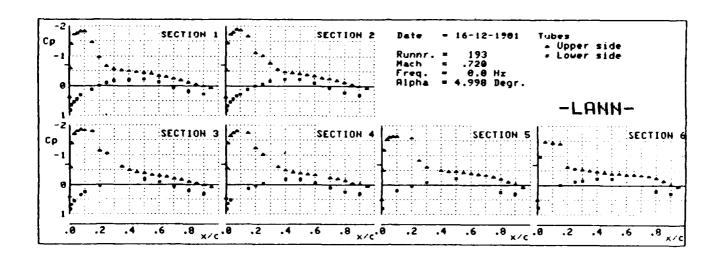


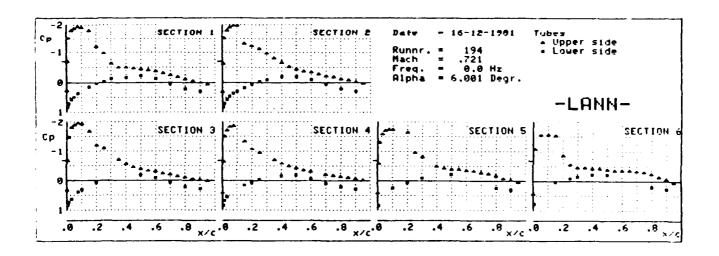


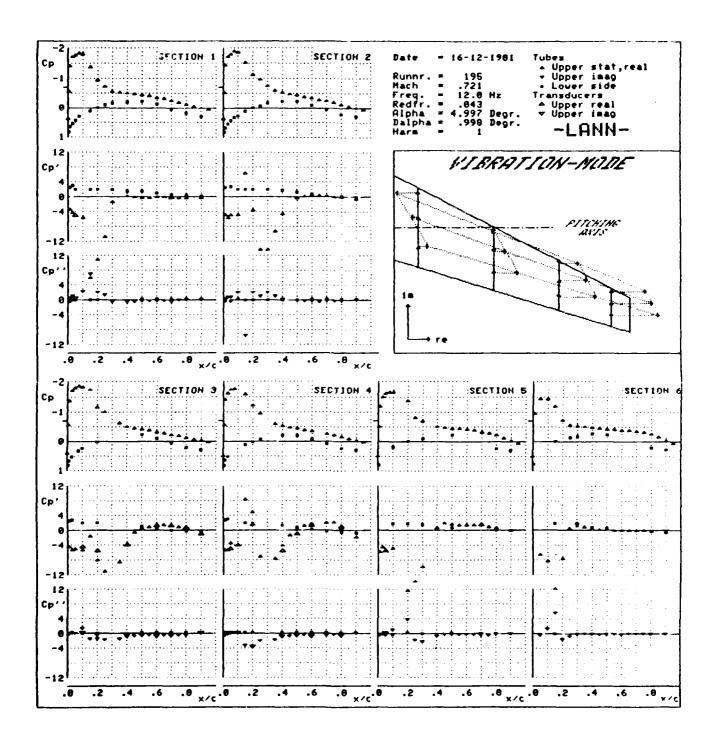


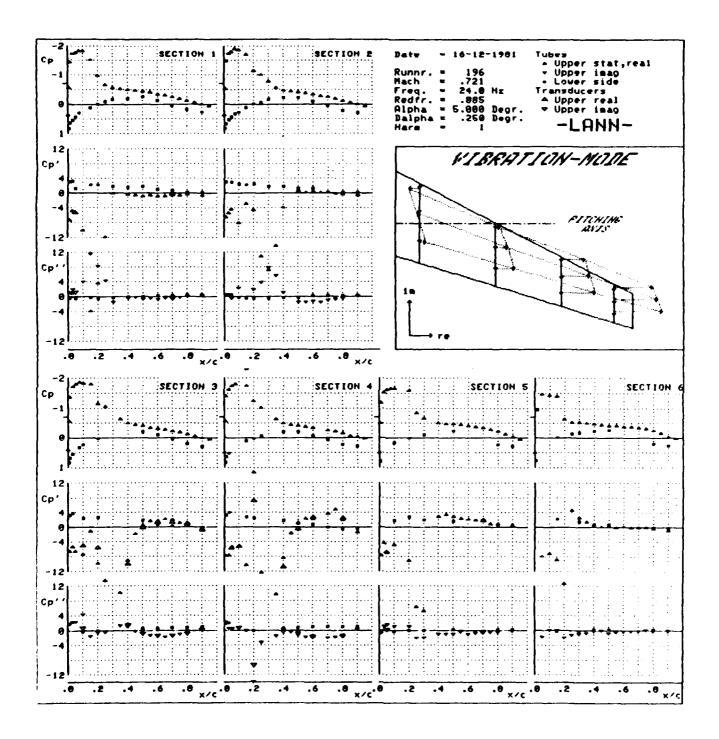


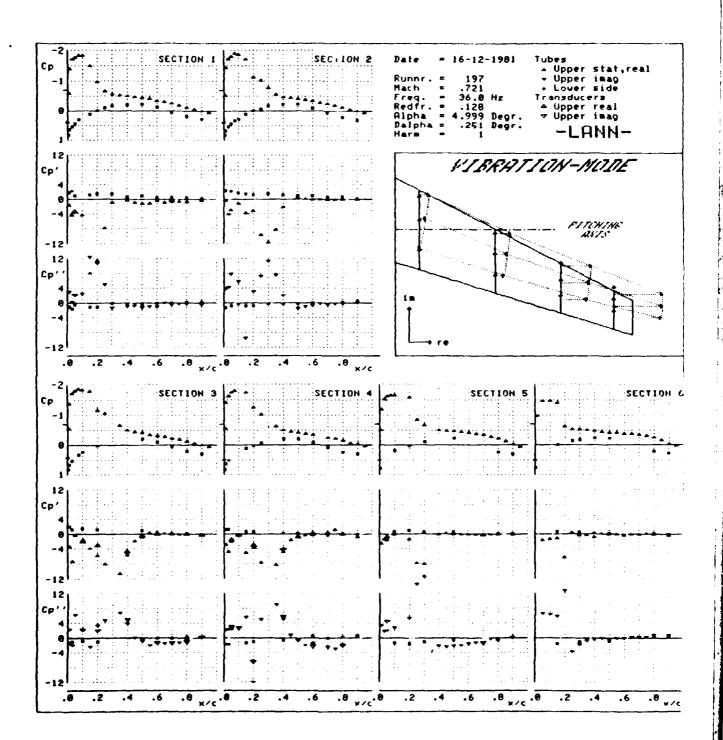


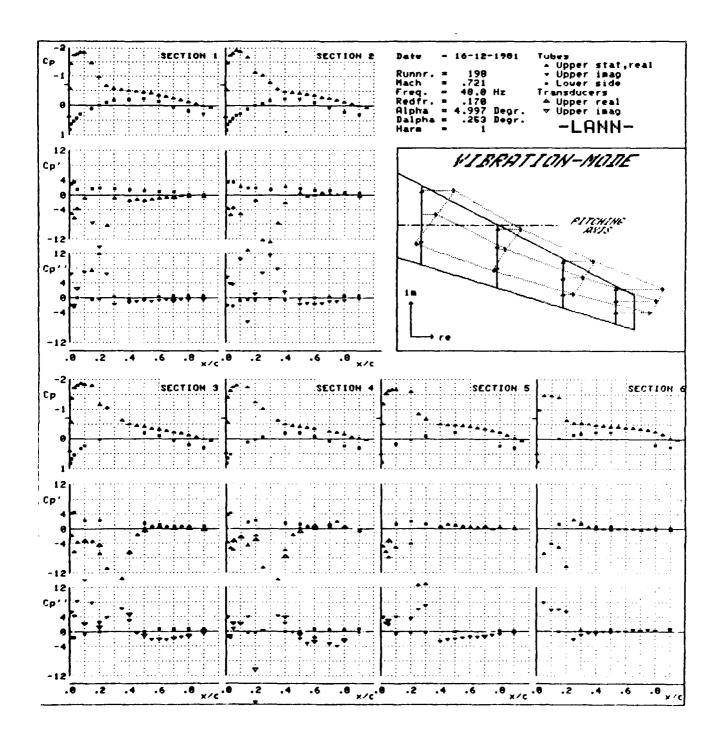


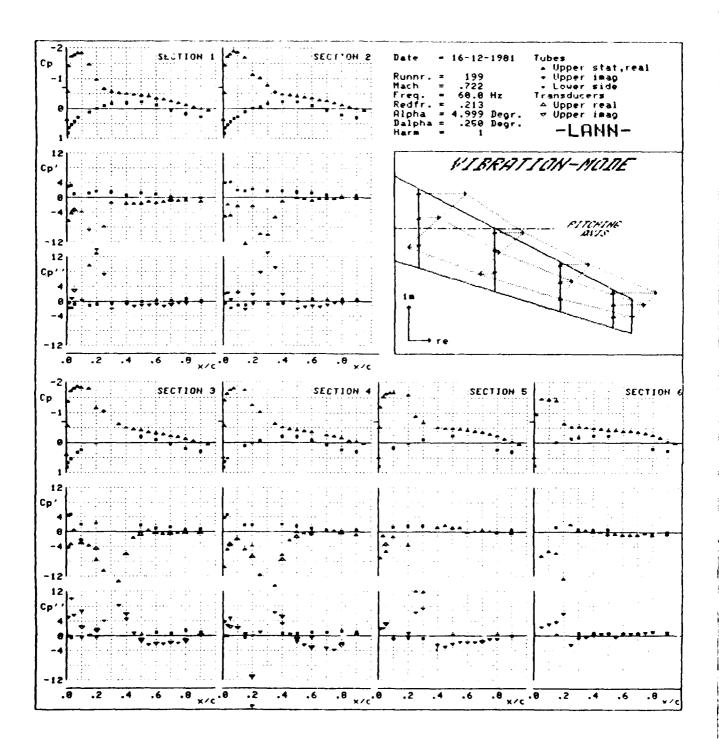


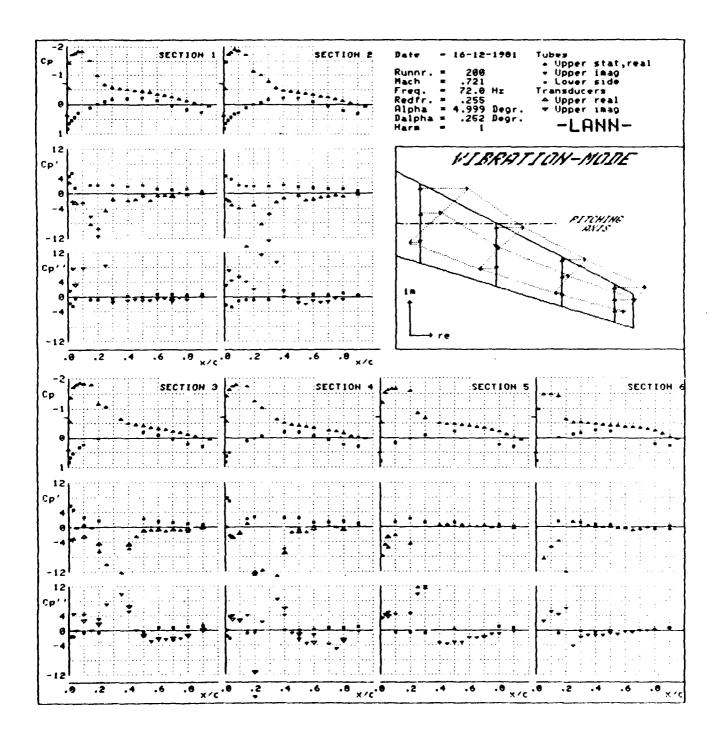


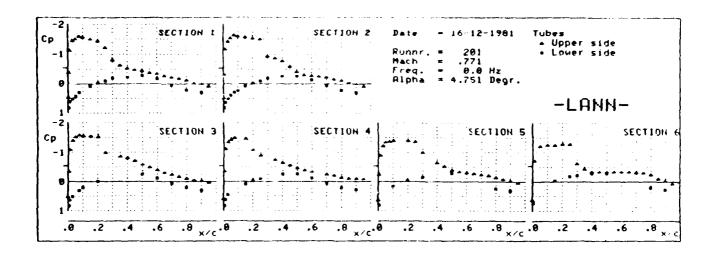


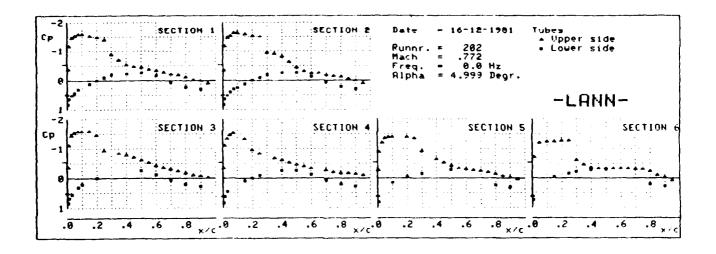


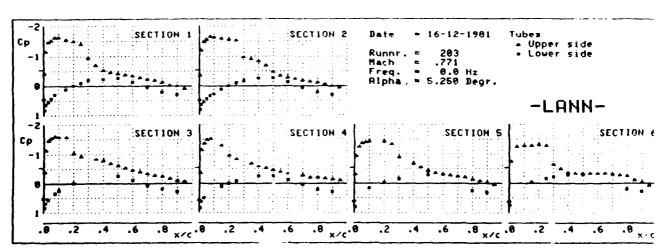


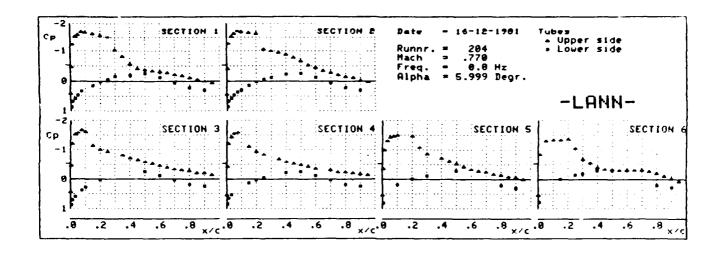


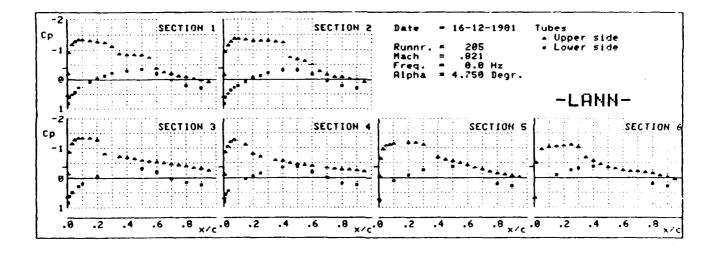


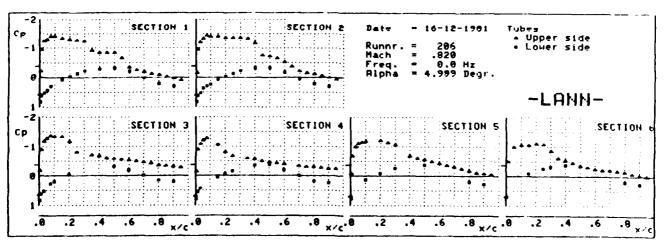


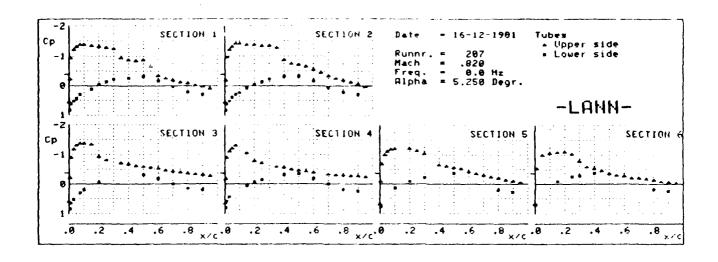


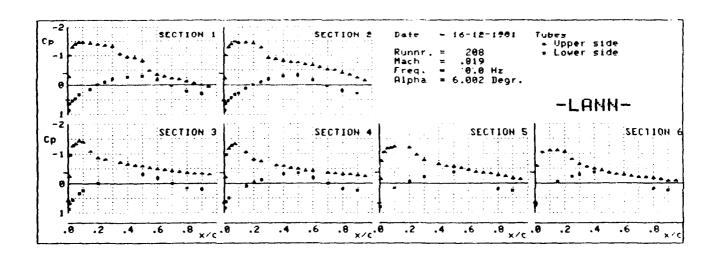


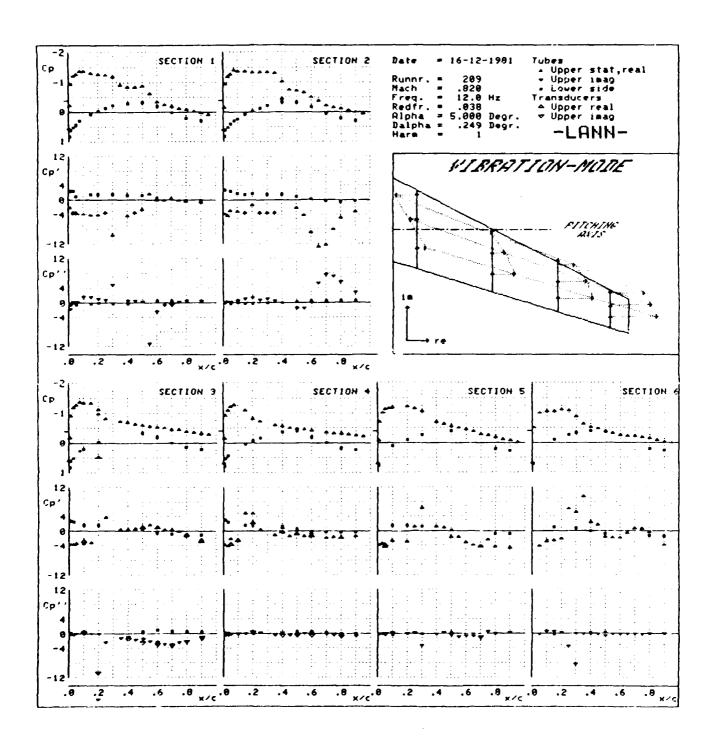


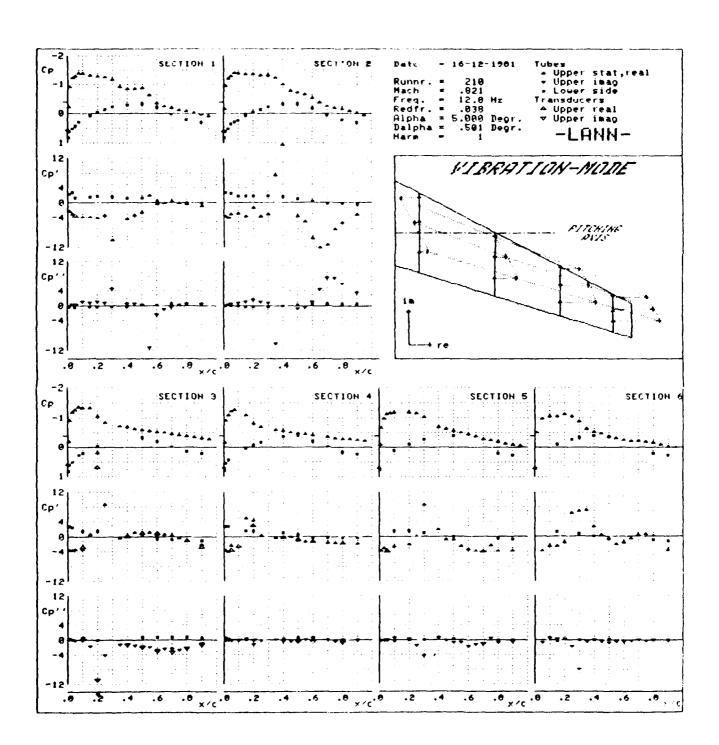


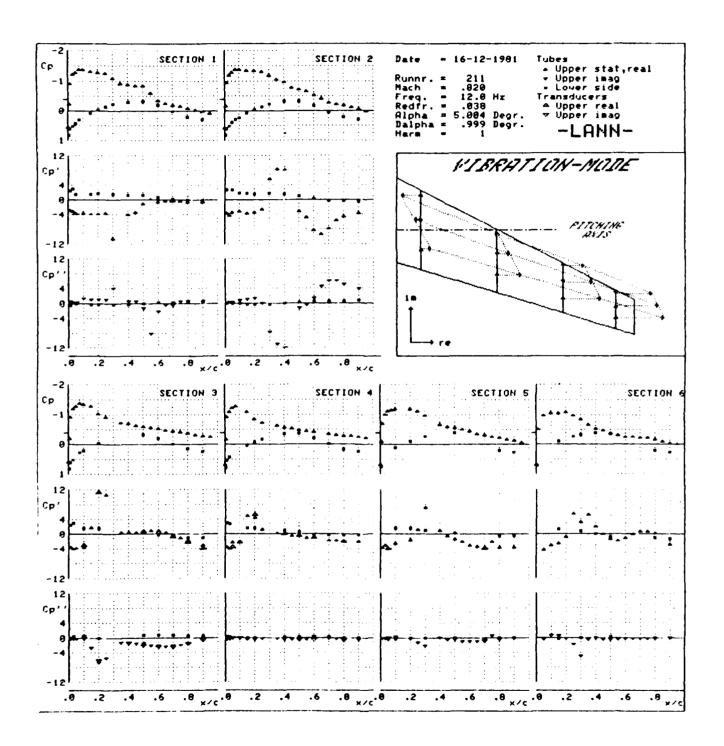


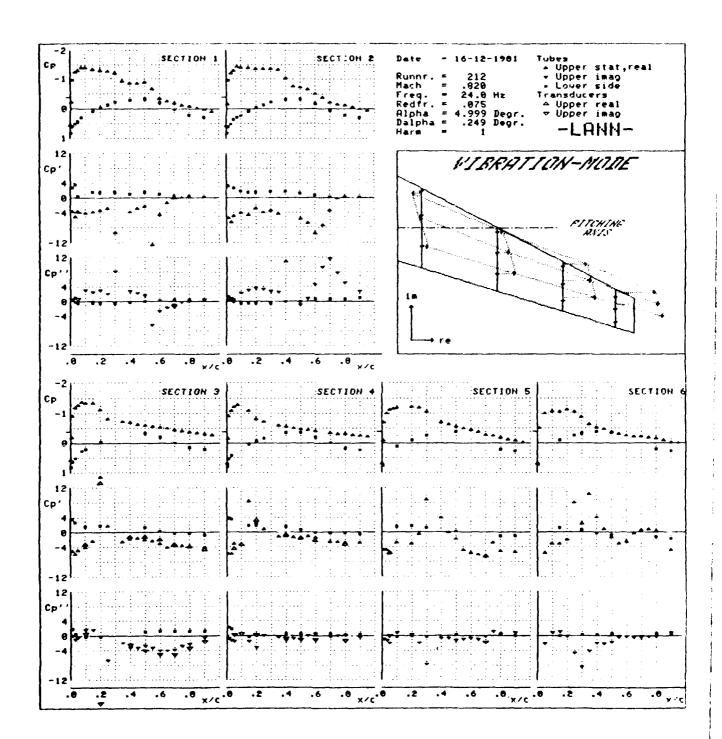


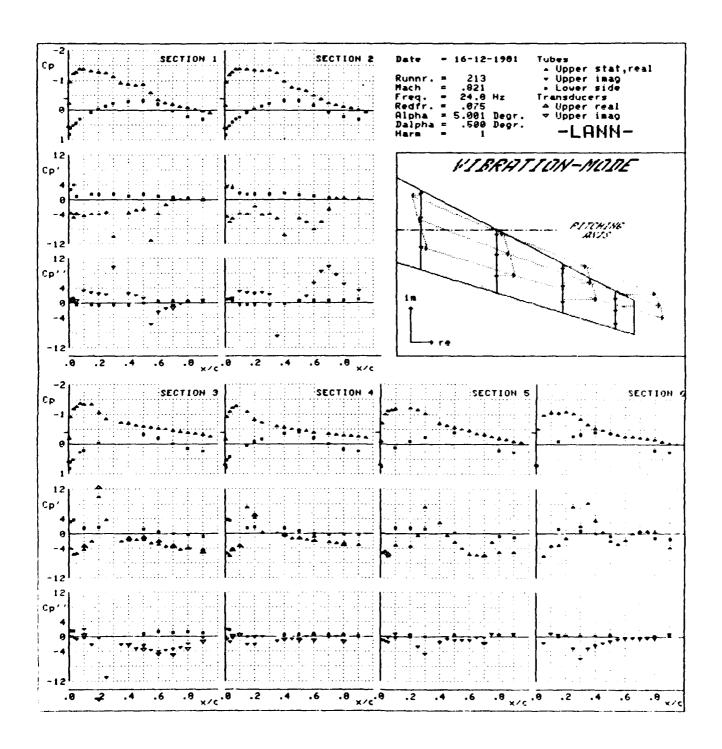


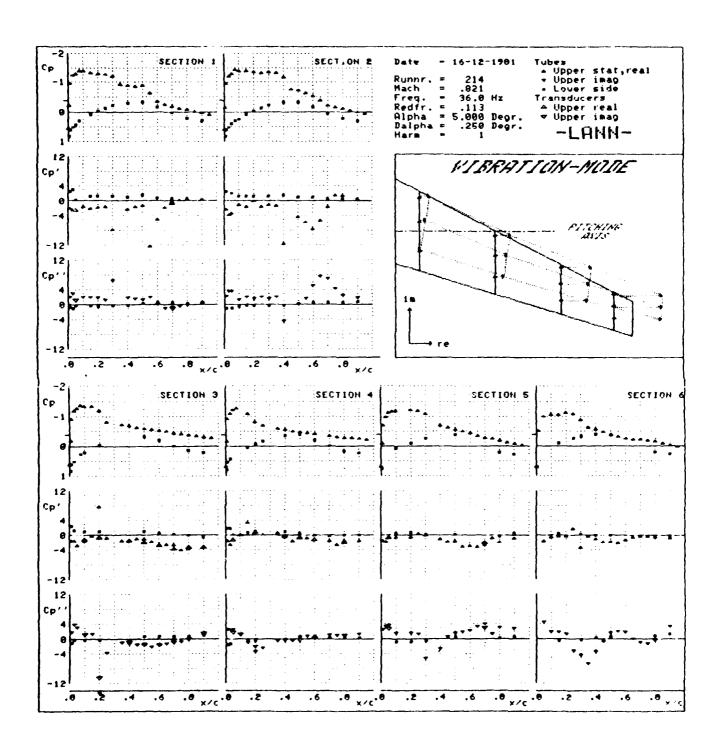


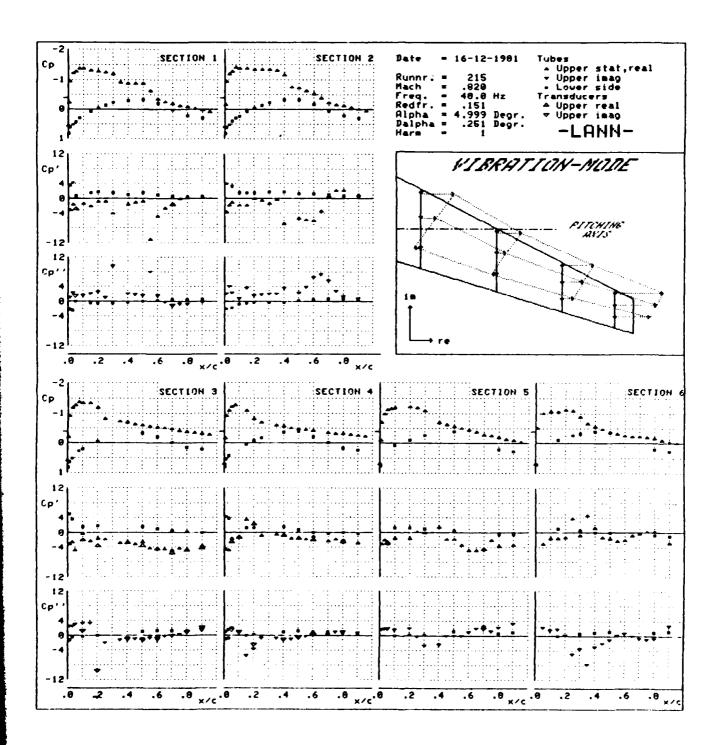


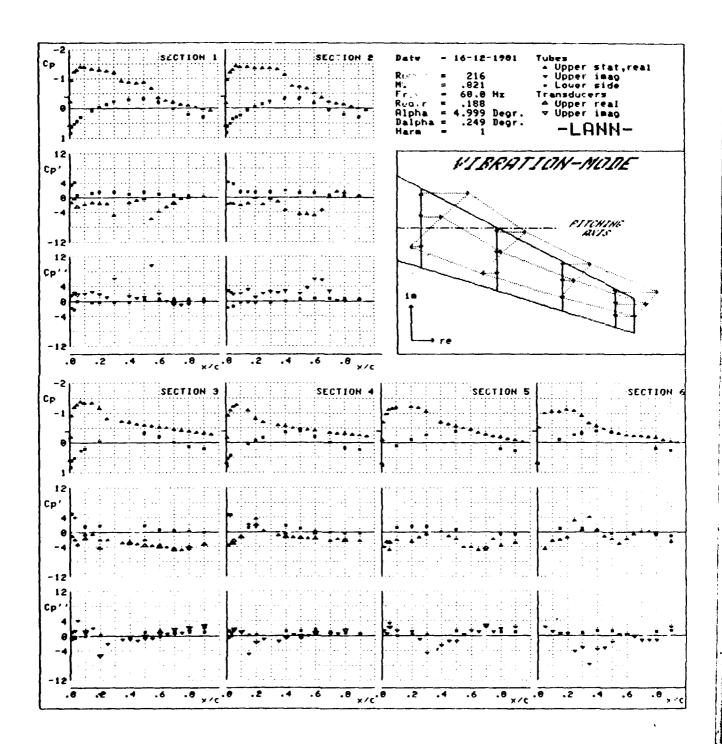


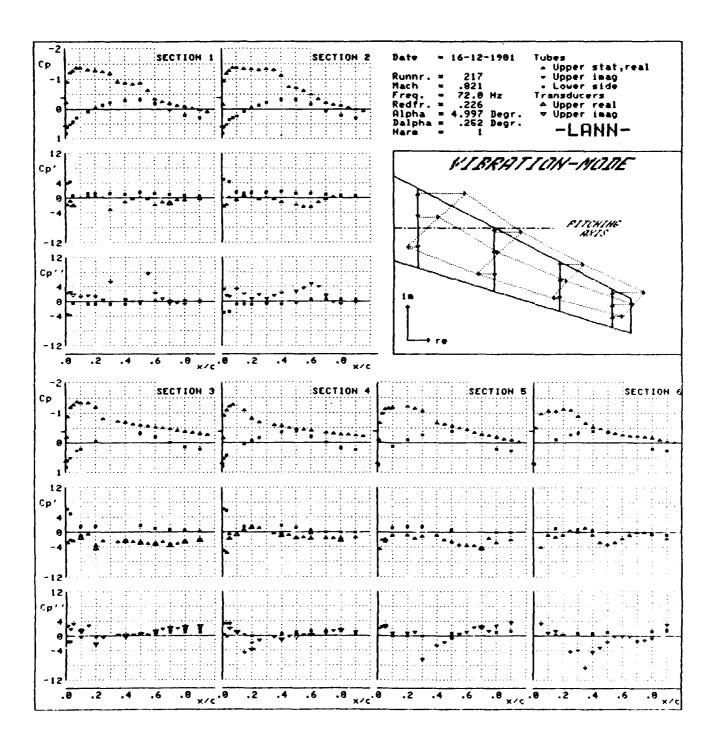


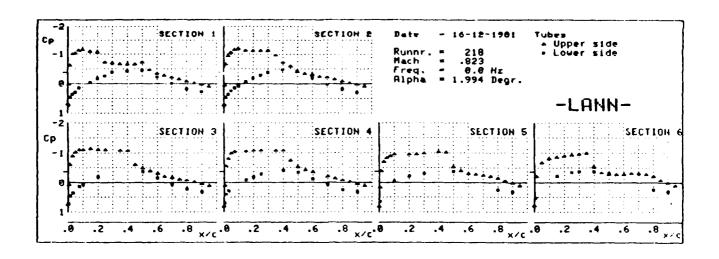


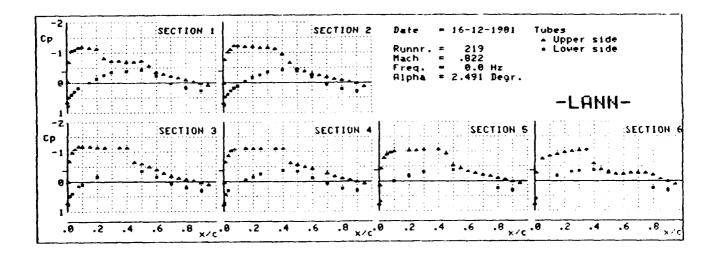


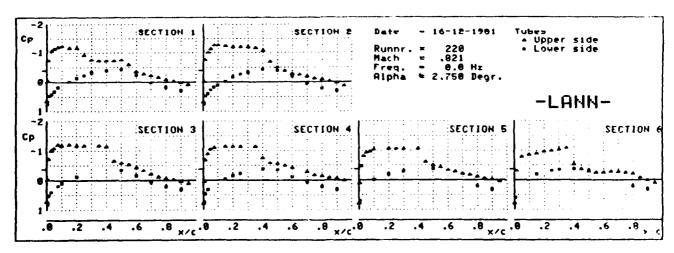


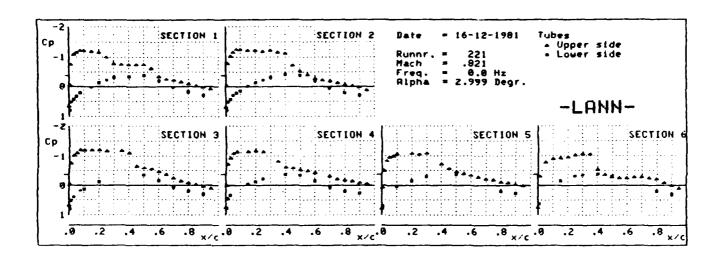


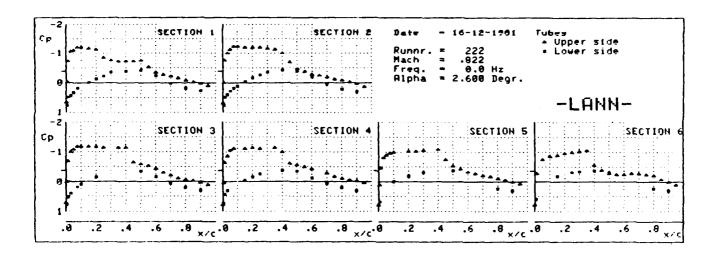


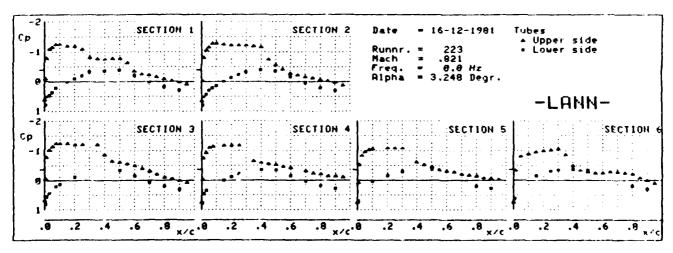


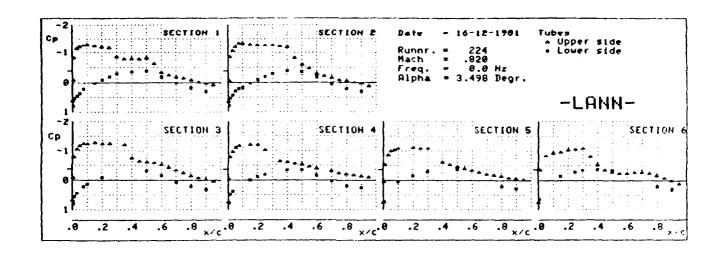


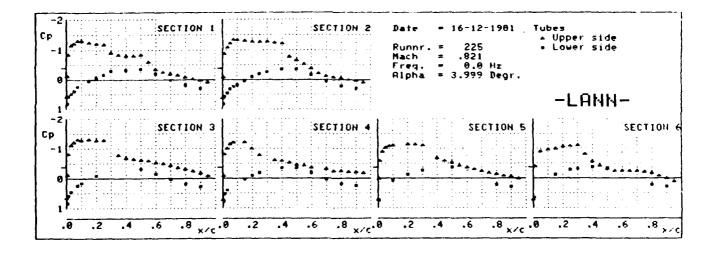


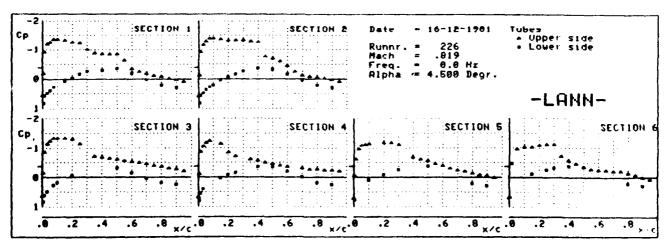


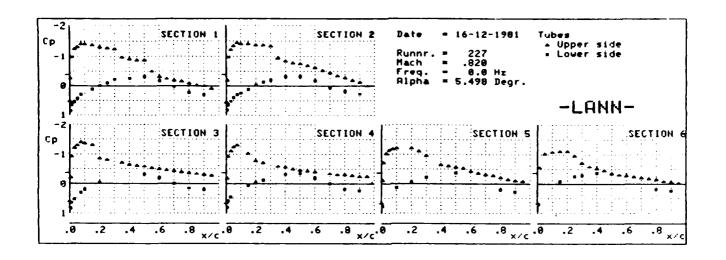


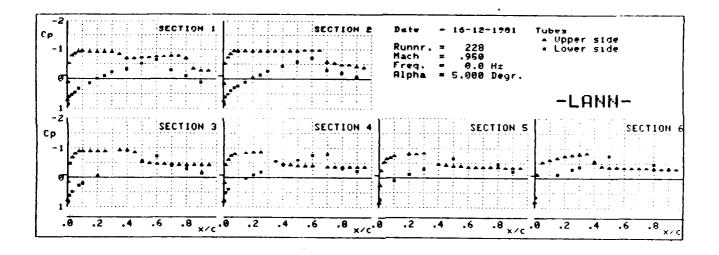


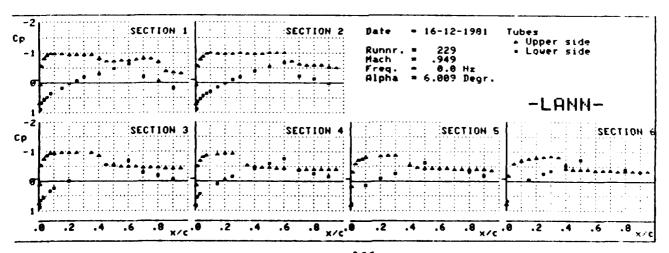


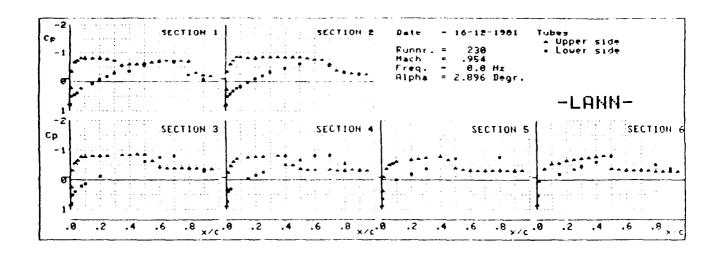


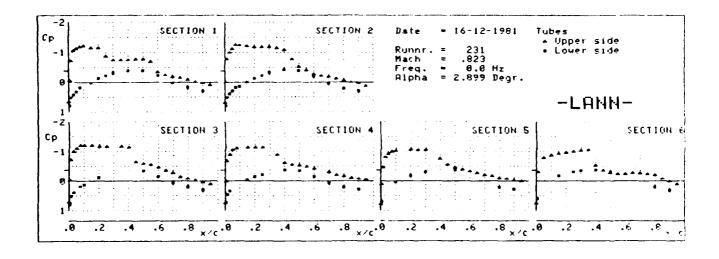


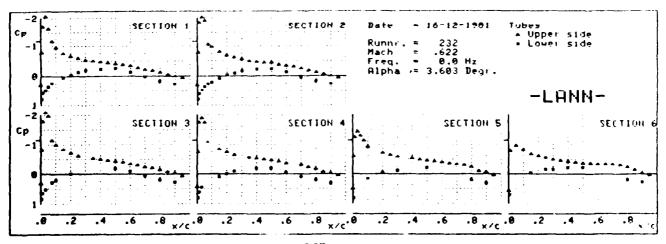


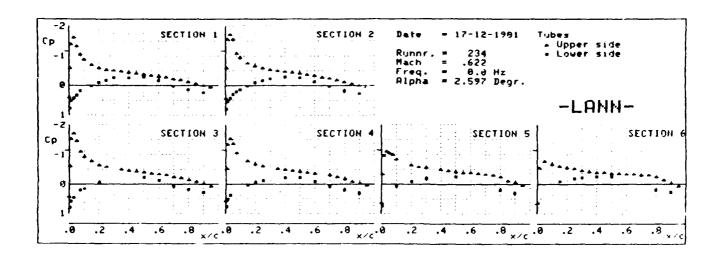


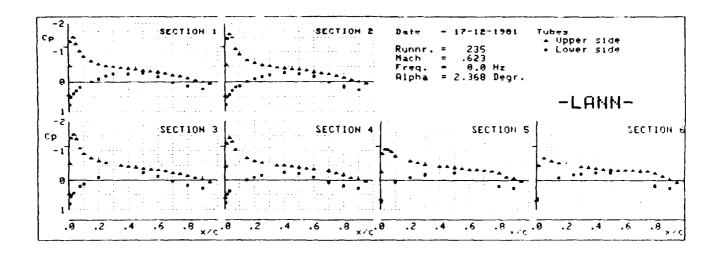


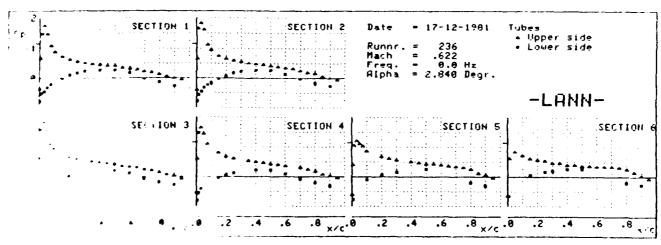


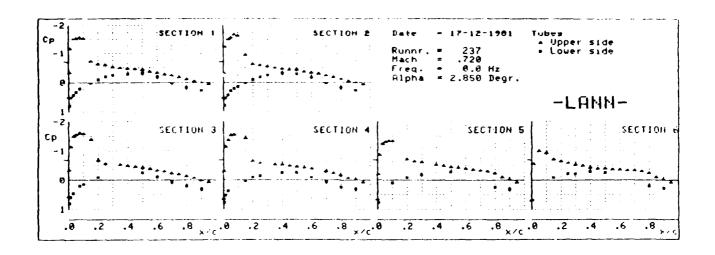


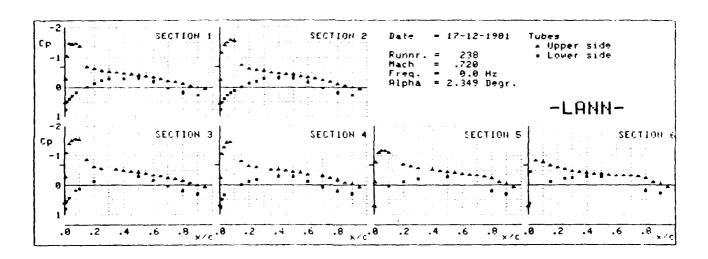


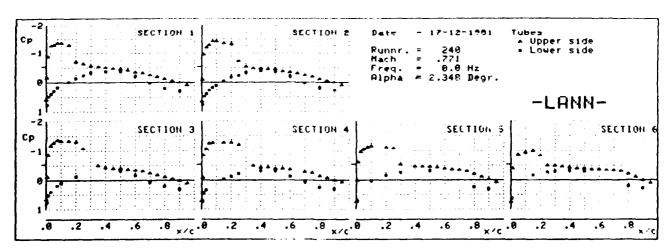


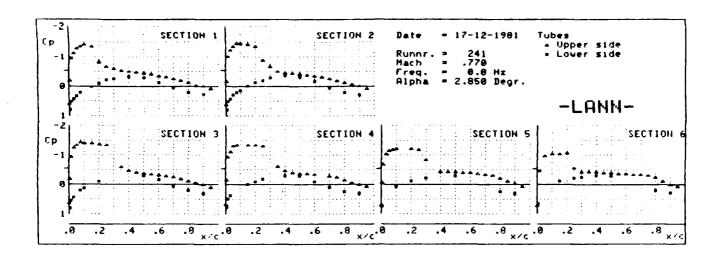


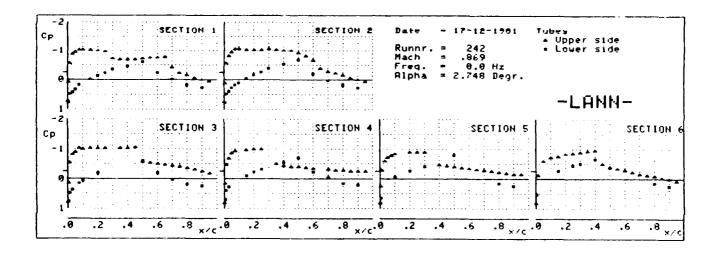


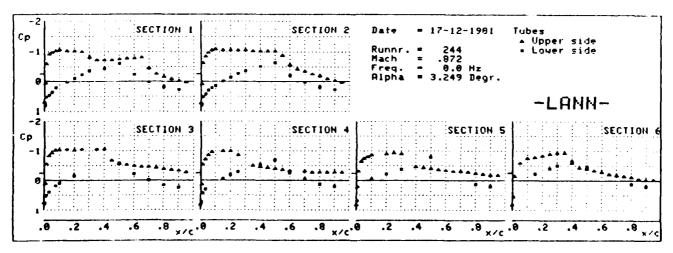


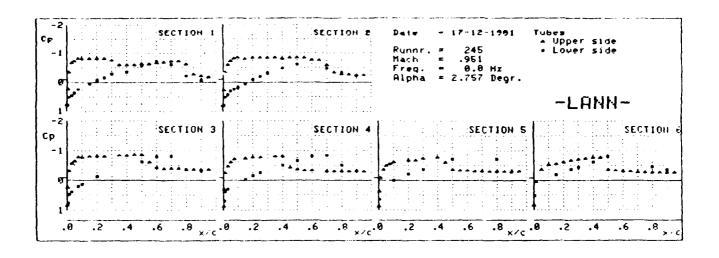


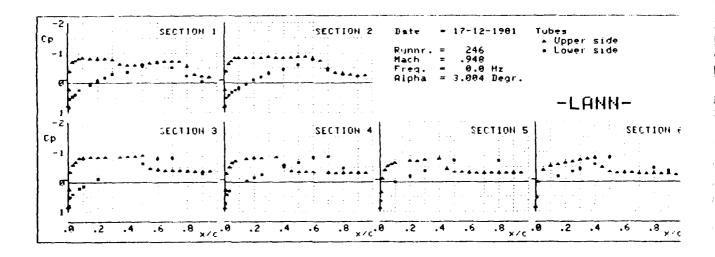


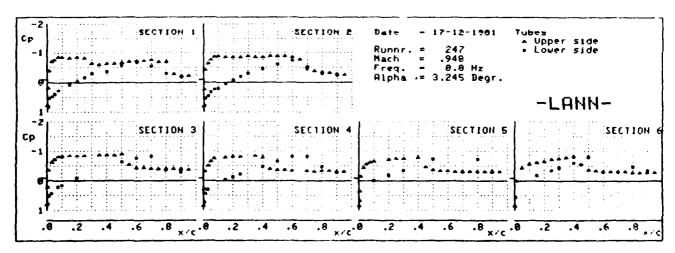


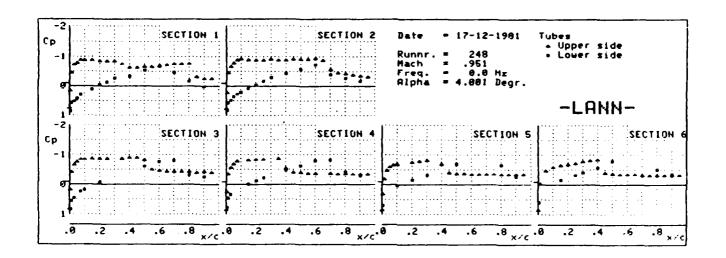


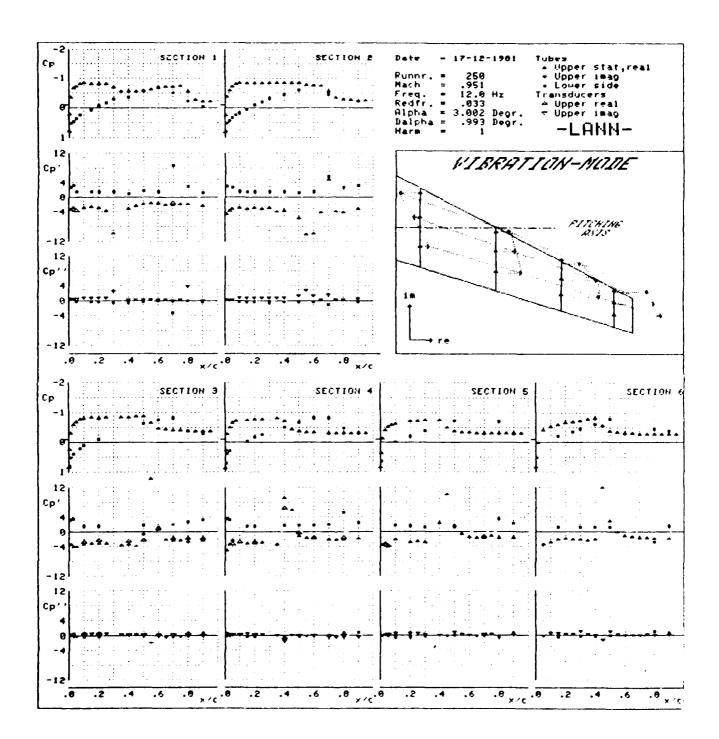


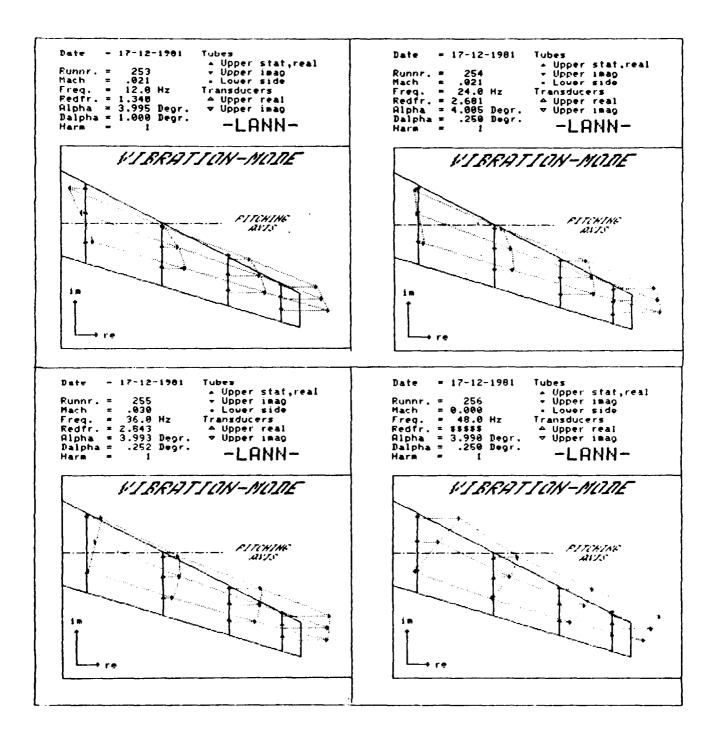


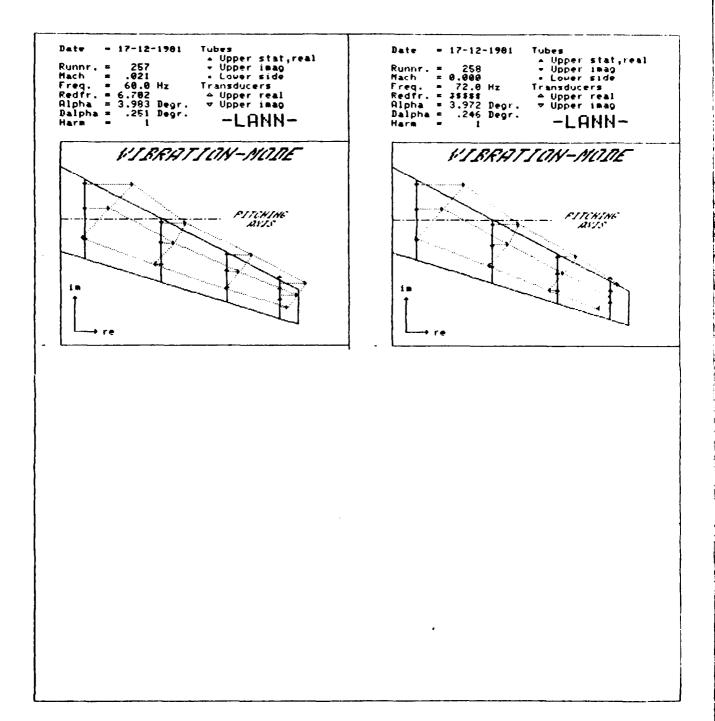




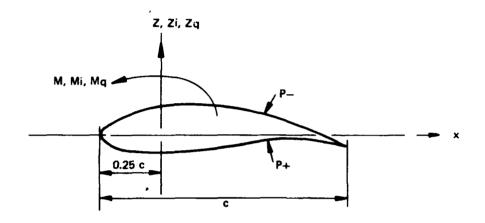








## APPENDIX A Definitions and sign conventions



Note: Coefficients derived from the zeroth harmonic component of unsteady pressure signals, are indicated simply as "steady" coefficients instead of "mean" coefficients. For a pure sinusoidal signal, there is principally no difference between steady and mean coefficients.

## Steady

Steady pressure coefficient:

$$C_{pm} = \frac{p_m^{-p}_{\infty}}{q}$$

Steady sectional normal force:

$$Z = Cz \ q_{\infty} \cdot c \ ; Cz = - \int_{0}^{1} (Cpm_{+} - Cpm_{-})d(\frac{x}{c})$$

Steady sectional pitching moment about quarter-chord

$$M = Cm \ q_{\infty} \cdot c^2 \ ; \ Cm = -\int_{0}^{1} (Cpm_{+} - Cpm_{-})(\frac{x}{c} - 0.25)d(\frac{x}{c})$$

Steady wing normal force:

$$\mathbb{E}_{\text{wing}} = \mathbb{C}_{Z} \cdot q_{\infty} \cdot S$$
;  $\mathbb{C}_{Z} = -\frac{1}{S} \int_{0}^{S} \int_{0}^{1} (Cpm_{+} - Cpm_{-}) d(\frac{x}{c}) \cdot c \cdot dy$ 

Steady wing pitching moment about aerodynamic centre:

$$M_{\text{wing}} = C_{\text{M}} \cdot q_{\infty} \cdot c_{\text{AC}} \cdot S$$
;  $C_{\text{M}} = -\frac{1}{Sc_{\text{AC}}} \int_{0}^{S} \int_{0}^{1} (Cpm_{+} - Cpm_{-})(\frac{x - x_{\text{AC}}}{c})d(\frac{x}{c})c^{2}.dy$ 

## Unsteady

Unsteady pressure coefficient:

$$Cpi = C'_p + i \cdot C''_p = \frac{p_i}{q_{\omega} \cdot \alpha_i}$$

Unsteady sectional normal force:

$$Zi = 2\pi \cdot q_{\infty} \cdot \frac{c}{2} \cdot Czi \cdot \Delta \alpha \cdot e^{i\omega t}$$

$$Czi = Cz' + i \cdot Cz' = -\frac{1}{\pi} \int_{C}^{1} (Cpi_{+} - Cpi_{-})d(\frac{x}{c})$$

Unsteady sectional pitching moment about quarter-chord:

$$\begin{aligned} \text{Mi} &= 2\pi \cdot q_{\infty} \cdot \left(\frac{c}{2}\right)^2 \cdot \text{Cmi} \cdot \Delta \alpha \cdot e^{i\omega t} ; \\ \\ \text{Cmi} &= \text{Cm} + \text{i.cm} = -\frac{2}{\pi} \int_{0}^{1} \left(\text{Cpi}_{+} - \text{Cpi}_{-}\right) \left(\frac{x}{c} - 0.25\right) d\left(\frac{x}{c}\right) \end{aligned}$$

Unsteady wing normal force:

$$Zi_{wing} = 2\pi \cdot q_{\infty} \cdot \frac{S}{2} \cdot C_{Zi} \cdot \Delta \alpha \cdot e^{i\omega t}$$
;  
 $C_{Zi} = C_{Z}^{1} + i \cdot C_{Z}^{"} = -\frac{1}{\pi S} \int_{0}^{S} \int_{0}^{1} (Cpi_{+} - Cpi_{-})d(\frac{x}{c}) \cdot c \cdot dy$ 

Unsteady wing pitching moment about aerodynamic centre:

$$\begin{aligned} \text{Mi}_{\text{wing}} &= 2\pi \cdot q_{\infty} \cdot (\frac{^{\text{c}}_{\text{AC}}}{2}) \cdot \frac{\text{S}}{2} \cdot C_{\text{Mi}} \cdot \Delta \alpha \cdot e^{i\omega t} ; \\ C_{\text{Mi}} &= C_{\text{M}}^{\text{I}} + i \cdot C_{\text{M}}^{\text{II}} = -\frac{2}{\pi \text{Sc}_{\text{AC}}} \int_{0}^{\text{S}} \int_{0}^{1} (C_{\text{pi}} - C_{\text{pi}}) (\frac{x - x_{\text{AC}}}{c}) d(\frac{x}{c}) \cdot c^{2} \cdot dy \end{aligned}$$

## Quasi-steady

Quasi-steady pressure coefficient:

$$Cpq = \frac{P_q}{q_{m}\Delta\alpha}$$

Quasi-steady sectional normal force:

$$Zq = 2\pi \cdot q_{\infty} \cdot \frac{c}{2} Czq \cdot \Delta\alpha$$
;

$$Czq = \frac{1}{\pi} \cdot \frac{Cz(\alpha_m + \Delta\alpha) - Cz(\alpha_m - \Delta\alpha)}{2\Delta\alpha}$$

Quasi-steady sectional pitching moment about quarter-chord:

$$Mq = 2\pi \cdot q_{\infty} \cdot \left(\frac{c}{2}\right)^2 \cdot Cmq \cdot \Delta\alpha$$
;

$$Cmq = \frac{2}{\pi} \cdot \frac{Cm(\alpha_m + \Delta\alpha) - Cm(\alpha_m - \Delta\alpha)}{2\Delta\alpha}$$

Quasi-steady wing normal force:

$$Zq_{\text{wing}} = 2\pi \cdot q_{\infty} \cdot \frac{S}{2} \cdot C_{Zq} \cdot \Delta \alpha$$
;

$$C_{Zq} = \frac{1}{\pi} \cdot \frac{C_Z(\alpha_m + \Delta \alpha) - C_Z(\alpha_m - \Delta \alpha)}{2\Delta \alpha}$$

Quasi-steady wing pitching moment about aerodynamic centre:

$$Mq_{wing} = 2\pi \cdot q_{\infty} \cdot (\frac{^{c}AC}{2}) \cdot \frac{S}{2} \cdot C_{Mq} \cdot \Delta \alpha$$
;

$$C_{Mq} = \frac{2}{\pi} \cdot \frac{C_{M}(\alpha_{m} + \Delta \alpha) - C_{M}(\alpha_{m} - \Delta \alpha)}{2\Delta \alpha}$$

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